



SPACE MANIFOLD DYNAMICS

Tides and motions in planetary systems

en l'honneur de Sylvio Ferraz-Mello

08–10 apr 2026
PARIS

ettore perozzi



Sputnik Sylvio

ULTIMA HORA

Captados em São Paulo os sinais do satellite

Quando encerravamos o expediente desta edição, eramos informados de que a equipe que trabalha no Observatorio sob a orientação de seu diretor, o prof. Abrão de Moraes, havia obtido exito em seus esforços no sentido de captar as emissões do satellite artificial lançado anteontem. Por três vezes foram ouvidos sinais, em transmissões que duraram cerca de dez minutos, em sua fase de intensidade maxima. A frequencia através da qual se fez a re-

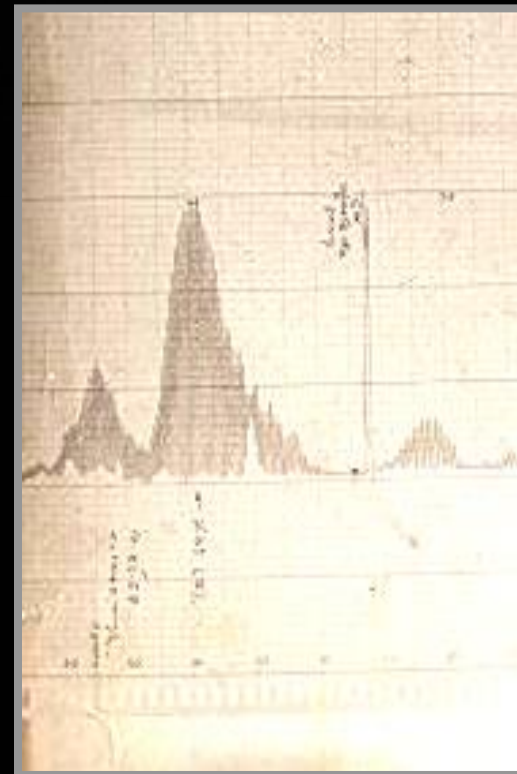
cepção foi a de 20.005 quilociclos. Segundo nos esclareceu o prof. Abrão de Moraes, não é possível por ora, no Observatorio, captar as transmissões na frequencia de 40 megaciclos, a que fazem referencia os telegramas procedentes de Moscou — isso devido ao fato de os receptores comuns não alcançarem essa frequencia. Já estão sendo feitas porem as necessarias adaptações — acrescentou — para possibilitar a recepção em 40 megaciclos.

Ainda segundo o diretor do Observatorio, os sinais emitidos parecem provir de um transmissor poderoso.

A equipe que vem trabalhando com o prof. Abrão de Moraes compõe-se dos profs. Luis de Queirós Orsini e Helio Guerra Vieira, da Escola Politecnica, e Silvio Ferraz de Melo, do proprio Observatorio.



O prof. Abrão de Moraes e o assistente Sylvio, no Observatório Astronômico e Geofísico, atravessam a madrugada e a tarde de ontem à espera de que o "Sputnik II" desse sinal de vida, anotando todos os dados científicos de interesse. D.N. - 5-XI-57 - 1ª ed. - 1ª pág.





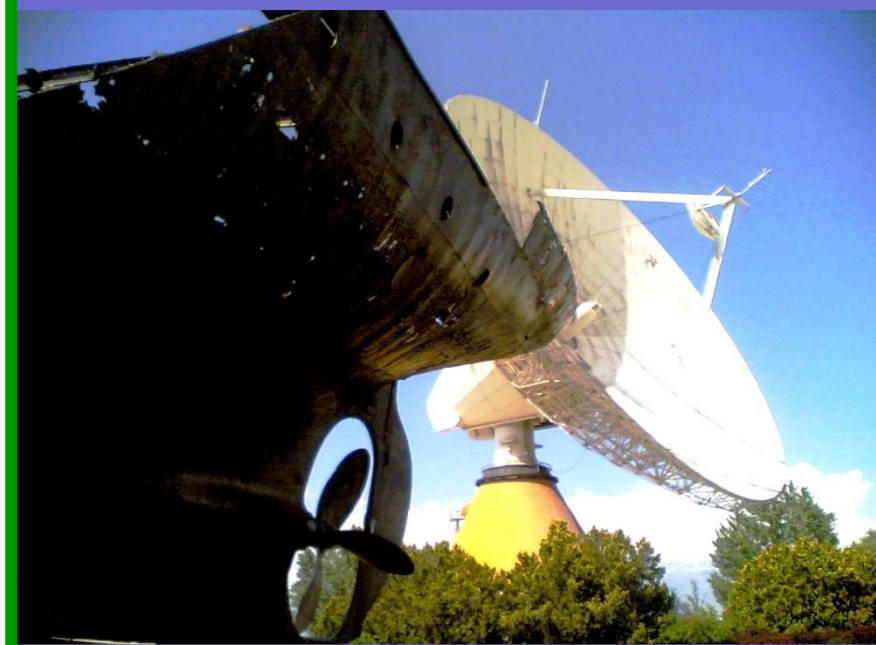
**NOVEL SPACEWAYS
FOR SCIENTIFIC
AND EXPLORATION MISSIONS**

Conference Chairman
SYLVIO FERRAZ-MELLO
Universidade de São Paulo - Brazil

Organising Committee

Chairman
ETTORE PEROZZI Telespazio

ROBERTO BATTISTON INFN
ALESSANDRA GELLETI
Università di Roma "Tor Vergata"
GUIDO DI COCCO INAF
GLAUCO DI GENOVA Telespazio
RENO MANDOLESI INAF
WALTER PECORELLA Telespazio
and Moon Base Italia WG
PIERGIORGIO PICCOZZA INFN
FRANCESCO PERILLO Telespazio
GIOVANNI VALSECCHI INAF



Centro Spaziale del Fucino 15-17 October 2007

Ettore Perozzi
Sylvio Ferraz-Mello
Editors

Space Manifold Dynamics

*Novel Spaceways for
Science and Exploration*

 Springer



CONTRIBUTORS

Mariano Andrenucci Alta S.p.A., Pisa, Italy

Edward Belbruno Department of Astrophysical Sciences, Princeton University, USA

Miguel Belló DEIMOS Space SL, Tres Cantos, Madrid, Spain

Carlo Burigana INAF-IASF Bologna, Italy

Cosmo Casaregola Alta S.p.A., Pisa, Italy

Silvano Casini DdeB, Houston, TX, USA

Alessandra Celletti Dipartimento di Matematica, Università di Roma Tor Vergata, Italy

Christian Circi Scuola di Ingegneria Aerospaziale, Università di Roma "La Sapienza", Italy

Bruce A. Conway Dpt of Aerospace Engineering, University of Illinois, Urbana, USA

Alessio Di Salvo Rheinmetall Italia, Roma, Italy

Sylvio Ferraz-Mello Universidade de Sao Paulo, Brazil

Koen Geurts Alta S.p.A., Pisa, Italy

Jesús Gil-Fernández GMV, Tres Cantos, Madrid Spain

Gerard Gómez Dpt de Matematica Aplicada i Anàlisi. Universitat de Barcelona, Spain

Raúl Cadenas Gorgojo GMV, Tres Cantos, Madrid, Spain

Mariella Graziano GMV, Tres Cantos, Madrid, Spain

Massimiliano Guzzo Dpt Matematica Pura e Applicata, Università degli Studi di Padova, Italy

Pablo Ibáñez ETSI Aeronáuticos, Technical University of Madrid (UPM), Madrid, Spain

Nazzareno Mandolesi INAF-IASF Bologna, Italy

Riccardo Marson Telespazio, Roma, Italy

Christopher Martin Dpt of Aerospace Engineering, University of Illinois, Urbana, USA

