

RayGal relativistic ray-tracing (Michel-Andrès Breton)

+

e-MANTIS emulator (Iñigo Sáez-Casares PhD)

=>

Yann RASERA

LUTH/Univ. Paris Cité /Obs. de Paris /PSL/CNRS/IUF

April 23rd, 2024

The ProGraceRay Project: PRObing GRAvity at Cosmological scales with relativistic RAY-tracing

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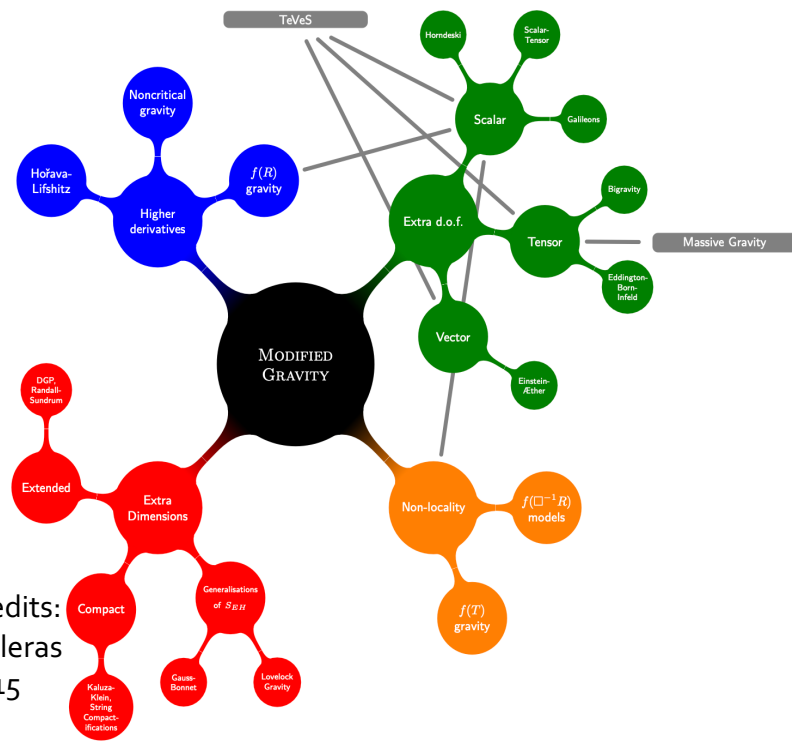
April 23rd, 2024

The ProGraceRay Team

Partner	Name	First name	Current position	Role & responsibilities in the project (4 lines max)	Involvement (p.month)
LUTH Paris Observatory <u>Meudon</u>	RASERA	Yann	Associate professor	Coordinator , Tasks 1.1, 1.2, 3.1, 3.2, 4.1-4.4, 5.1, 5.3, 5.4	44p.month
	CORASANITI	Pier-Stefano	CNRS Researcher	Tasks 1.1,1.2,3.1, 3.2, 4.4, 5.4	12p.month
	ROY	Fabrice	Research Engineer	Tasks 1.1,1.2, 3.1,3.2	18p.month
	LE BRUN	Amandine	CNRS Researcher	Tasks 1.1, 1.2, 2.1-2.3, 3.1, 3.2, 5.4	12p.month
	REVERDY	Vincent	CNRS Researcher	Tasks 3.1,3.2	12p.month
	SAEZ-CASARES	<u>lǎjao</u>	PhD student	Tasks 1.1,1.2, 5.1, 5.2	10p.month
	<u>Postdoc 1: To be recruited</u>		Postdoctoral Researcher	Tasks 1.1,1.2, 3.1	24p.month
IAP CNRS Paris	DUBOIS	Yohan	CNRS Researcher	Partner's leader Tasks 2.1-2.3, 5.3, 5.4	10p.month
	LAVAUX	<u>Guilhem</u>	CNRS Researcher	Tasks 2.1-2.3	10p.month
	COLOMBI	Stéphane	CNRS Researcher	Tasks 1.1, 1.2, 2.1-2.3	6p.month
	CUSIN	Giulia	CNRS Researcher	Tasks 1.1, 3.1, 5.3	6p.month
	PEIRANI	Sébastien	CNRS Researcher	Tasks 2.1-2.3	8p.month
	SAGA	Shohei	Postdoctoral Researcher	Tasks 5.2	5p.month
	<u>Postdoc 2: To be recruited</u>		Postdoctoral Researcher	Tasks 2.1-2.3	24p.month
AIM CEA <u>Saclay</u> Gif sur Yvette	PIRES	Sandrine	Engineer-Researcher	Partner's leader Tasks 4.1, 4.3, 4.4, 5.4	14p.month
	CODIS	Sandrine	CNRS Researcher	Tasks 4.3, 4.4, 5.2, 5.3	6p.month
	<u>Postdoc 3: To be recruited</u>		Postdoctoral Researcher	Tasks 4.1- 4.4	12p.month
LAM Aix-Marseille University Marseille	DE LA TORRE	Sylvain	Assistant Astronomer	Partner's leader Tasks 4.2, 4.3, 4.4, 5.2, 5.3, 5.4	12p.month
	JULLO	Eric	Assistant Astronomer	Tasks 4.3, 4.4, 5.2, 5.3, 5.4	10p.month
	<u>Postdoc 3: To be recruited</u>		Postdoctoral Researcher	Tasks 4.3-4.4, 5.2-5.4	12p.month
EXTERNAL					
ICE-CSIC-IEEC (Spain)	BRETON	<u>Michel-Andr�s</u>	Postdoctoral Researcher	External member Tasks 3.1-3.2, 4.2	5p.month
YITP/Kyoto University (Japan)	TARUYA	Atsushi	Associate professor	External member Tasks 4.2, 4.3, 4.4, 5.2, 5.3, 5.4	6p.month

BACKGROUND

WHAT IS THE NATURE OF GRAVITY AT COSMOLOGICAL SCALES?



Lovelock theorem of General Relativity:
 From a **local gravitational action** which contains only **second derivatives** of the **four-dimensional space-time metric**, then the only possible equations are Einstein-field equations



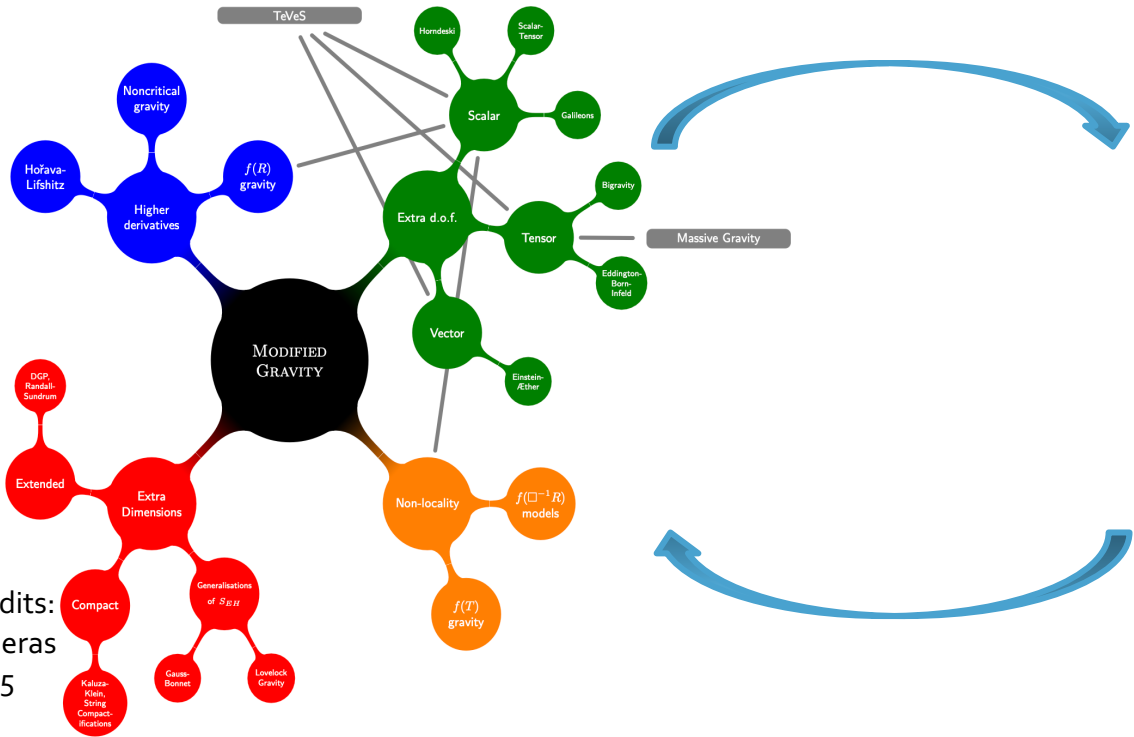
Modified gravity according to Lovelock theorem

1. **Non-locality** (or emergence) : no local action
2. **Higher-derivatives**: more than 2nd derivatives
3. **Extra-dimensions** : more than 4D
4. **Extra degrees of freedom**: scalar, vector and/or tensor

Modified gravity theories

Credits:
Trilleras
2015

WHAT IS THE NATURE OF GRAVITY AT COSMOLOGICAL SCALES?



