



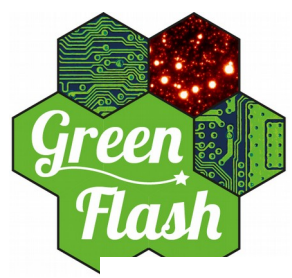
# Efficient supervision strategy for tomographic AO systems on E-ELT



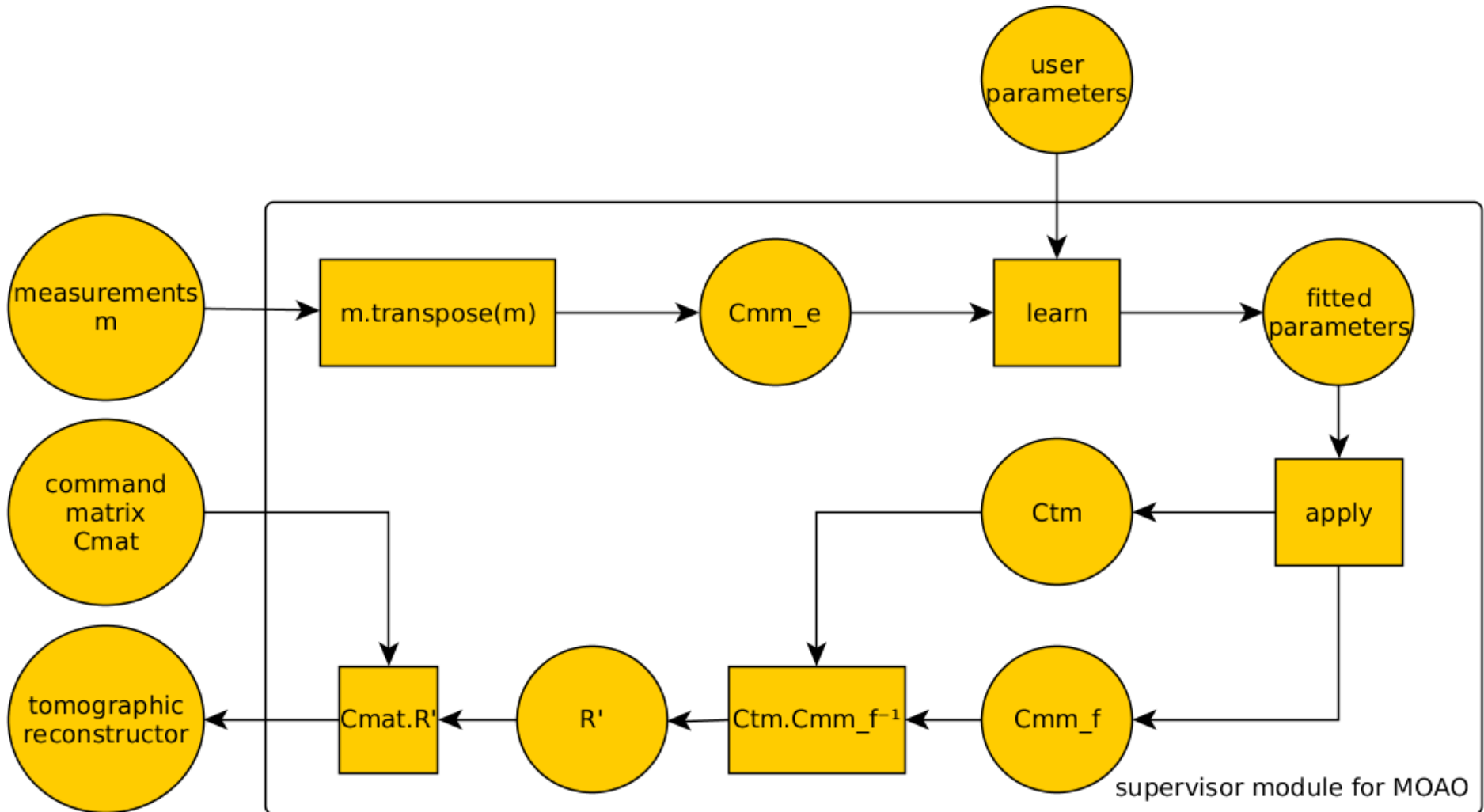


# Efficient supervision strategy for tomographic AO systems on E-ELT

- Supervisor module
- Learn
- Solver
- Improvements



# Supervisor module for MOAO



- Atmospheric parameters from measurements
- Model function  $f$  , possibility to compute independently:
  - element
  - layer