Josep J. Masdemont Dpt Matematica Aplicada, Universitat Politècnica de Catalunya, Spain

Filippo Ongaro ISMERIAN - Istituto di Medicina Rigenerativa e Anti-Aging, Italy

Pierpaolo Pergola Alta S.p.A., Pisa, Italy

Ettore Perozzi Telespazio, Roma, Italy

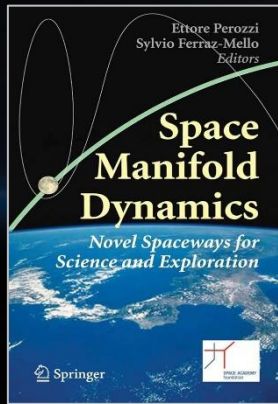
Vladimir M. Petrov Institute for Biomedical Research, Russian Academy of Science, Moscow

Franco Rossitto Moon Base Working Group

Paolo Teofilatto Scuola di Ingegneria Aerospaziale, Università di Roma "La Sapienza", Italy

Luca Valenziano INAF-IASF Bologna, Italy

Carlos Corral Van Damme GMV, Tres Cantos, Madrid Spain



recommendations

During the final panel discussion, the participants to the workshop “Novel Spaceways for Scientific and Exploration Missions” have produced a commonly agreed list of strategic considerations and of specific actions to be undertaken for fully exploiting the potential benefits for the scientific, exploration and technological programs of the major space agencies.

Introductory statements:

There is the need of establishing a **strong and continuous link** among the research, the industrial communities and the space agencies, even at a basic level (e.g. regular organization of workshops and schools).

The terminology “**Space Manifold Dynamics**” (SMD) is adopted for referring to the dynamical systems approach to spaceflight dynamics, thus encompassing more specific definitions (stable/unstable manifolds, Lagrange trajectories, weak stability boundary, etc.);

Topics deserving immediate attention:

filling the gap between industry and research on specific issues used to investigate space manifold dynamics (e.g. apply new methods, translating mission requirements into theory);

focus on the effect of dissipative systems on SMD in terms of outcomes, methods and applications (e.g. low-thrust engines, non-gravitational forces, tethered systems);

explore the “geography” of the solar system using novel dynamical approaches, such as mapping techniques and lagrangian trajectories;

build the “cartography” associated to the utilization of the near-Earth space (e.g. periodic orbits, lunar transfers);

define the concept of “mixed approach” to space mission design, i.e. dividing a complex trajectory into sections for which a given methods applies better (e.g. traditional ballistic + gravity assist for transfer trajectories, SMD for orbit insertion and satellite tour design);

develop a simulation environment to investigate the new challenges posed by manned and unmanned exploration to numerical optimization methods (e.g. flight time vs. delta-V, electric vs chemical propulsion or other alternatives);

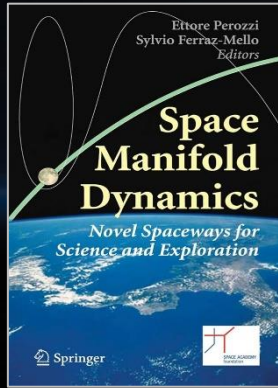
study the impact of SMD trajectories on human spaceflight and in particular on the radiation issue (e.g. finding “sheltered” mission profiles);

evaluate the consequences of adopting a SMD approach on both, ground support and spacecraft subsystems requirements (e.g. TLC, GNC, propulsion);

Specific actions to be considered:

Interplanetary trajectory orbit determination needs a new start: novel methods are required for developing new generation high-precision orbit determination operational software.

The Workshop highlights the relevance of the generation of **high-quality planetary ephemeris** as well of other celestial and artificial bodies for both, astronomical research and space applications.



recommendation

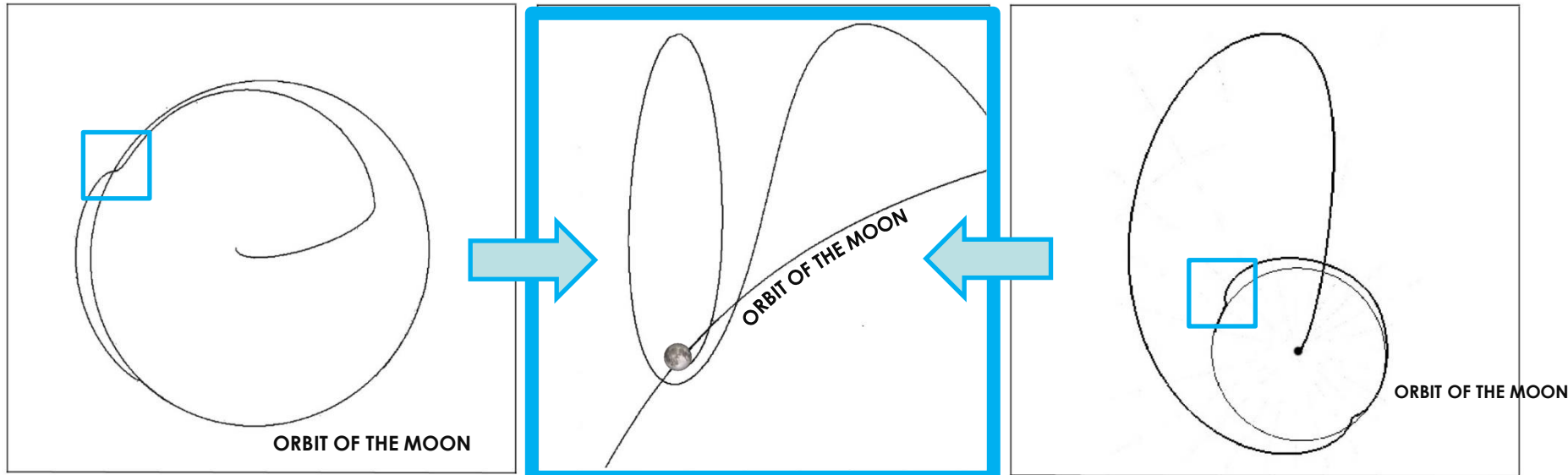
filling the gap between industry and research on specific issues used to investigate space manifold dynamics (e.g. apply new methods, translating mission requirements into theory);

evaluate the consequences of adopting a SMD approach on both, ground support and spacecraft subsystems requirements (e.g. TLC, GNC, propulsion);

Magia mission tradeoff



JET PROPULSION LABORATORY INTEROFFICE MEMORANDUM
312/90.4-1731-EAB
June 15, 1990
TO: Distribution
FROM: E. A. Belbruno and J. K. Miller
SUBJECT: A Ballistic Lunar Capture Trajectory For The Japanese Spacecraft Hiten