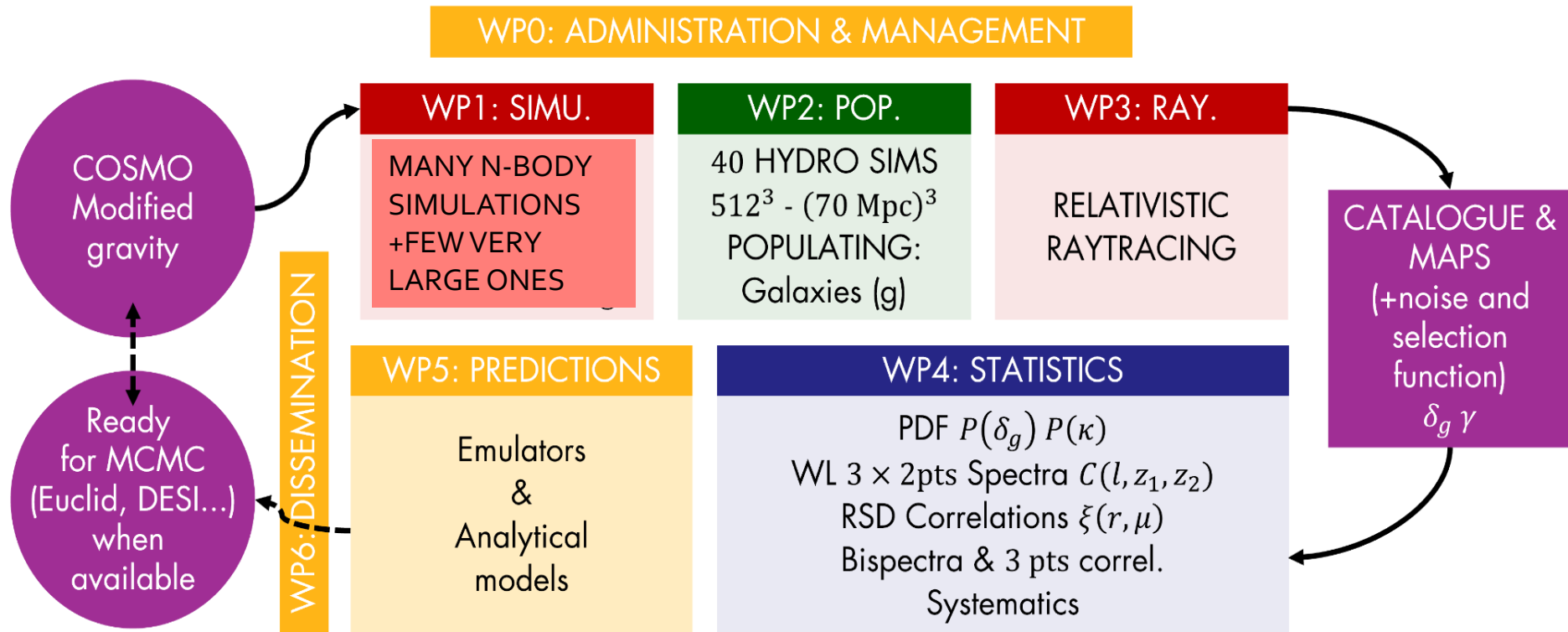
Modified gravity theories



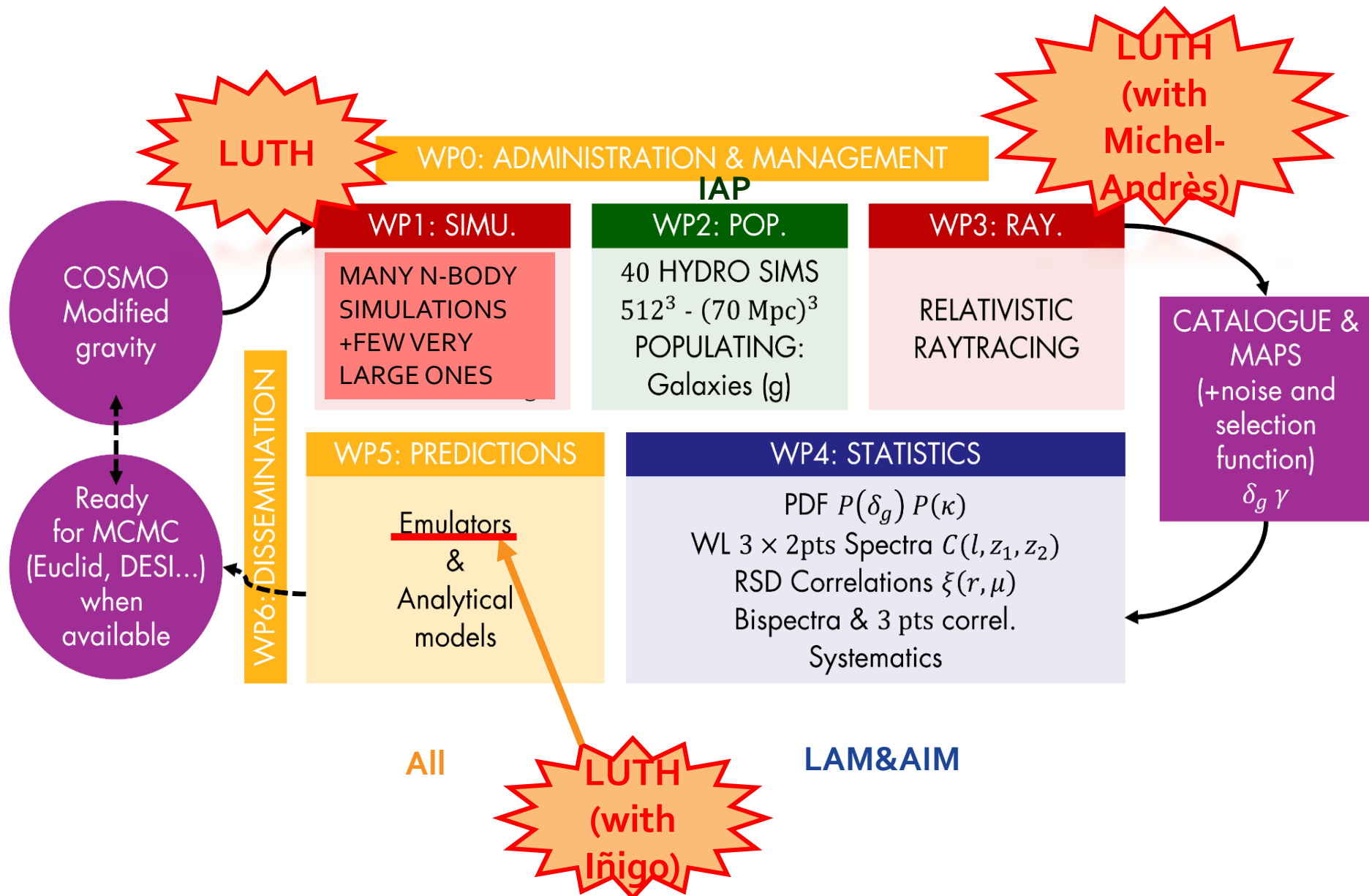
Large-Scale Structure surveys

METHODS

ORGANISATION OF THE WORK

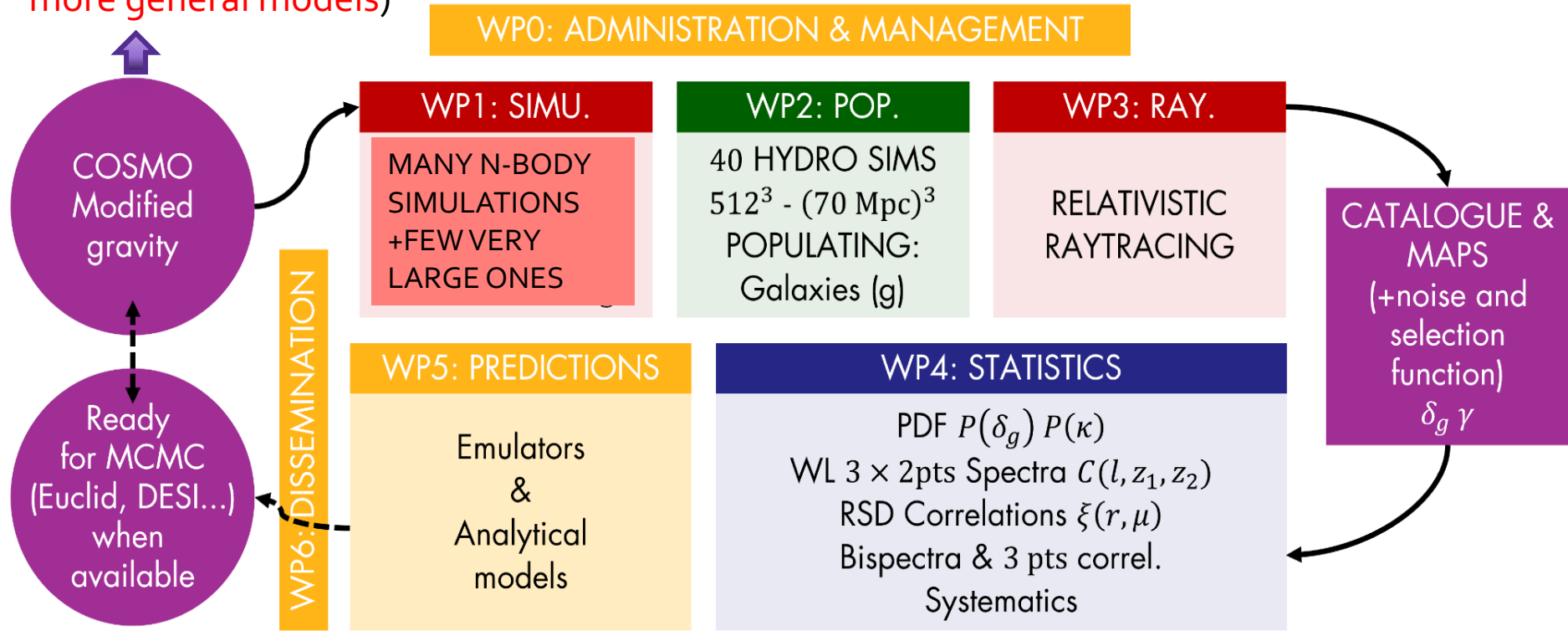


ORGANISATION OF THE WORK

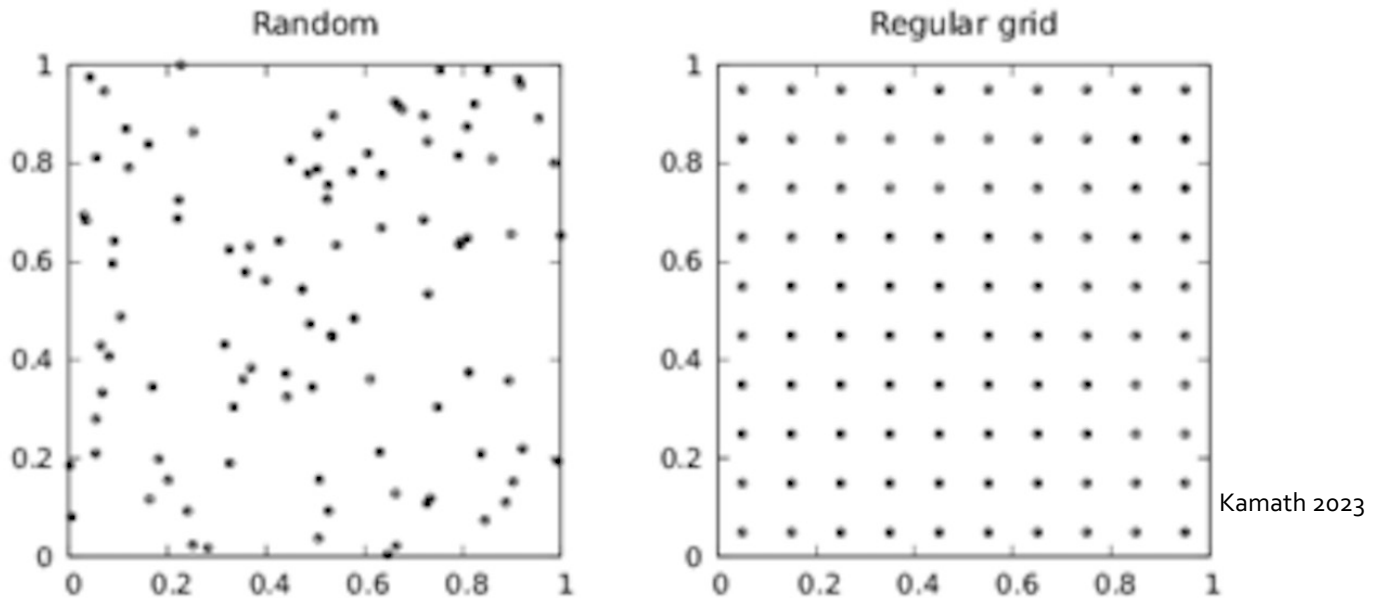


CHOOSING THE DARK ENERGY TYPE

- (e.g. Λ -CDM, w -CDM, $f(R)$ -CDM, more general models)
 - Cold Dark Matter+ cosmological constant (STANDARD MODEL $w=-1$)
 - CDM+ fluid of dark energy with equation of state $w \neq -1$ (Iñigo&MAB)
 - CDM+ $f(R)$ Hu&Sawicki modified gravity (Iñigo)
 - Cold Dark Matter+ more generic modified gravity (ProGraceRay)