- Score function  $F(x) = \sum_{k=1}^{N^2} [Cmm_k - f_k(x)]^2$



# Learn

## Algorithm 3.16. Levenberg–Marquardt method

**begin**

$k := 0; \quad \nu := 2; \quad \mathbf{x} := \mathbf{x}_0$

$\mathbf{A} := \mathbf{J}(\mathbf{x})^\top \mathbf{J}(\mathbf{x}); \quad \mathbf{g} := \mathbf{J}(\mathbf{x})^\top \mathbf{f}(\mathbf{x})$

$found := (\|\mathbf{g}\|_\infty \leq \varepsilon_1); \quad \mu := \tau * \max\{a_{ii}\}$

**while** (**not** *found*) **and** ( $k < k_{\max}$ )

$k := k+1; \quad \text{Solve } (\mathbf{A} + \mu\mathbf{I})\mathbf{h}_{lm} = -\mathbf{g}$

**if**  $\|\mathbf{h}_{lm}\| \leq \varepsilon_2(\|\mathbf{x}\| + \varepsilon_2)$

$found := \mathbf{true}$

**else**

$\mathbf{x}_{\text{new}} := \mathbf{x} + \mathbf{h}_{lm}$

$\varrho := (F(\mathbf{x}) - F(\mathbf{x}_{\text{new}})) / (L(\mathbf{0}) - L(\mathbf{h}_{lm}))$

**if**  $\varrho > 0$

{step acceptable}

$\mathbf{x} := \mathbf{x}_{\text{new}}$

$\mathbf{A} := \mathbf{J}(\mathbf{x})^\top \mathbf{J}(\mathbf{x}); \quad \mathbf{g} := \mathbf{J}(\mathbf{x})^\top \mathbf{f}(\mathbf{x})$

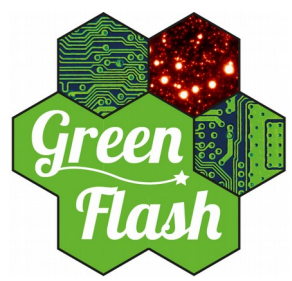
$found := (\|\mathbf{g}\|_\infty \leq \varepsilon_1)$

$\mu := \mu * \max\{\frac{1}{3}, 1 - (2\varrho - 1)^3\}; \quad \nu := 2$

**else**

$\mu := \mu * \nu; \quad \nu := 2 * \nu$

**end**



# Learn

$$J_{ij} = \frac{\partial f_i}{\partial x_j} \quad \forall (i, j) \in \llbracket 1, N^2 \rrbracket \times \llbracket 1, np \rrbracket$$

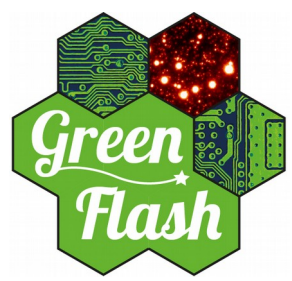
$$H = J^T \cdot J$$

$$g = J^T \cdot (Cmm - f(x))$$

$$H_{i,j} = \sum_{k=1}^{N^2} \frac{\partial f_k}{\partial x_i} \cdot \frac{\partial f_k}{\partial x_j}$$