SMD external transfer

lunar ballistic capture

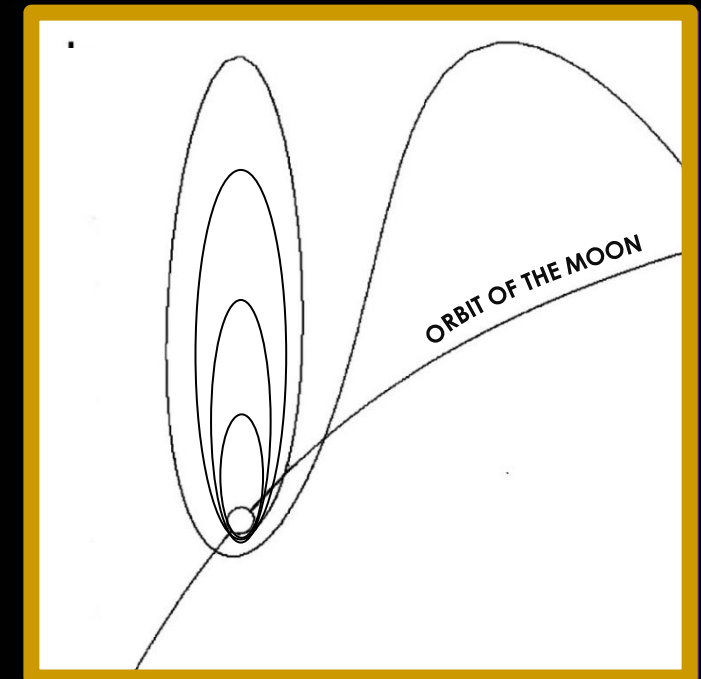
SMD external transfer

Magia mission tradeoff



Hohmann	SMD external
Transfer Time: 4 days	Transfer Time: 90 days
Total delta-V = 3.9 km/s	Total delta-V = 3.8 km/s
2 manoeuvres: TLI, LOI	2 manoeuvres: TLI, LOI
TLI=3.1; LOI=0.8, NOI=0.0	TLI=3.2; LOI=0.0; NOI=0.6
Elliptic trajectory (high LOI)	WSB trajectory (no LOI)
LOI critical	Ballistic Capture (LOI non-critical)
consolidated guidance	innovative guidance
Needs quick reaction time	Allows slow reaction time
-	Possible E-M-S cruise science
Apollo-like	Science & Exploration precursor

TLI = Trans Lunar Injection;
LOI = Lunar Orbit Insertion;
NOI = Nominal Orbit Insertion



orbit circularization

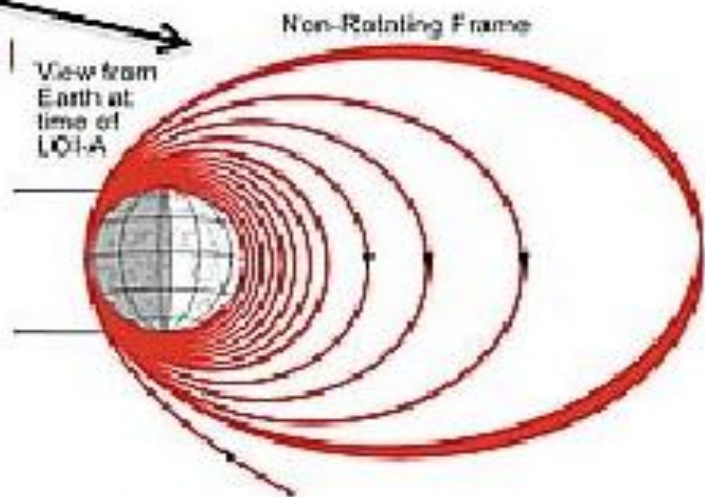
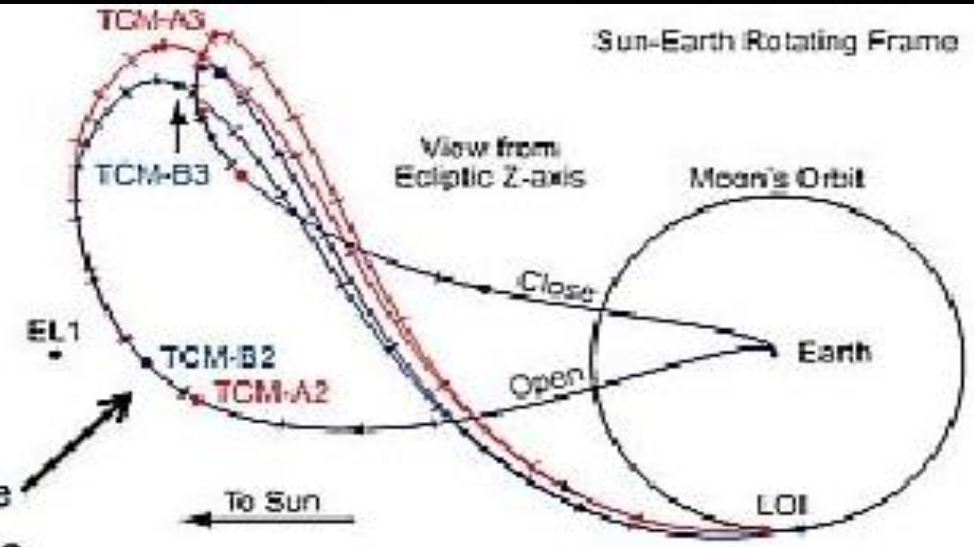
GRAIL mission profile



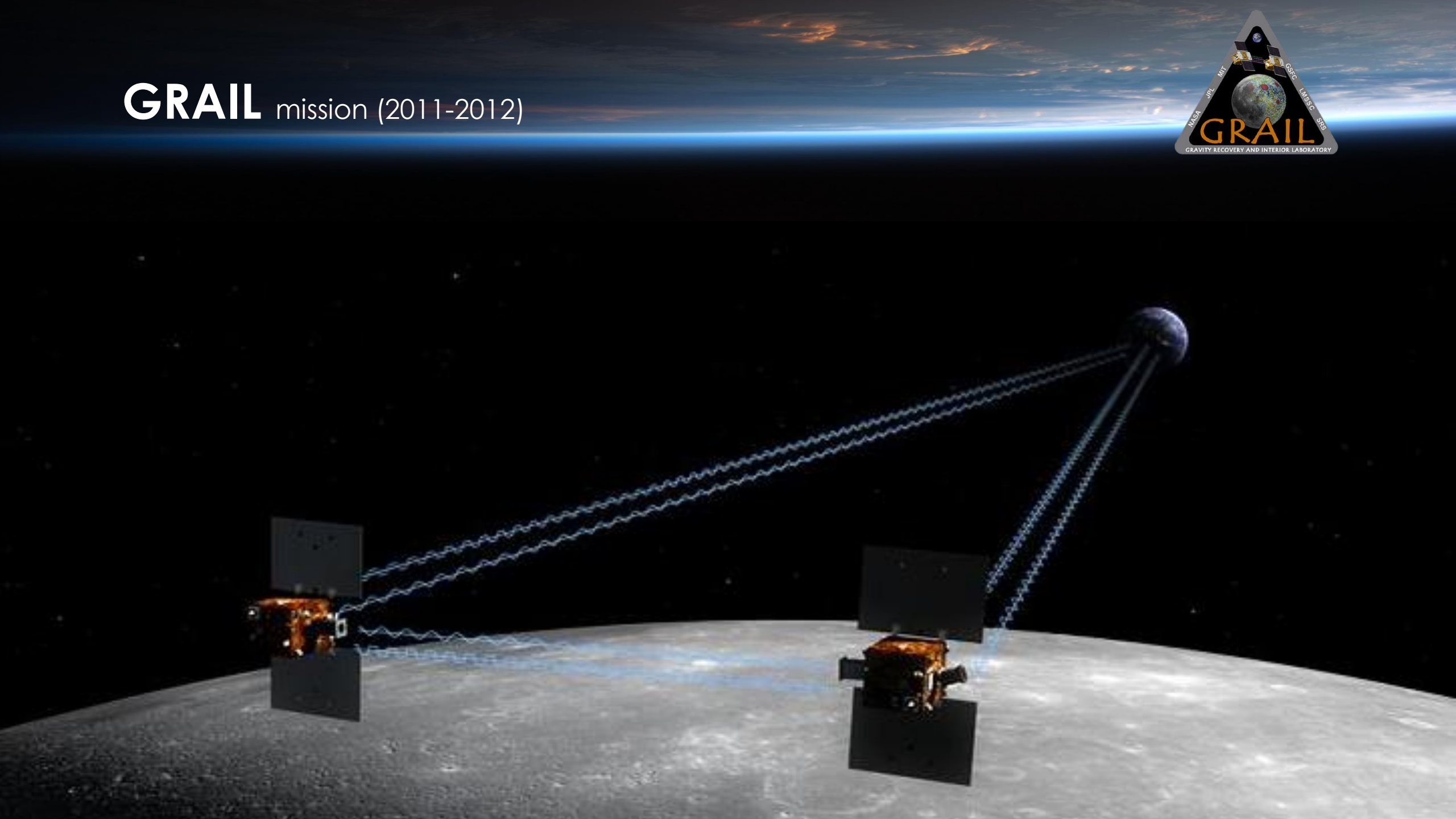
cis

Mission Phases

- 1) Launch Phase
- 2) Trans-Lunar Cruise (TLC) Phase
- 3) Lunar Orbit Insertion (LOI) Phase
- 4) Orbit Period Reduction (OPR) Phase
- 5) Transition to Science Formation (TSF)
- 6) Science Phase
- 7) Decommissioning Phase