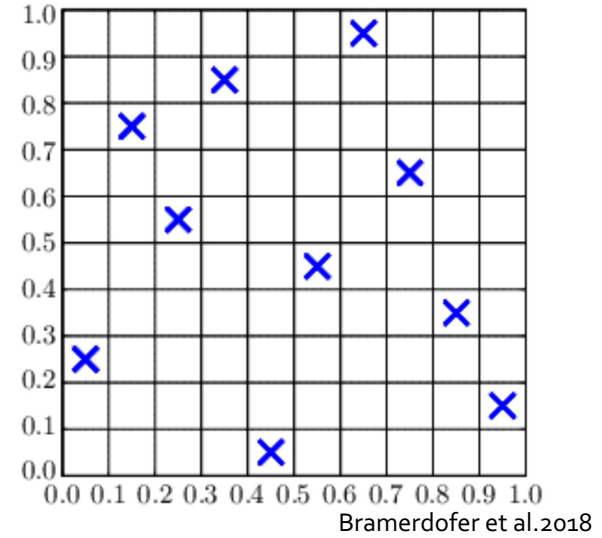
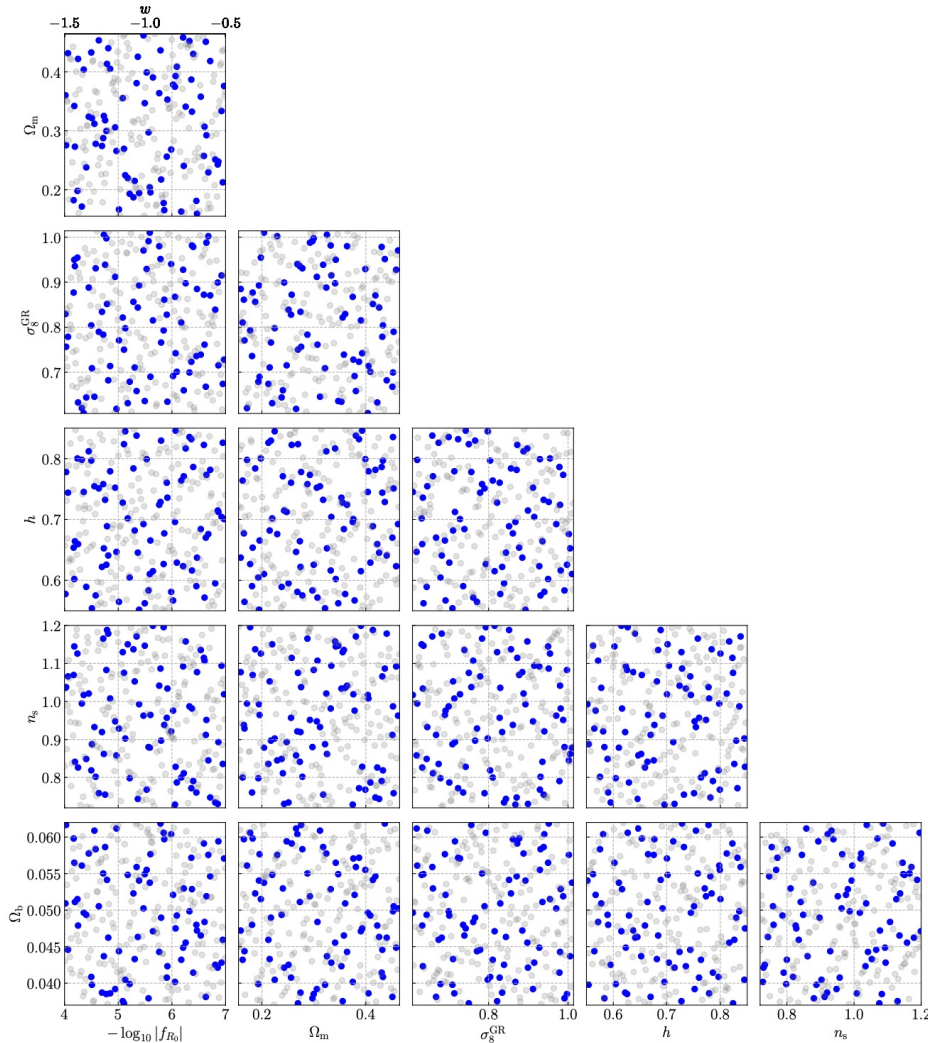


RANDOM OR GRID SAMPLING OF THE PARAMETER SPACE



- Cosmological inference in 5D (at least) => needs $\sim 10^5$ accurate predictions
- 1 cosmological N-body simulation => $\sim 10^4$ h (for 512^3 part. in modified gravity)
- Total time => 10^9 h => TOO MUCH CPU TIME!!!!

LATIN HYPERCUBE SAMPLING OF THE PARAMETER SPACE



« Sudoku-like sampling »

Since the statistics are smooth :

- Needs $\sim 20 \times \text{NDIM}$ points ~ 100 models to capture all the (cross-)derivatives
- Needs 10^6 h \Rightarrow THIS IS POSSIBLE!

Sáez-Casares et al., submitted to A&A, 2024

ACCURATE MODEL OF LARGE-SCALE STRUCTURE FORMATION IN GR

METHODS

GR INITIAL CONDITIONS: COMPOSITION AND DISTRIBUTION OF COMPONENTS

Gaussian

(+ GR $a(t)$
Background)

Weak-field GR

DYNAMICS OF GRAVITATIONAL INTERACTION

DYNAMICS OF DARK MATTER

DYNAMICS OF DARK ENERGY

Non relativistic
GR
geodesics

*Vlasov-Poisson:
Cold Dark Matter*

Λ

NON-LINEARITIES

ANALYTICAL PERTURBATIVE

(I.E.

SEMI-ANALYTICAL

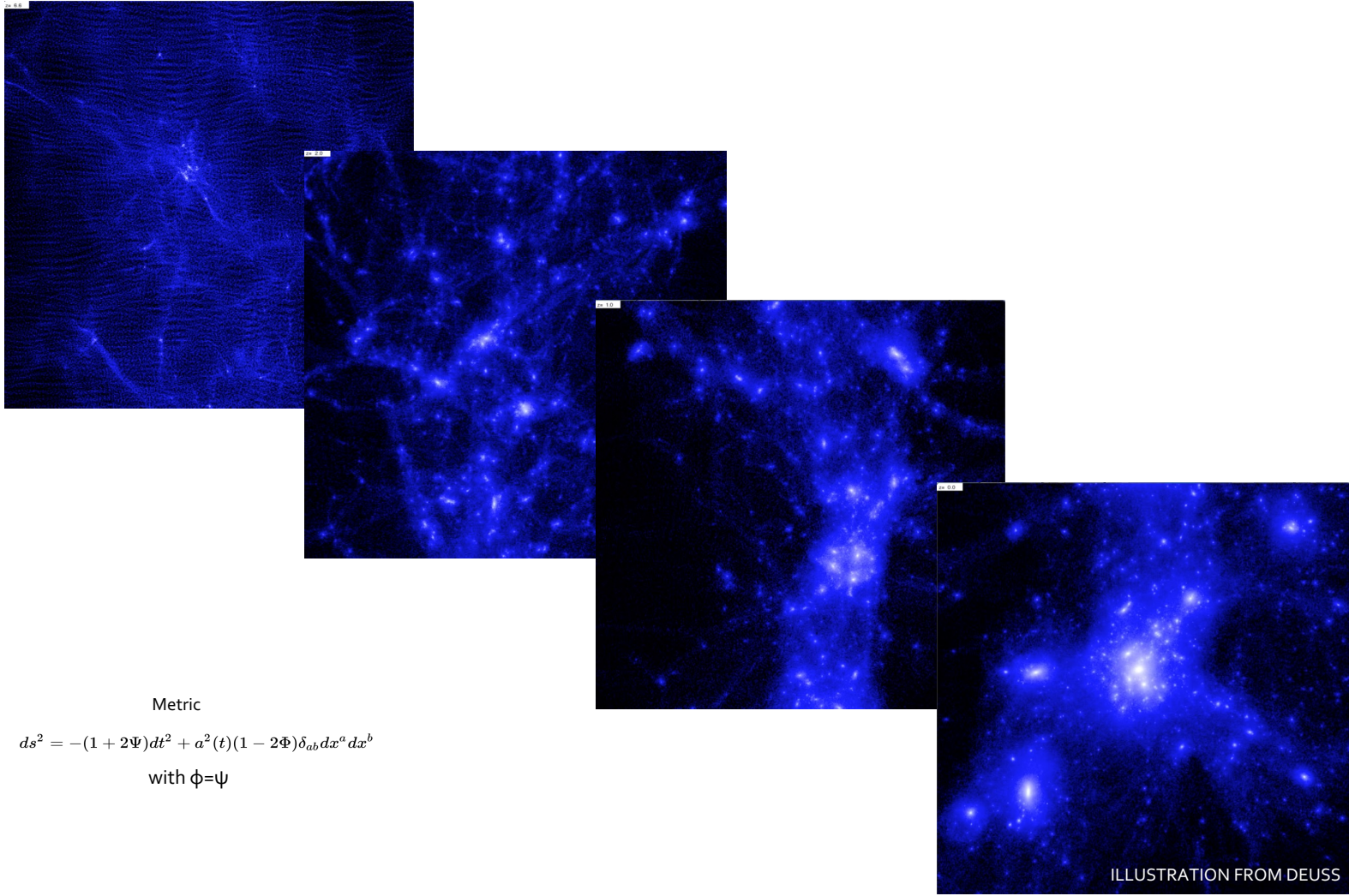
NUMERICS (SIMULATIONS)

Metric

$$ds^2 = -(1 + 2\Phi)dt^2 + a^2(t)(1 - 2\Phi)\delta_{ab}dx^a dx^b$$

with $\phi=\psi$

GR INITIAL CONDITIONS: COMPOSITION AND DISTRIBUTION OF COMPONENTS



NON-LINEARITIES

ANALYTICAL PERTURBATIVE
(I.E. SEMI-ANALYTICAL
NUMERICS (SIMULATIONS))