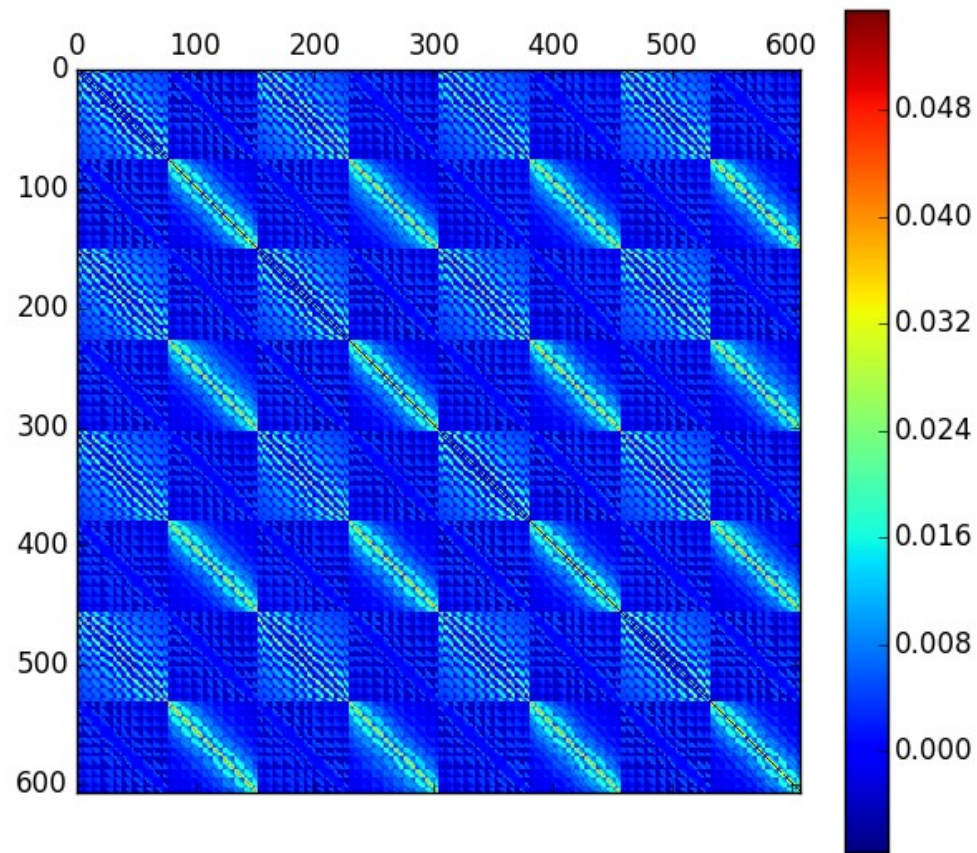
$$g_i = \sum_{k=1}^{N^2} \frac{\partial f_k}{\partial x_i} \cdot (Cmm_k - f_k(x))$$