GRAIL mission (2011-2012)



SMART-1 solar electric propulsion (2003-2005)



**SEP + SMD =
extremely low energy
transfer**

SMART-1 Electric Propulsion Operational Experience

IEPC-2005-245

D. Milligan^{*}, D. Gestal[†], O. Camino[‡] and P. Pardo-Voss[§]
European Space Operations Centre, Robert Bosch Str. 5, 64293 Darmstadt, Germany

D. Estublier^{**}
ESA/ESTEC, Kepleraan 1, Noordwijk, The Netherlands

and

C. Koppel^{††}
Snecma Moteurs, Division Moteurs-Spatiaux, Villaroche Nord, France

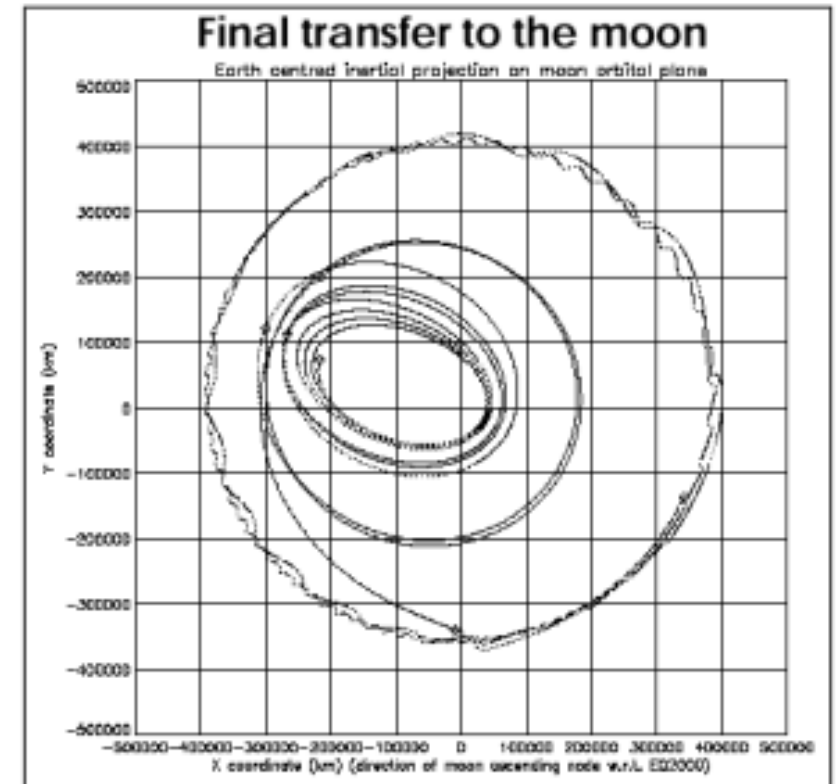
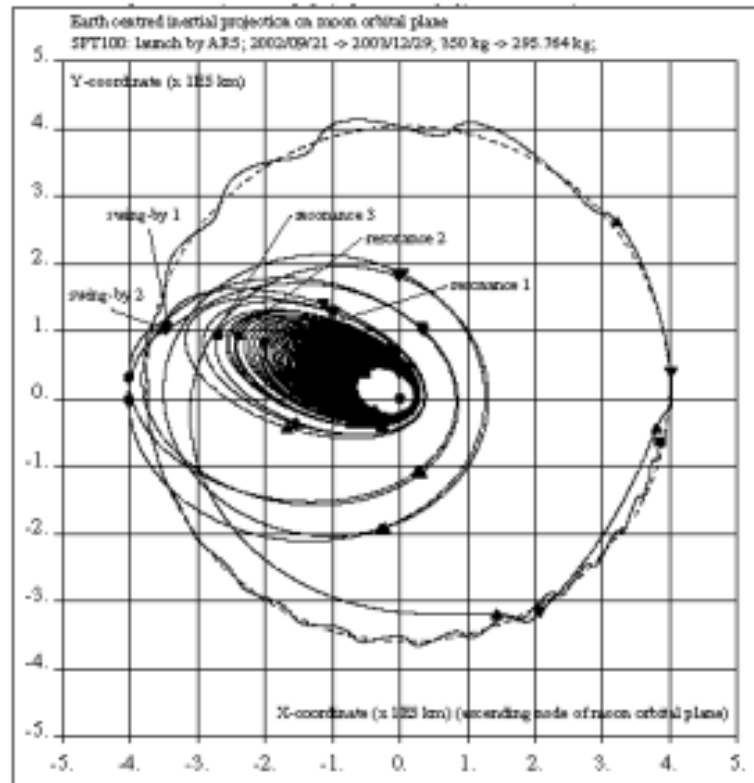
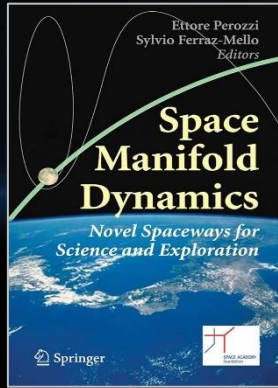


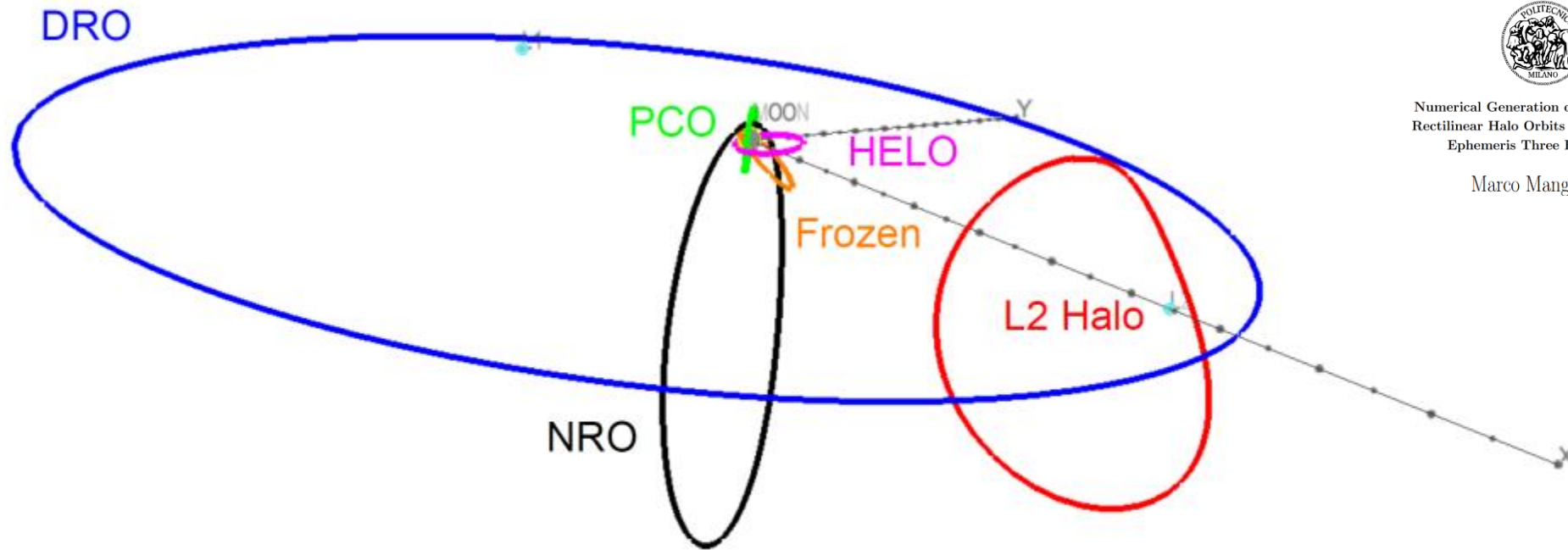
Figure 4 Comparison pre-launch planned (left) and in flight executed (right) Lunar capture strategies