Metric

$$ds^2 = -(1 + 2\Psi)dt^2 + a^2(t)(1 - 2\Phi)\delta_{ab}dx^a dx^b$$

with $\Phi = \Psi$

GR INITIAL CONDITIONS: COMPOSITION AND DISTRIBUTION OF COMPONENTS

EXAMPLE

Name	Model(s)	$L_{\text{box}} [h^{-1}\text{Mpc}]$	N_{part}	$m_{\text{part}} [(\Omega_{\text{m}}/0.3071) h^{-1} M_{\odot}]$	N_{real}	N_{cosmo}
L328_M10_wcdm	wCDM	328.125	512^3	$2.25 \cdot 10^{10}$	64	80
L656_M11_wcdm	wCDM	656.25	512^3	$1.79 \cdot 10^{11}$	64	80
L328_M10_frcdm	$f(R)$ CDM	328.125	512^3	$2.25 \cdot 10^{10}$	8	80
L656_M11_frcdm	$f(R)$ CDM	656.25	512^3	$1.79 \cdot 10^{11}$	8	80
L328_M9_wcdm	wCDM	328.125	1024^3	$2.81 \cdot 10^9$	1	16
L656_M10_wcdm	wCDM	656.25	1024^3	$2.25 \cdot 10^{10}$	1	16
L328_M10_P18	P18	328.125	512^3	$2.25 \cdot 10^{10}$	384	1
L328_M10_w12	w12	328.125	512^3	$2.25 \cdot 10^{10}$	64	1
L328_M10_F5	F5	328.125	512^3	$2.25 \cdot 10^{10}$	64	1
L164_M10	P18, F5, F6	164.0625	256^3	$2.25 \cdot 10^{10}$	1	3
L164_M9	P18, F5, F6	164.0625	512^3	$2.81 \cdot 10^9$	1	3
L164_M8	P18	164.0625	1024^3	$3.51 \cdot 10^8$	1	1

The wCDM and f(R)CDM
e-MANTIS simulation suite
 Sáez-Casares et al., 2023
 Sáez-Casares et al., submitted to A&A, 2024

We combine:

- several universe realizations
- several mass resolutions
- several simulation volumes

=> to increase the effective dynamical range



ACCURATE MODEL OF LARGE-SCALE STRUCTURE FORMATION IN GR

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GR INITIAL CONDITIONS: COMPOSITION AND DISTRIBUTION OF COMPONENTS

Gaussian

(+ GR $a(t)$
Background)

Weak-field GR

SOURCES OF LIGHT

DYNAMICS OF MESSENGERS

*Relativistic
GR geodesics: photons*

OBSERVER

Metric
 $ds^2 = -(1 + 2\Psi)dt^2 + a^2(t)(1 - 2\Phi)\delta_{ab}dx^a dx^b$
with $\Phi = \Psi$

NON-LINEARITIES

ANALYTICAL PERTURBATIVE

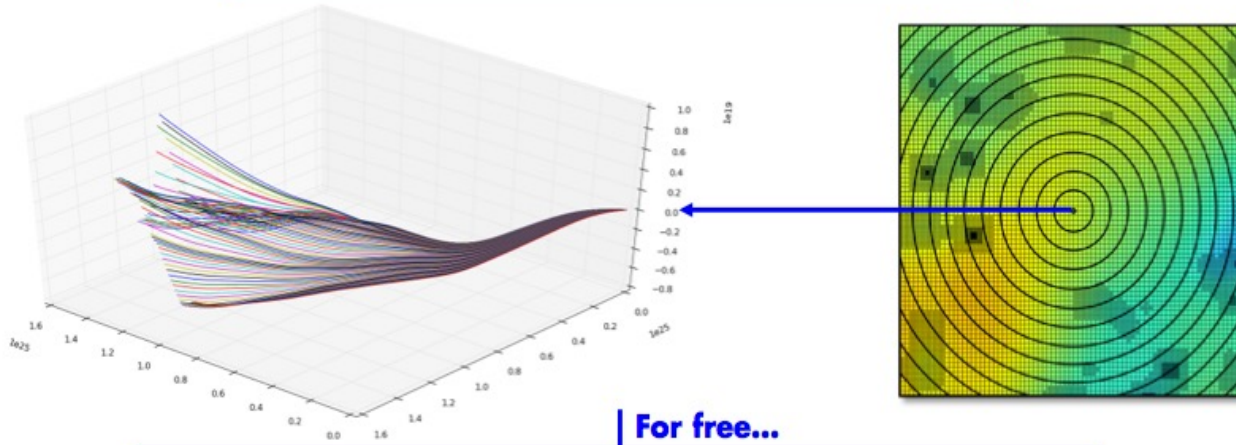
(I.E.

SEMI-ANALYTICAL

NUMERICS (SIMULATIONS)

GR INITIAL CONDITIONS: COMPOSITION AND DISTRIBUTION OF COMPONENTS

3D backward raytracing



For free...

**Weak lensing
(convergence & shear)**

A 2D heatmap showing convergence and shear patterns, with a grid of lines overlaid to illustrate the lensing effect.

Integrated Sachs-Wolfe

A 3D diagram showing light rays passing through a gravitational well, illustrating the Integrated Sachs-Wolfe effect.

**Luminosity distance
Angular distance
Redshift distortions
Time delays
...**

A diagram showing a light cone with a grid of lines, representing various cosmological distances and time delays.

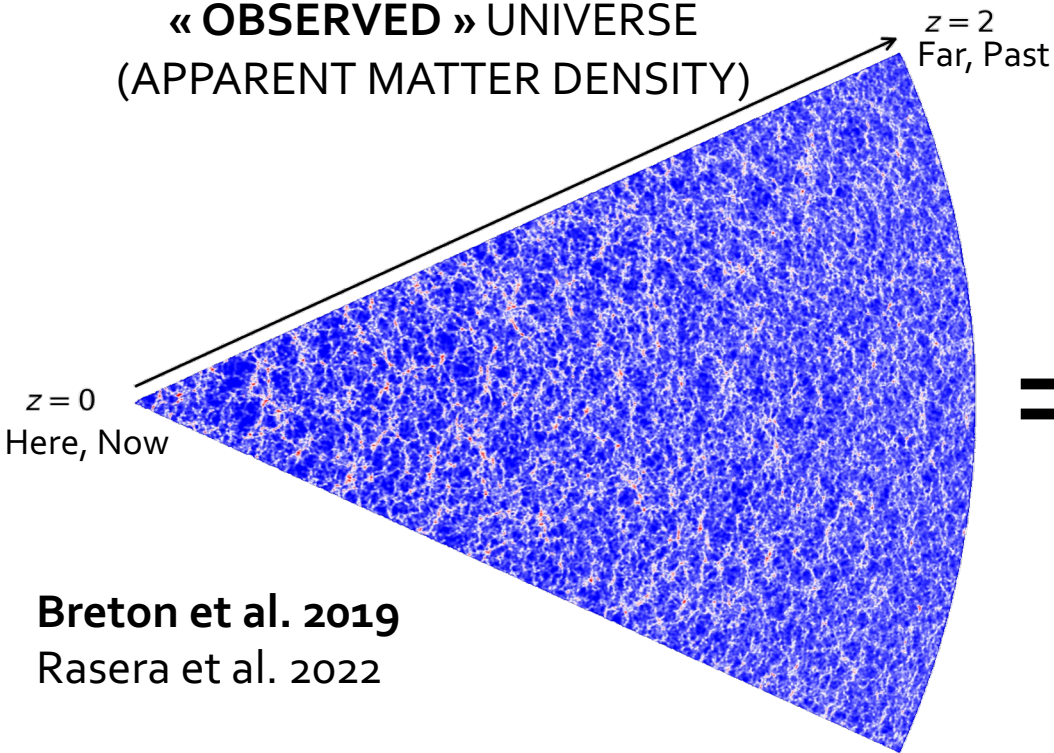
NON-LINEARITIES

ANALYTICAL PERTURBATIVE (I.E. SEMI-ANALYTICAL NUMERICS (SIMULATIONS))