- Parameters bind to layers



# Learn

- Approximation by removing XY components

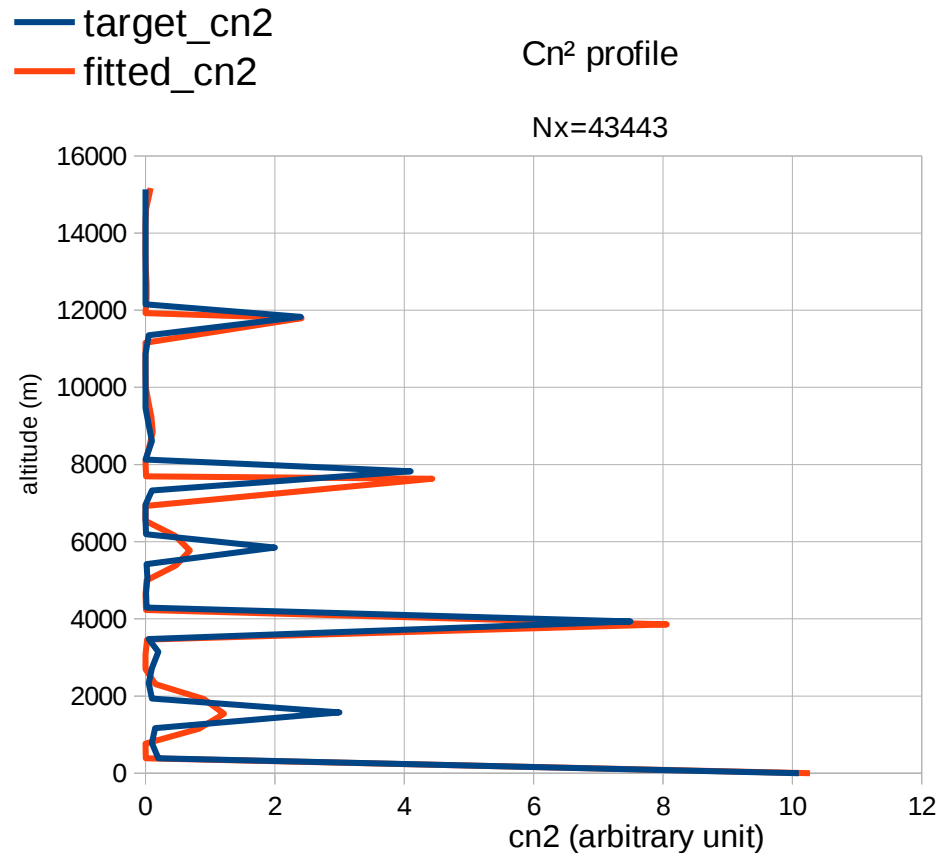






# Learn

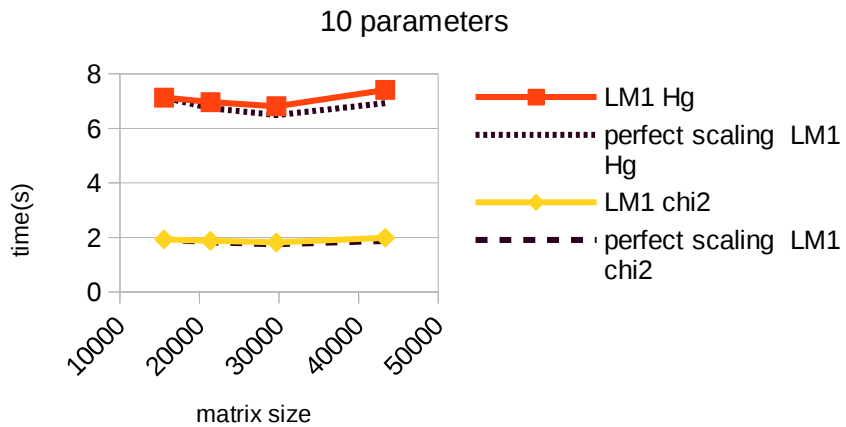
- 2 LM (5 layers, 40 layers)
- Profile score=3.08 ( $\text{sum}(\text{Cmm}^2)=27500$ )



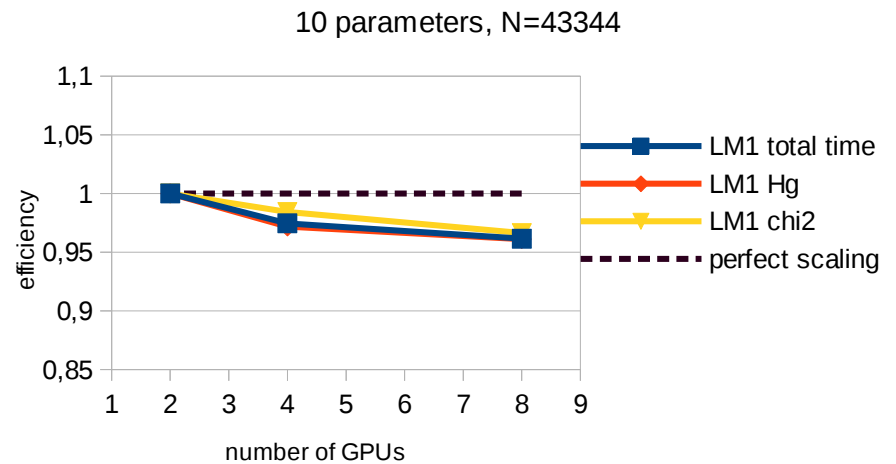


- Intel(R) Xeon(R) CPU E5-2620 v3 @ 2.40GHz + 4 Tesla K80
- First LM : 150s    Second LM : 1303 s