recommendation

build the “cartography” associated to the utilization of the near-Earth space (e.g. periodic orbits, lunar transfers);

LUNAR GATEWAY L1 near rectilinear orbit

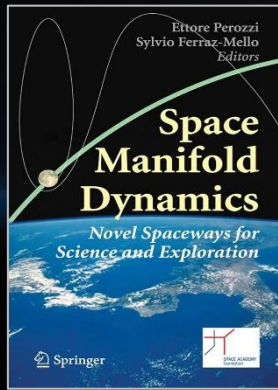


Numerical Generation of cis-Lunar Near Rectilinear Halo Orbits in the Restricted Ephemeris Three Body Model

Marco Mangialardo.

Figure 1.1: Different orbits considered for the LOP-G. Acronyms: Distant Retrograde Orbit (DRO), Prograde Circular Orbit (PCO), Near Rectilinear Orbit (NRO), Elliptical Lunar Orbit (ELO). Credit

R. Whitley and R. Martinez, "Options for staging orbits in cislunar space," in 2016 IEEE Aerospace Conference. IEEE, 2016, pp. 1-9.

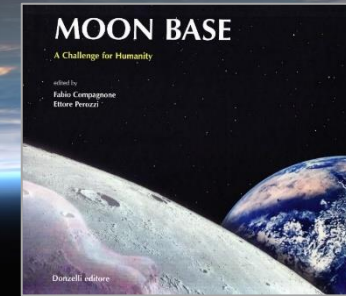


recommendation

study the impact of SMD trajectories on human spaceflight and in particular on the radiation issue (e.g. finding “sheltered” mission profiles)

Moon Base

long-term lunar exploration



Moon harbor: a LL1 halo orbiting infrastructure for manned / unmanned missions support (e.g refurbishing space telescopes, space elevator)

Low altitude lunar **orbiters / landers**

High altitude lunar constellations for **satellite navigation**

High eccentricity orbits / halo orbiters for **telecommunications**

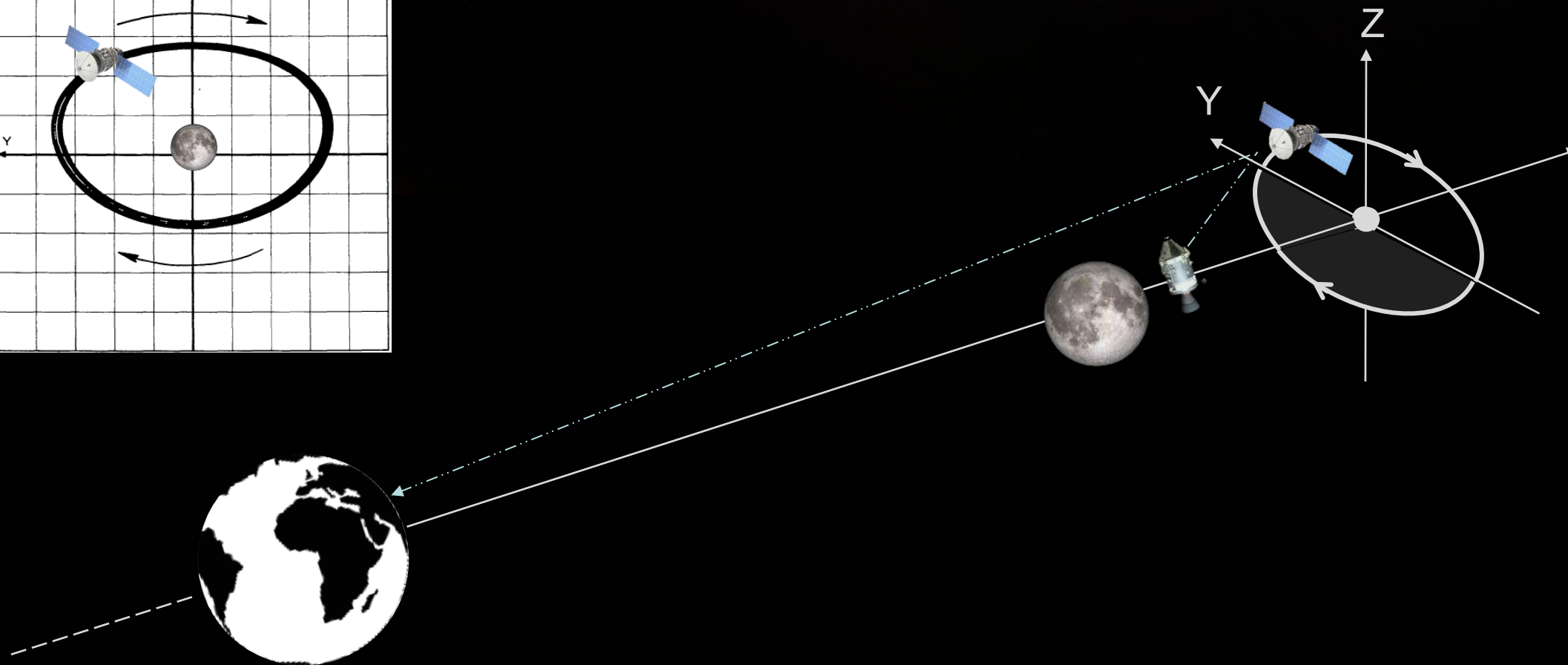
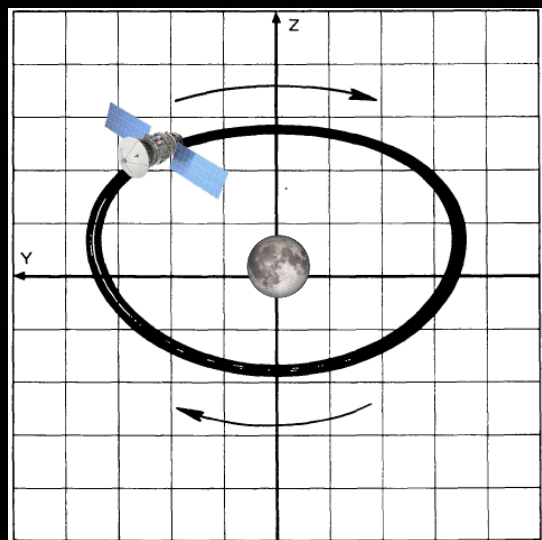
Operations **safety** (avoiding critical events – lunar rescue trajectories)

Flexibility of mission profile (e.g. different launch scenario)

Long transfers: **cruise science** (e.g. gravitational redshift, solar/magnetosphere interactions)

Manned vs unmanned missions (radiation issue, non-critical cargo delivery)