ds^2

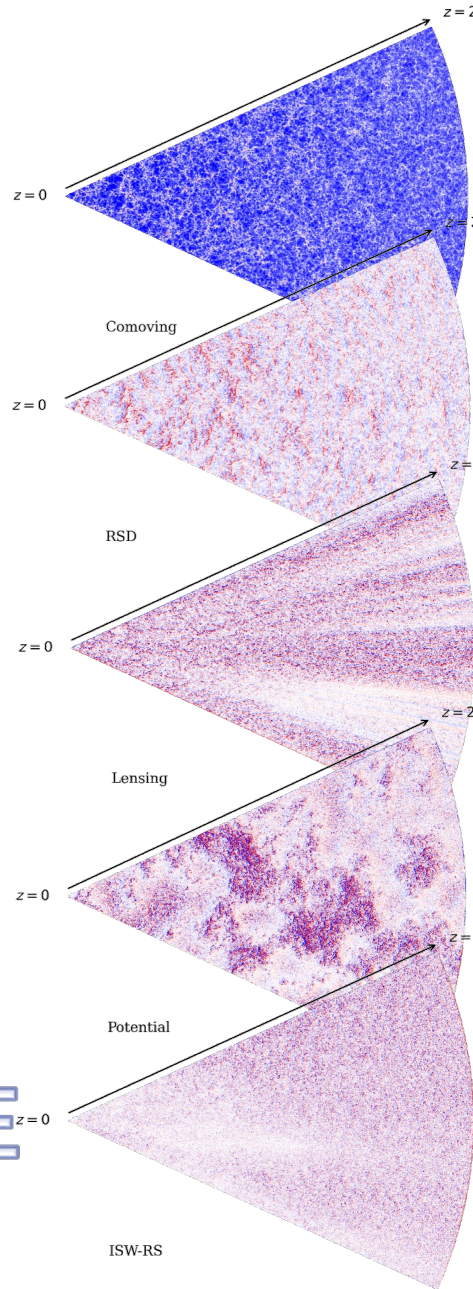
EXAMPLE

SIMULATION
OF A SLICE OF THE
« **OBSERVED** » UNIVERSE
(APPARENT MATTER DENSITY)



Breton et al. 2019
Rasera et al. 2022

=



« TRUE »
UNIVERSE

+

DOPPLER
EFFECT

+

WEAK
LENSING

+

GRAVITATIONAL
REDSHIFT

+

INTEGRATED
SACHS WOLFE
EFFECT

THE RAYGAL UNIVERSE

70 billion particles \Rightarrow cosmic structure formation
1 billion photons \Rightarrow general relativistic effects

(type « **RayGal data** » on any search engine)

Rem: #of sims to be increased in ProGraceRay->emulator

ACCURATE MODEL OF LARGE-SCALE STRUCTURE FORMATION IN GR

METHODS

GR INITIAL CONDITIONS: COMPOSITION AND DISTRIBUTION OF COMPONENTS

Gaussian

(+ GR $a(t)$
Background)

Weak-field GR

DYNAMICS OF GRAVITATIONAL INTERACTION

DYNAMICS OF DARK MATTER

SOURCES OF LIGHT

DYNAMICS OF DARK ENERGY

Non relativistic GR geodesics

Vlasov-Poisson: Cold Dark Matter

Λ

NON-LINEARITIES

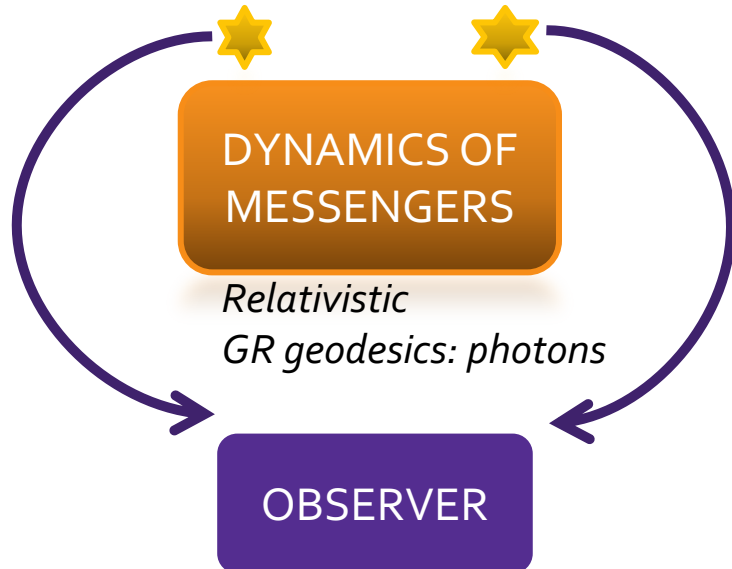
ANALYTICAL PERTURBATIVE

(I.E.

SEMI-ANALYTICAL

NUMERICS (SIMULATIONS)

Metric
 $ds^2 = -(1 + 2\Phi)dt^2 + a^2(t)(1 - 2\Phi)\delta_{ab}dx^a dx^b$
with $\phi=\psi$



DYNAMICS OF MESSENGERS

Relativistic GR geodesics: photons

OBSERVER

MG INITIAL CONDITIONS: COMPOSITION AND DISTRIBUTION OF COMPONENTS

Gaussian

(+ **MG a(t)**
Background)

Weak-field
MODIFIED GRAVITY

DYNAMICS OF GRAVITATIONAL INTERACTION

Non relativistic
MODIFIED GRAVITY
geodesics

DYNAMICS OF DARK MATTER

SOURCES OF LIGHT

DYNAMICS OF DARK ENERGY

NON-LINEARITIES

ANALYTICAL PERTURBATIVE

(I.E.

SEMI-ANALYTICAL

NUMERICS (SIMULATIONS)

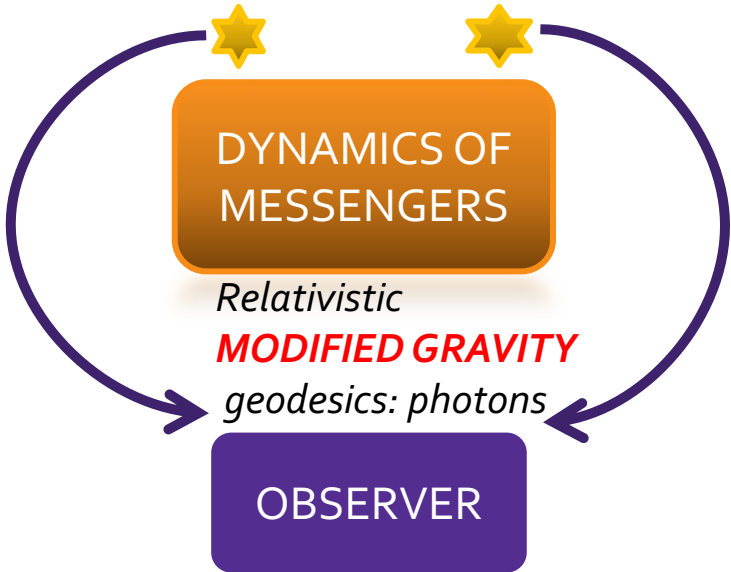
Vlasov-Poisson:
Cold Dark MATter

Λ or other

Metric (Jordan Frame)