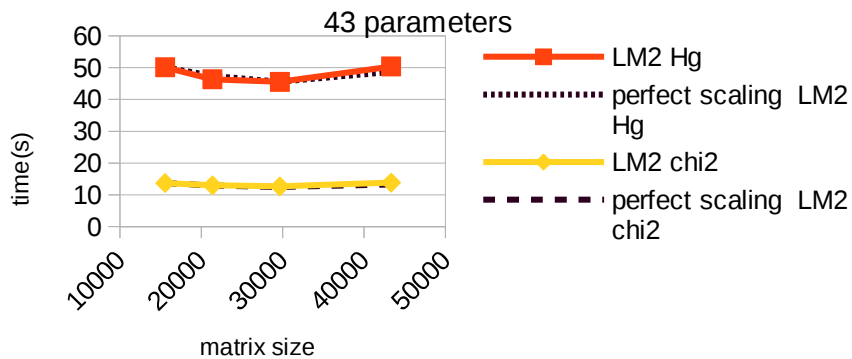
Weak scaling for the first LM



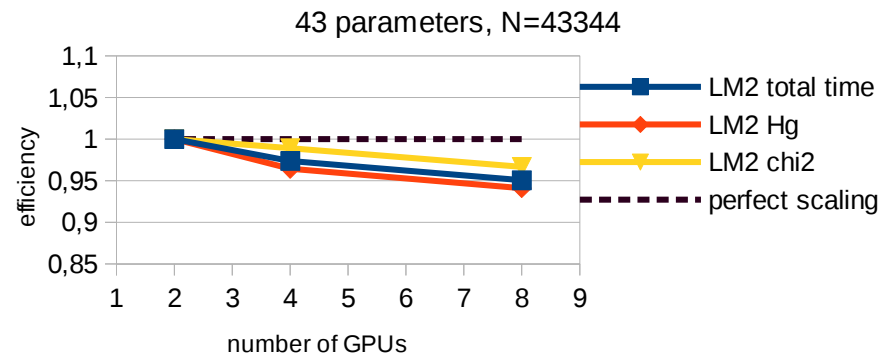
strong scaling for the first LM



Weak scaling for the second LM



strong scaling for the second LM

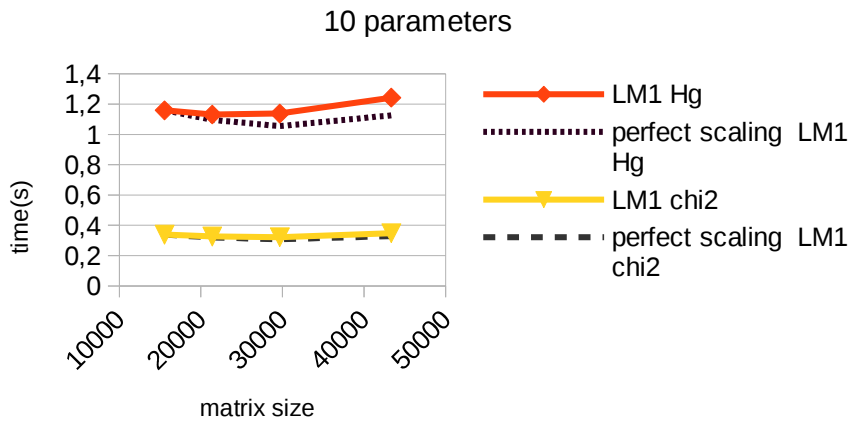




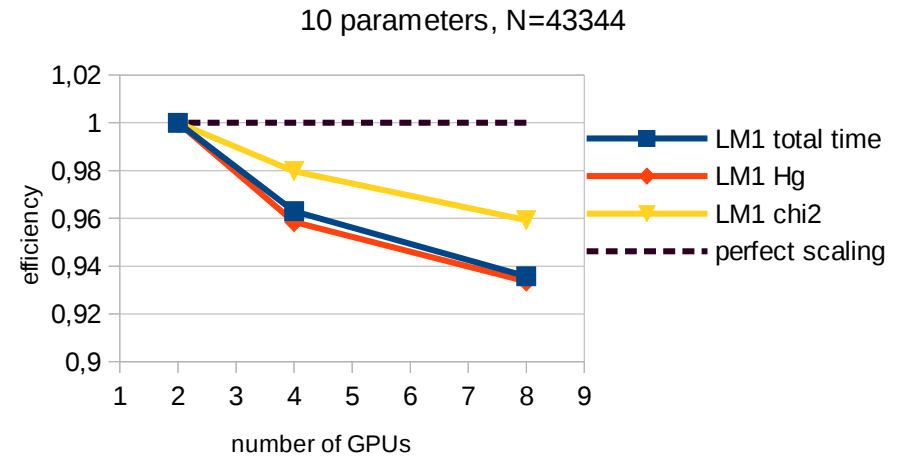
# Learn

- Intel(R) Xeon(R) CPU E5-2698 v4 @ 2.20GHz + 8 P100
- First LM : 25.5s    Second LM : 213,8s