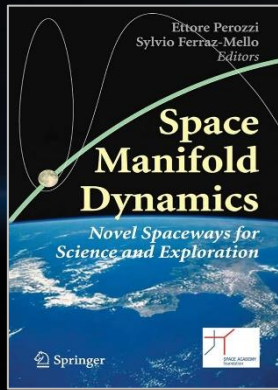
APOLLO L2 lunar data relay satellite



QUEQUIAO

L2 lunar far side telecom satellite





recommendation

define the concept of “mixed approach” to space mission design, i.e. dividing a complex trajectory into sections for which a given methods applies better (e.g. traditional ballistic + gravity assist for transfer trajectories, SMD for orbit insertion and satellite tour design);

Europa Lander proposal



Low Energy Capture into High Inclination Orbits for Ocean Worlds Missions

Principal Investigator: Martin W. Lo (392M)

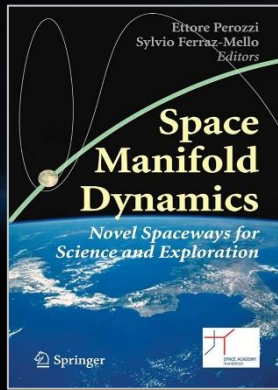
In recent years, resonant periodic orbits and their stable and unstable manifolds have seen significant interest and use as a tool for trajectory design in multi-body systems. For

High-order resonant orbit manifold expansions for mission design in the planar circular restricted 3-body problem

, [Rodney L. Anderson](#)^b, [Rafael de la Llave](#)^a

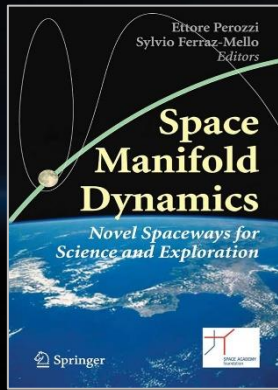
developing a procedure to compute intersections of the computed stable and unstable manifolds. We develop and implement algorithms that accomplish these three goals, and demonstrate their application to the problem of transferring between resonances in the Jupiter-Europa system.





recommendation

focus on the effect of dissipative systems on SMD in terms of outcomes, methods and applications (e.g. low-thrust engines, non-gravitational forces, tethered systems



recommendation

The terminology “*Space Manifold Dynamics*” (SMD) is adopted for referring to the dynamical systems approach to spaceflight dynamics, thus encompassing more specific definitions (stable/unstable manifolds, Lagrange trajectories, weak stability boundary, etc.);

Celestial Mechanics & dynamical astronomy

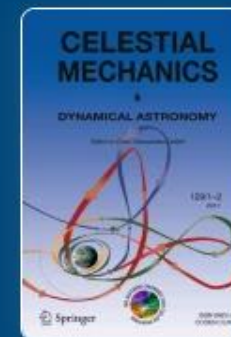
The first edition of the journal was published under the title “Celestial Mechanics” as an initiative of the Celestial Mechanics Institute. Later in 1989, the journal changed its name into “Celestial Mechanics and Dynamical Astronomy” (CM&DA). Over the years the editors-in-chief, associate editors and authors made a big effort to keep the journal up-to-date and retain a high scientific standard.

[Home](#) > [Celestial Mechanics and Dynamical Astronomy](#) > [Article](#) [Alessandra Celletti](#)

Topical collection “50 years of Celestial Mechanics and Dynamical Astronomy”

Preface | Published: 31 March 2020

Volume 132, article number 18, (2020) [Cite this article](#)



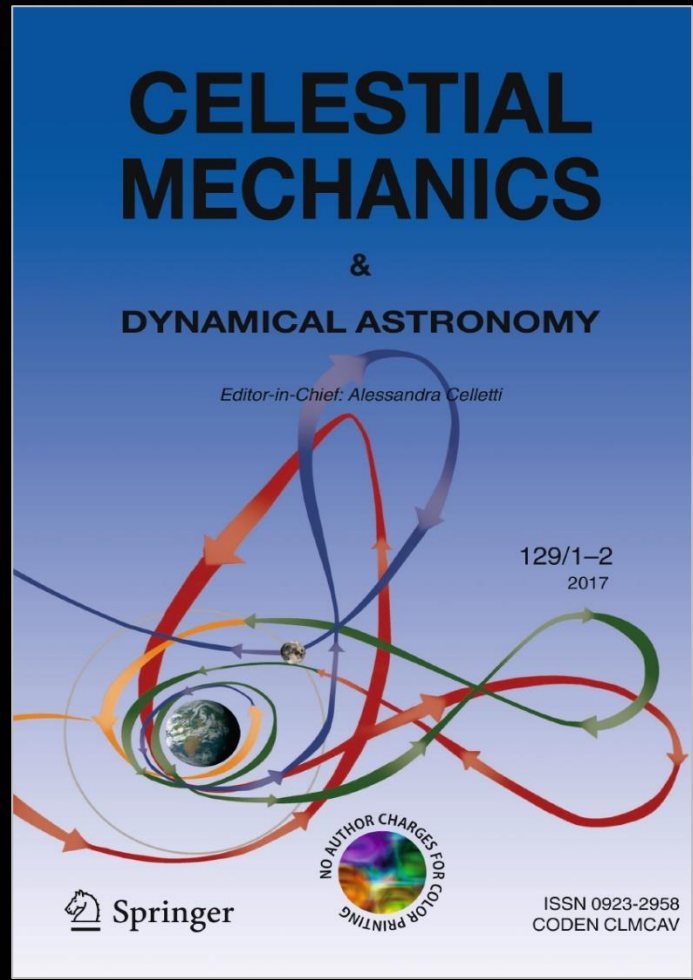
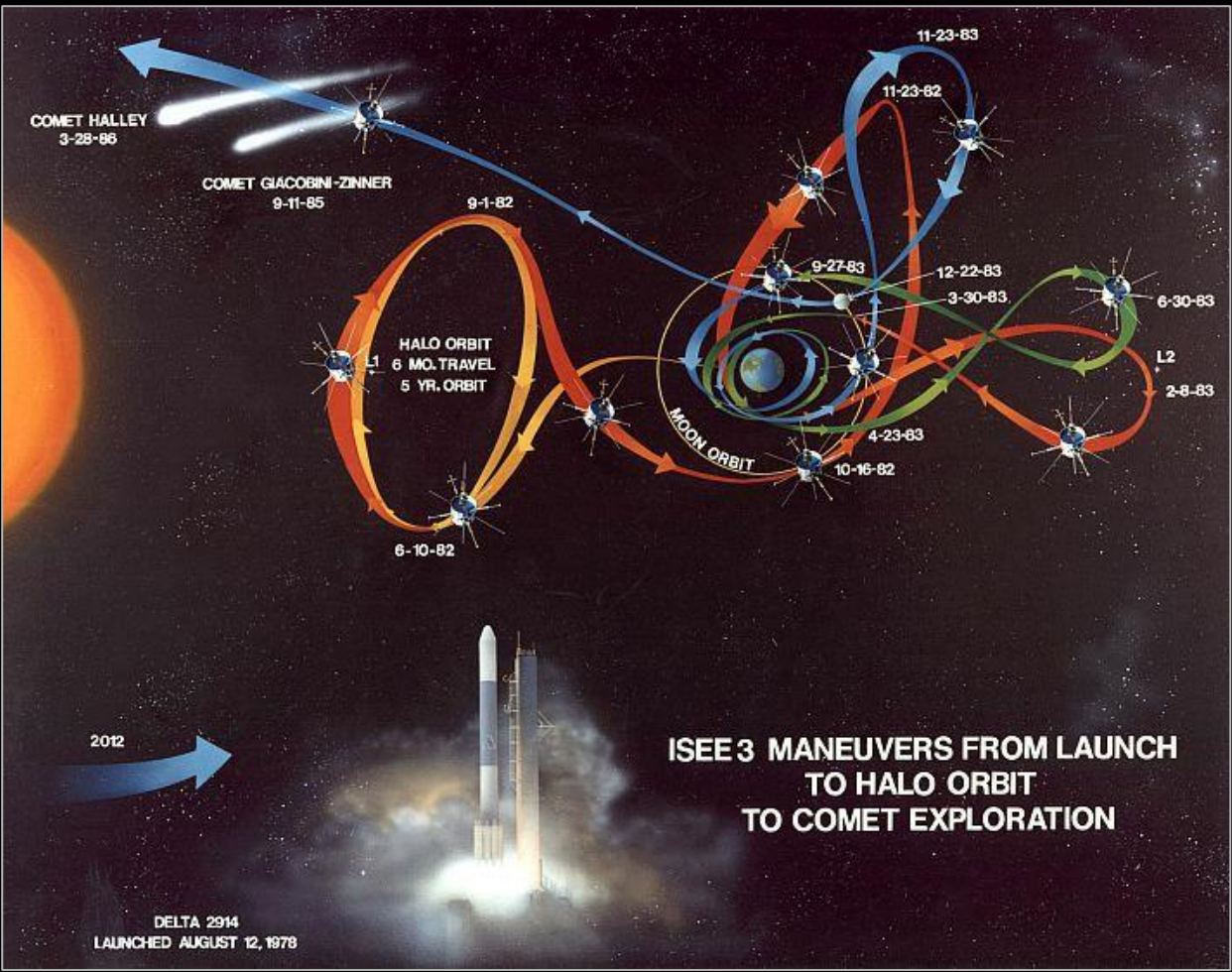
As written in 1990 by J.M.A. Danby ([CMDA 1990, vol. 50, 5–6]), the birth of the journal “Celestial Mechanics” dates back to a meeting at the Goddard Space Flight Center. The editorial of the first issue, while defining Celestial Mechanics as an old science that infers or proves “physical facts from the study of orbital behavior and other phenomena exhibited by celestial and artificial bodies,” underlined the need for research in this field,