$$ds^2 = -(1 + 2\Psi)dt^2 + a^2(t)(1 - 2\Phi)\delta_{ab}dx^a dx^b$$

with $\Phi \neq \Psi$

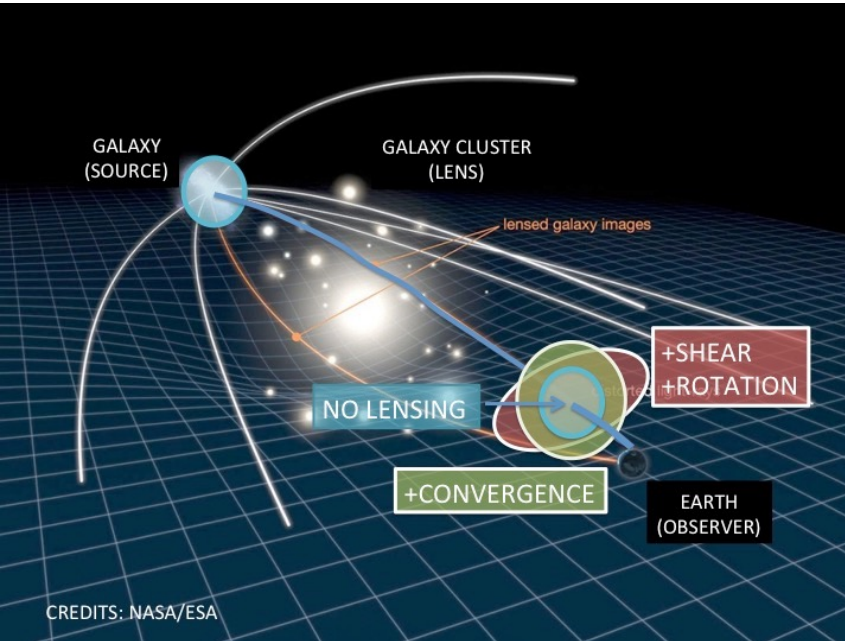


SOME RESULTS FROM RAYGAL & e-MANTIS

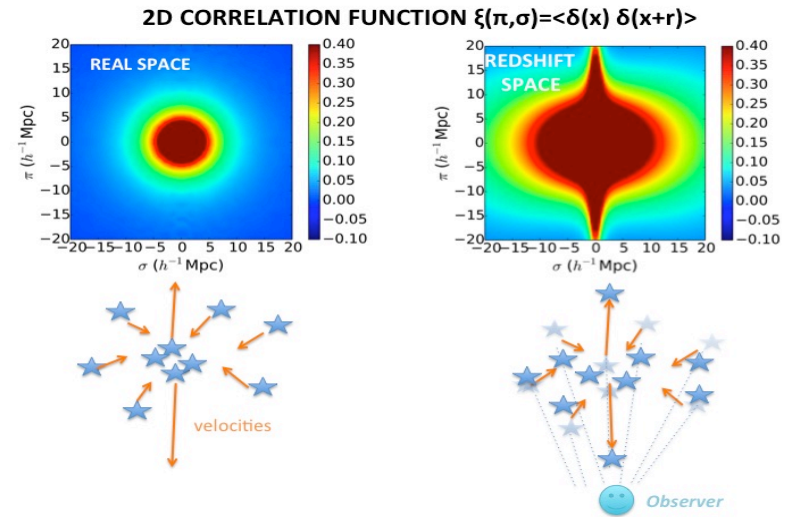
EXAMPLE OF RELATIVISTIC EFFECTS:WEAK-LENSING SHEAR (LEFT)

AND REDSHIFT SPACE DISTORTIONS (RIGHT)

LENSING



Redshift-Space Distortions (RSD)



AND

AND OTHERS (gravitational redshift, ISW effect, transverse Doppler, etc)

- Relativistic approach at large scales: **Yoo+ 2010; Bonvin&Durrer 2011; Yoo 2011; Lewis&Challinor 2011**

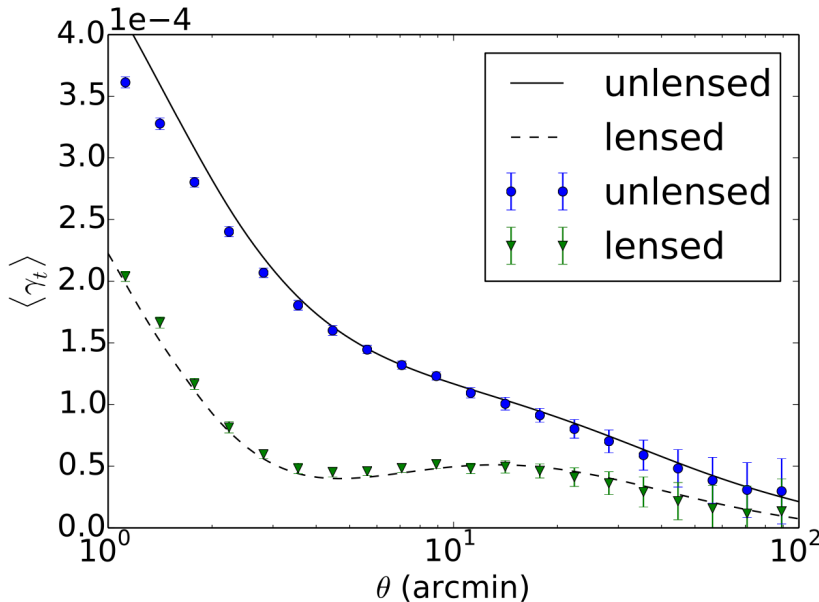
Use **similar formalism as for CMB** (i.e. weak field GR) but applied to galaxies

->LIMITATION OF ORIGINAL WORKS: **LINEAR REGIME**

- Relativistic approach at cluster scale and around: Kaiser2013, Zhao2013, Croft2013, Cai+2017
- > LIMITATION: How to connect with linear predictions ?

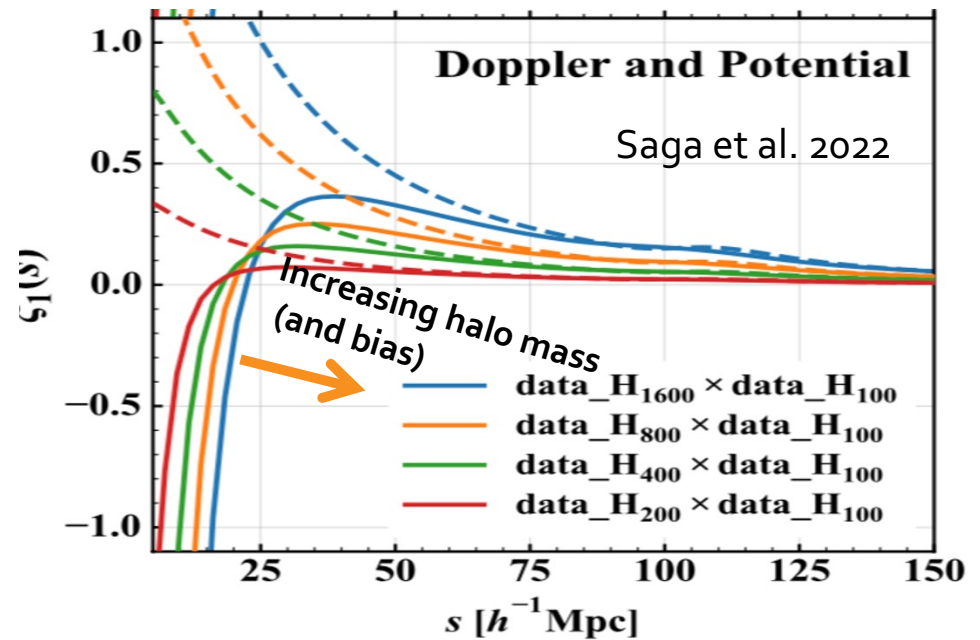
=> GR effects WITH SIM IS A HOT TOPIC: Killedar12, **Reverdy14**, Adamek16, Giblin17, Borzyszkowski17, **Breton19**, Adamek19, Leporizo, Guandalin21, Leporiz21, **Rasera22**, ... 24

EXAMPLE OF RELATIVISTIC EFFECTS WITH RAYGAL: PROFILE OF WEAK-LENSING SHEAR (LEFT) AND HALO-HALO DIPOLE (RIGHT)