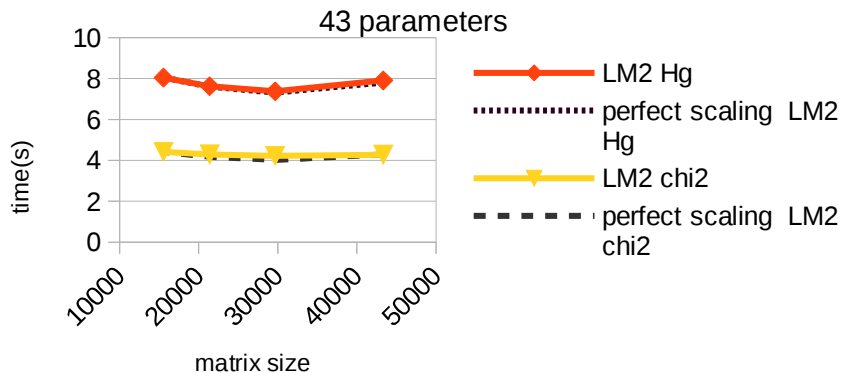
Weak scaling for the first LM



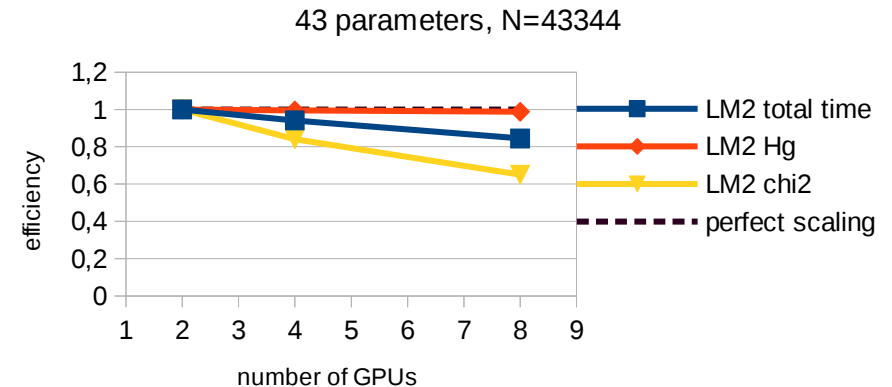
strong scaling for the first LM



Weak scaling for the second LM



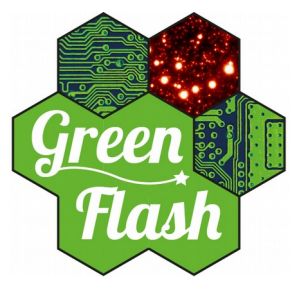
strong scaling for the second LM