ISEE-3/ICE trajectory (1978-1982-1986)



The Flight of ISEE-3/ICE: Origins, Mission History, and a Legacy

Robert W. Farquhar



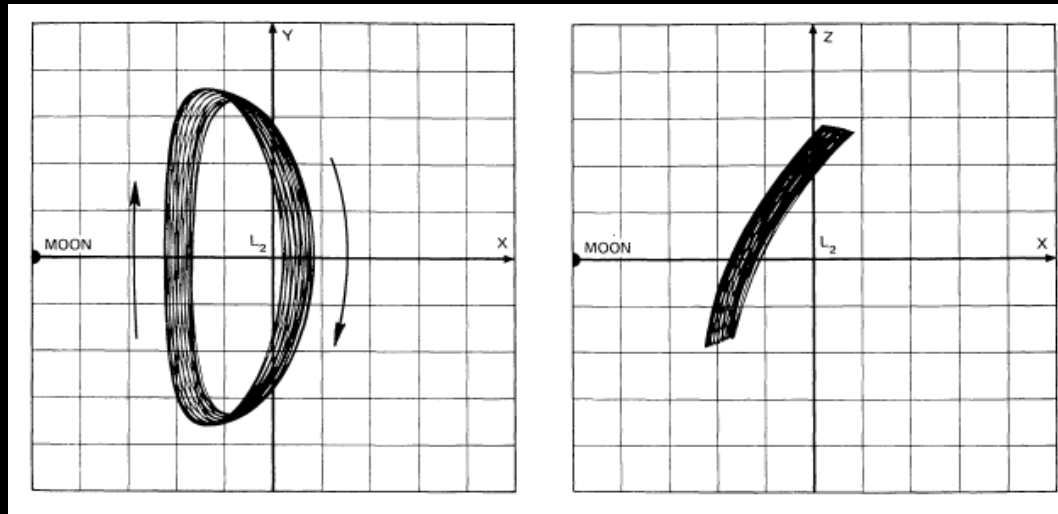
references librations vs manifolds

1973

QUASI-PERIODIC ORBITS ABOUT THE TRANSLUNAR LIBRATION POINT

ROBERT W. FARQUHAR and AHMED A. KAMEL*

Celestial Mechanics 7 (1973) 458–473.



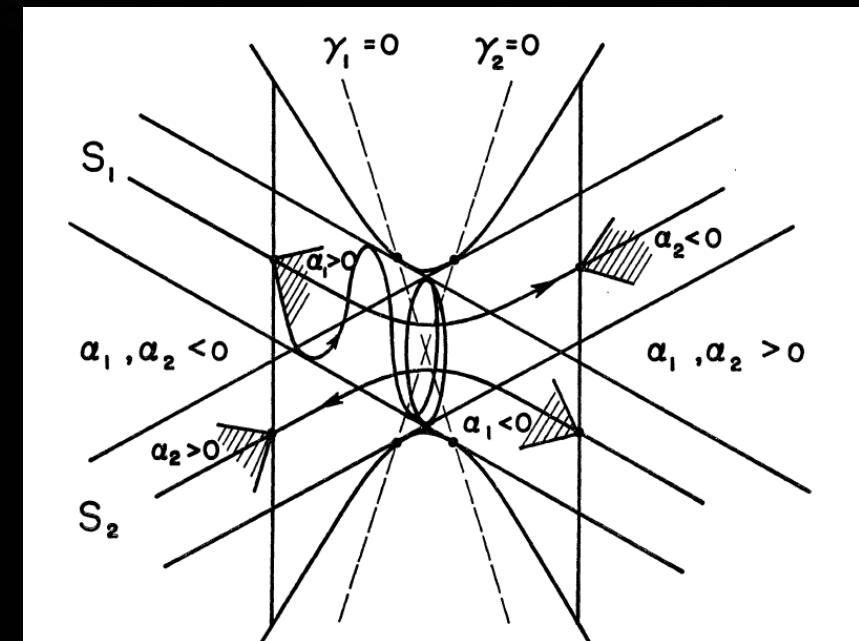
'Final Report for Lunar Libration Point Flight Dynamics Study', Contract NAS-5-11551, General Electric Co., April 1969.

1968

LOW ENERGY TRANSIT ORBITS IN THE RESTRICTED THREE-BODY PROBLEM*

C. C. CONLEY†

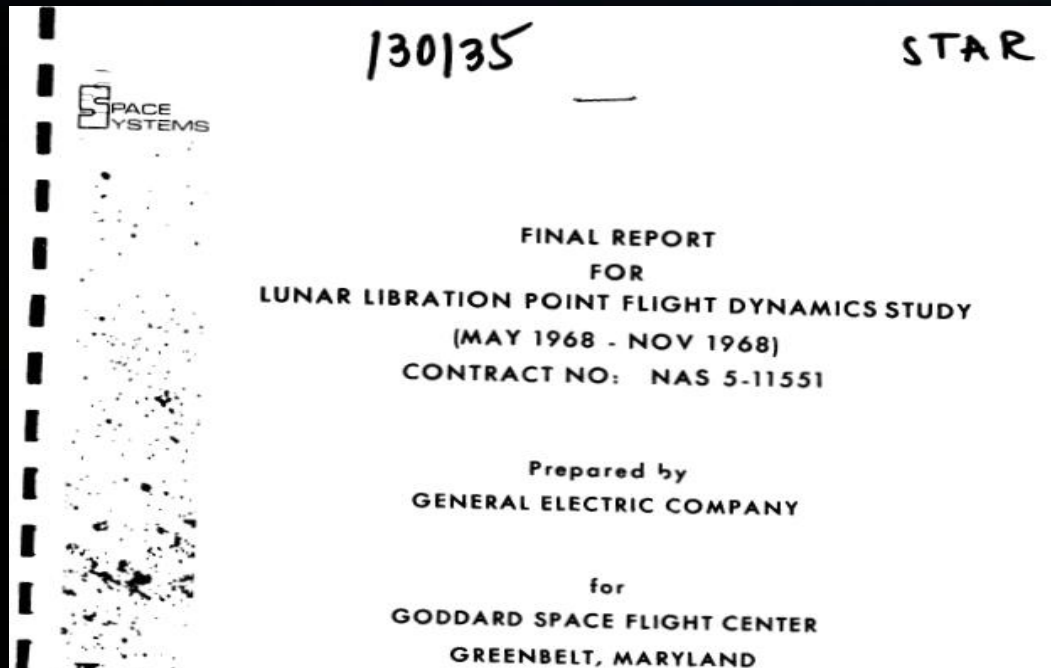
SIAM J. APPL. MATH.
Vol. 16, No. 4, July 1968