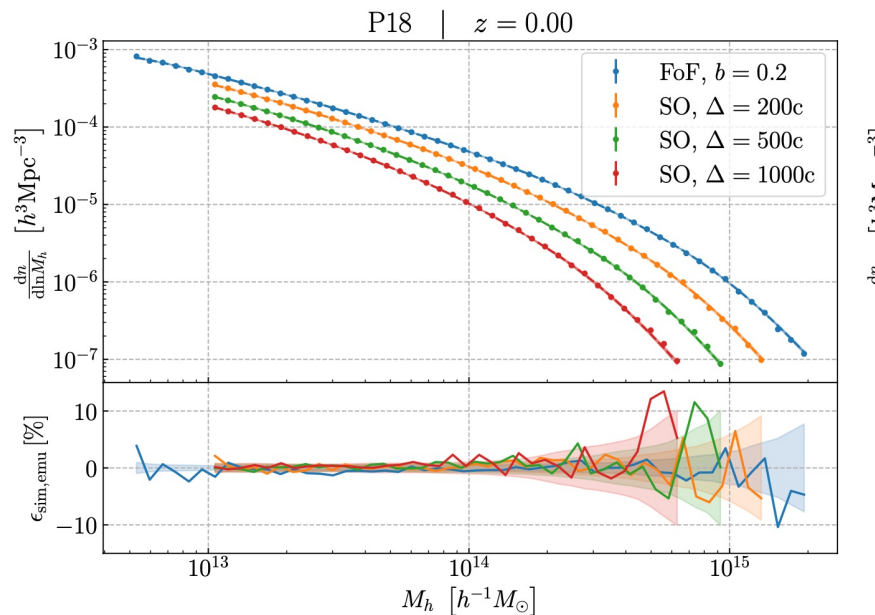
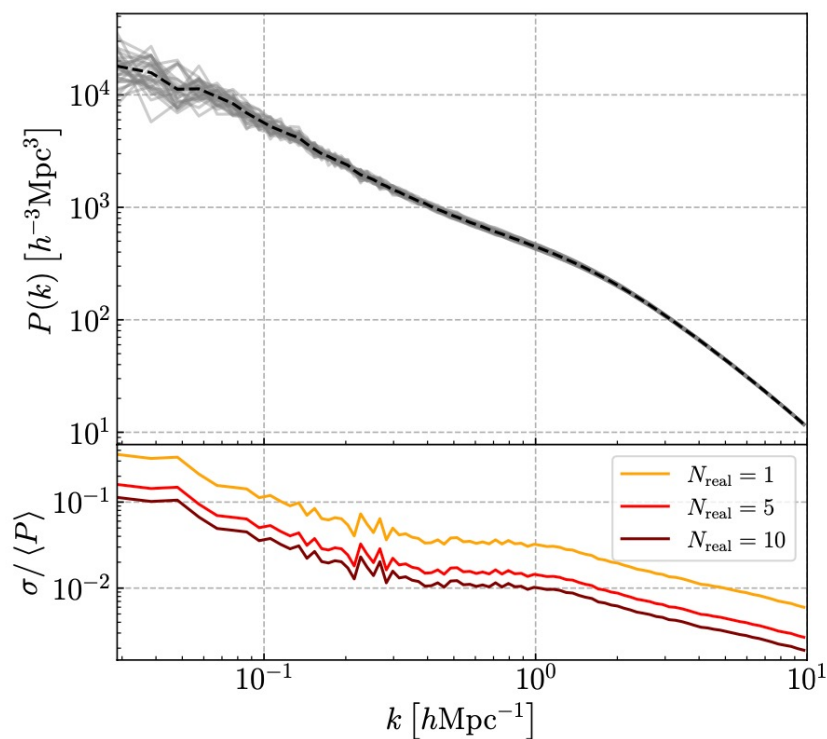
Courtesy: Michel-Andrès Breton

**THE WEAK-LENSING
SHEAR PROFILE IS
SENSITIVE
TO NON-TRIVIAL
RELATIVISTIC EFFECTS**

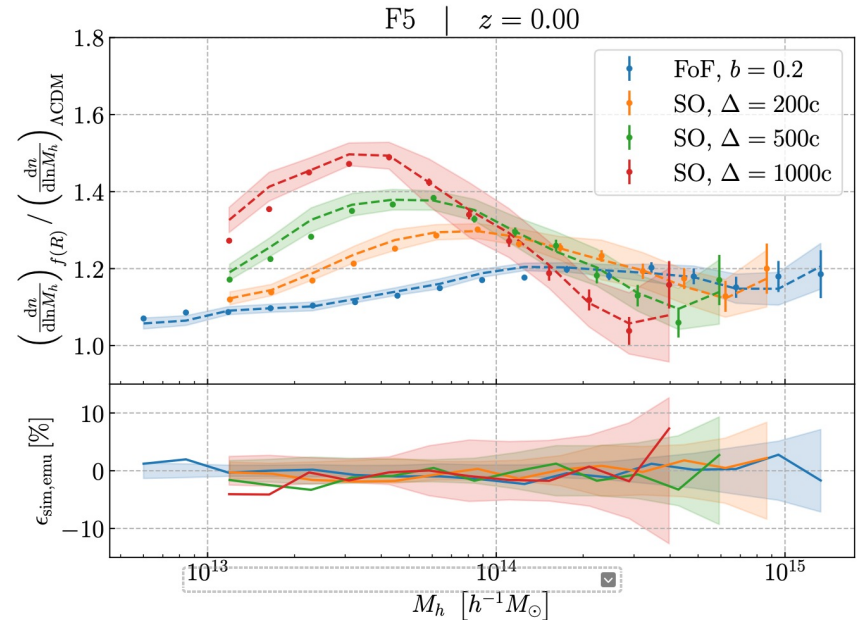
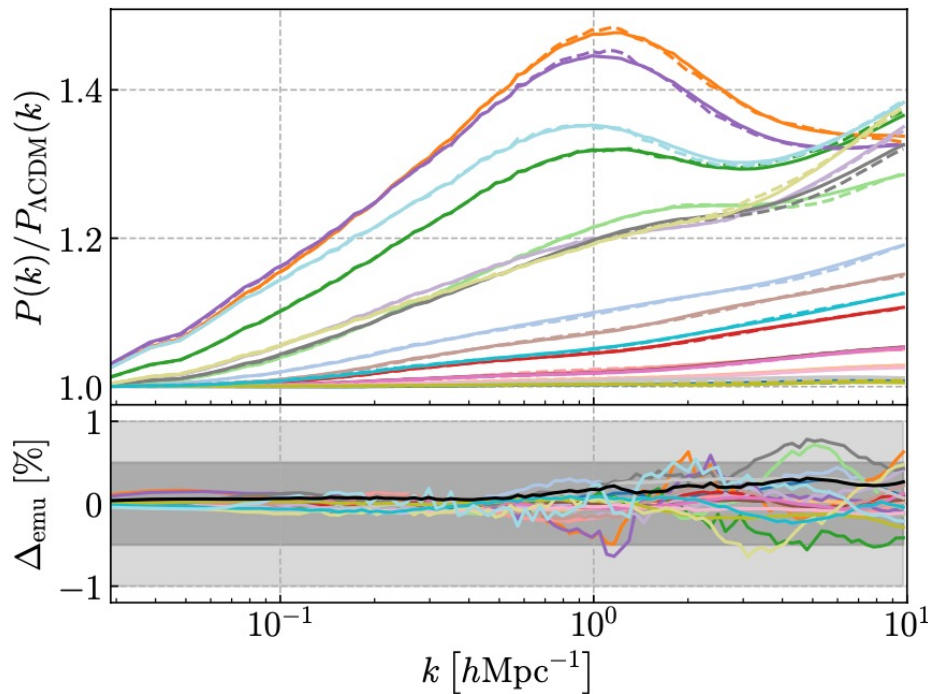


**THE HALO-HALO
DIPOLE IS A NEW PROBE
OF THE POTENTIAL AT COSMIC
SCALES**

EXAMPLE OF EMULATION WITH e-MANTIS: MATTER POWER SPECTRUM (LEFT) AND HALO MASS FUNCTION (RIGHT)



EXAMPLE OF EMULATION WITH e-MANTIS: MATTER POWER SPECTRUM BOOST (LEFT) AND HALO MASS FUNCTION BOOST (RIGHT)



ACCURATE (few %) AND FAST (few ms) PREDICTIONS OF
THE MATTER POWER SPECTRUM AND HALO MASS FUNCTION

SEE Iñigo'S THESIS DEFENSE EXPECTED 26 SEPTEMBER 2PM
SAVE THE DATE !
(IF EVERYTHING GOES WELL OF COURSE ;-))

CONCLUSION

PROGRACERAY PROJECT

Goal

Fast predictions of multiple complementary observables
in a wide range of modified gravity models

Methods

Number of simulations as in e-MANTIS + Size of simulations as in RayGal
Relativistic ray-tracing (as in RayGal)
Emulators (as in e-Mantis)

Constraints

Comparison with data from DESI, Euclid and LSST will enable strong constraints on
the nature of gravity at cosmic scales