# Solver

- Generate matrices  $C_{tm}$  and  $C_{mm_f}$
- $R' = C_{tm} \cdot C_{mm_f}^{-1}$
- posv solve  $A \cdot x = B$
- Decompose posv
  - potrf
  - trsm
  - trsm



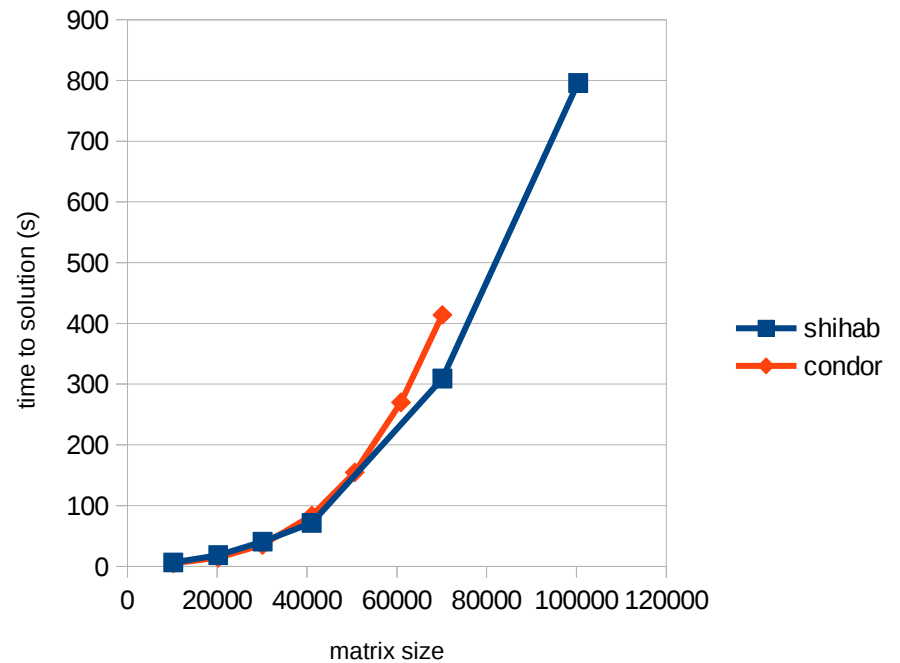
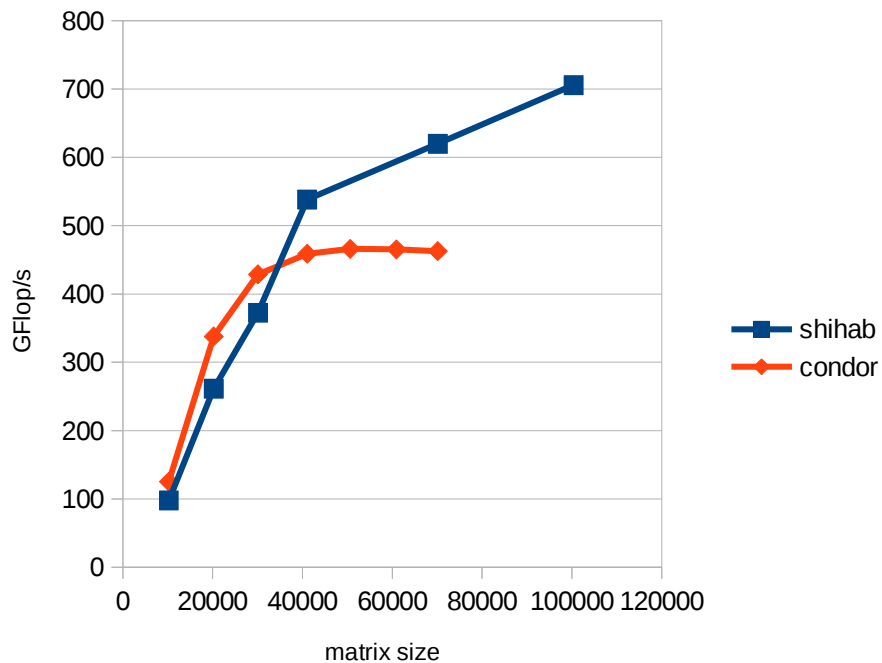
# Solver

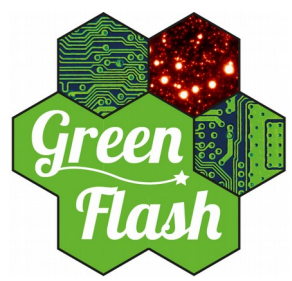
- Implementation with multiple libraries
  - LAPACK
  - PLASMA
  - Chameleon
- Several architectures
  - CPU Two sockets eighteen-cores Intel Haswell E5-2699 v3 @ 2.30GHz (shihab)
  - KNL One socket 64 cores Intel(R) Xeon Phi(TM) CPU 7210 @ 1.30GHz (condor)
  - GPU
    - Two sockets ten-cores Intel Ivy Bridge E5-2680 v2 @ 2.80GHz + 2K40
    - Intel(R) Xeon(R) CPU E5-2698 v4 @ 2.20GHz + 8 P100



# Solver

- Validation of the results against yorick application
- performance

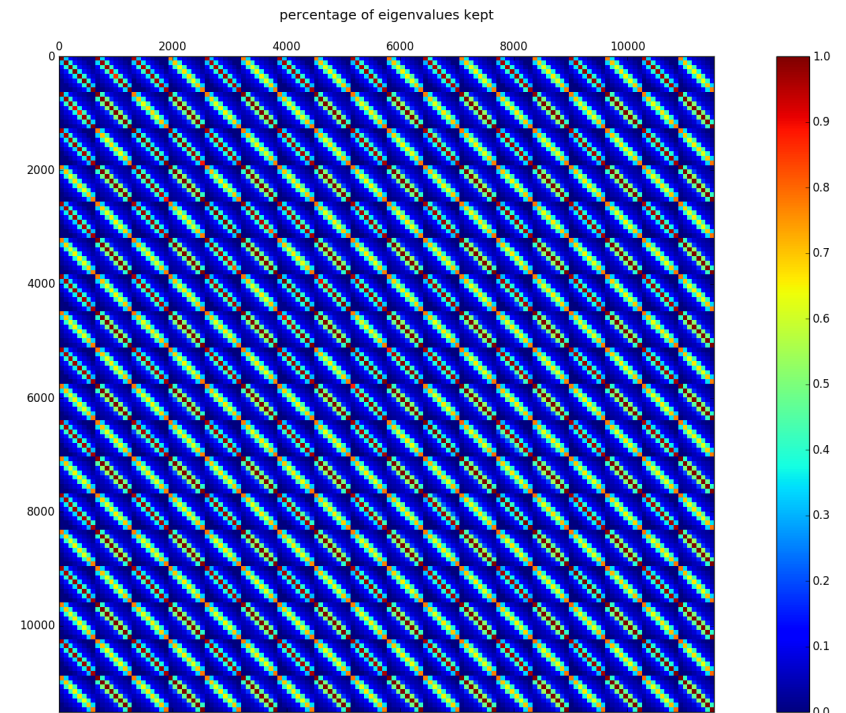




# Improvements

- Hierarchical matrices
  - Hierarchy of blocks
  - Data sparse (low rank blocks)
  - Singular values decomposition

- Compression up to 80 %
- Faster matrix generation
- H-matrix in solver ?





Thank you