CONLEY, *Notes on the restricted three body problem: Approximate behavior of solutions near the collinear Lagrangian points*, TMX-53292, NASA, George C. Marshall Space Flight Center, Huntsville, Alabama, 1965.

references librations vs manifolds

1968



1966

2. Farquhar, R. W., "Stationkeeping in the Vicinity of Collinear Libration Points with an Application to a Lunar Communications Problem," American Astronautical Society Paper 66-132, July 1966.

1961

6. Colombo, G., "The Stabilization of an Artificial Satellite at the Inferior Conjunction Point of the Earth-Moon System," Smithsonian Contrib., Astrophys, Vol. 6, pp 213-222, 1961.

1965

NASA TECHNICAL MEMORANDUM

NASA TM X-53292
July 12, 1965

NASA

George C. Marshall
Space Flight Center,
Huntsville, Alabama

PROGRESS REPORT NO. 7
ON STUDIES IN THE FIELDS OF SPACE FLIGHT AND GUIDANCE THEORY

This report is intended to be the first in a series whose ultimate aims include an existence proof for the "periodic" solutions discovered numerically by M. Davidson [1]. Whether or not this can be accomplished remains to be seen, but it does seem clear that a thorough understanding of the behavior of orbits near the equilibrium point will be required. More will be said about this question in later reports.

GPO PRICE \$ _____
CSFTI PRICE(S) \$ _____
Hard copy (HC) 1.88
Microfiche (MF) 2.50
653 July 65

55 33064
(THRU)
/ (CODE)
30 (CATEGORY)

1. Davidson, M. (to be published).

references librations vs manifolds

1961

The Stabilization of an Artificial Satellite at the Inferior Conjunction Point of the Earth-Moon System

By G. Colombo

It is obviously important to be able to keep an artificial satellite stable at the inferior conjunction point (L_1) of the earth-moon system, while using the minimum amount of momentum. The fact that the inferior conjunction point is an exact solution of the four-body problem (earth-moon-sun-satellite) **Colombo, 1960; Klemperer and Benedikt, 1958, p. 25**, if we neglect only high-order perturbations, is an advantage of this solution that makes it preferable in some ways to the triangular Lagrangian solution (L_4) of the restricted three-body problem. On the other hand, the larger

called capture, temporary capture, and escape.
As to the literature **EGOROV [1]** gives an approximate analysis based on the sphere of influence idea. The difficulty with such a treatment is that for such low energy orbits the motion near the libration point L_1 displays a character quite different from KEPLERIAN motion. Actually, **the estimates so obtained are somewhat misleading.** THÜRING [2] gives two numerical examples of transition orbits.
The orbits presented here have the common feature that they are initially

... is fixed at approximately 1/82

M. C. DAVIDSON, *Numerical examples of transition orbits in the restricted three body problem*, *Astronaut. Acta*, 10 (1964), pp. 308-313.

1964

Numerical Examples of Transition Orbits in the Restricted Three Body Problem

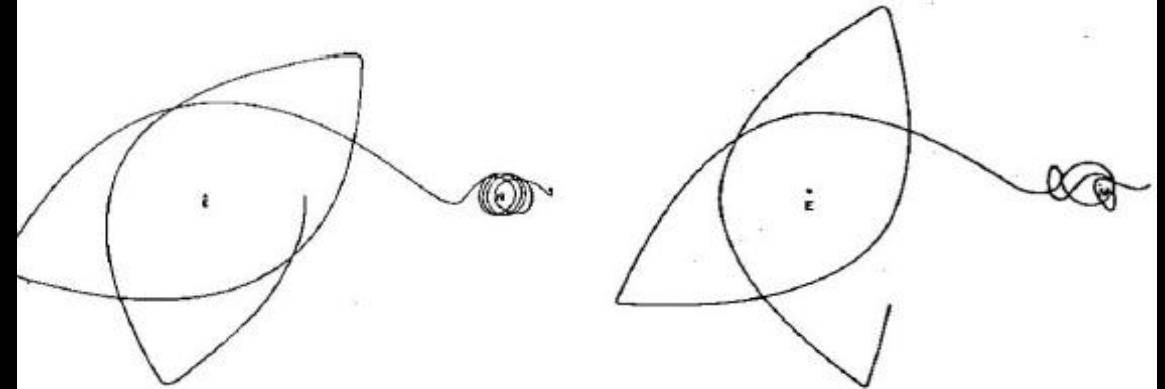
By

M. C. Davidson¹

(With 12 Figures)

¹ George C. Marshall Space Flight Center, Huntsville, Alabama, U.S.A.
(Received October 15, 1964)

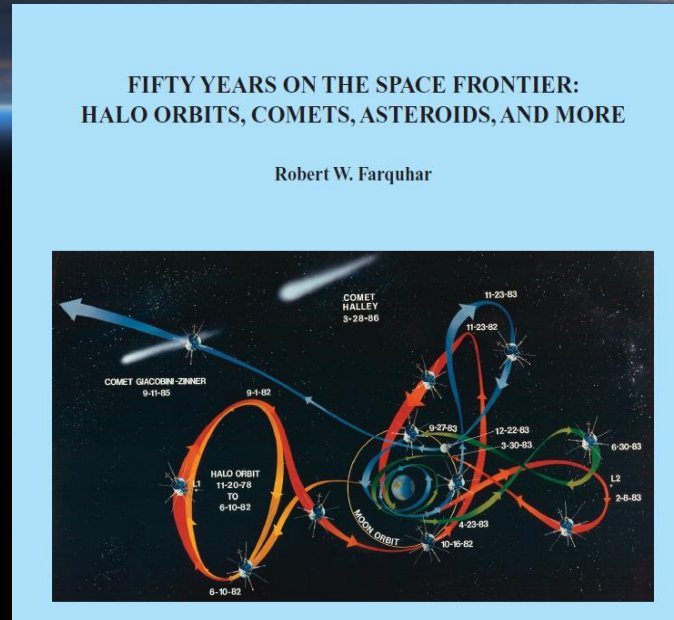
Abstract — Zusammenfassung — Résumé



References

1. F. A. EGOROV, Certain Problems of Moon Flight Dynamics. *The Russian Literature of Satellites*, Part 1, pp. 115-175 (1958).
2. D. THÜRING, Zwei spezielle Mondumlaufbahnen in der Raumfahrt um Erde und Mond. *Astronaut. Acta* 5, 241-250 (1959).

thirty years later...



<<According to Martin Lo, the “discoverer” of the Interplanetary Superhighway, the ISEE-3/ICE Trajectory Team was able to find a Superhighway trajectory using conventional methods because “**when you search around the halo orbits for a transfer trajectory from Earth, your path will invariably be controlled by the halo orbit’s stable manifold**”>>.

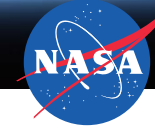
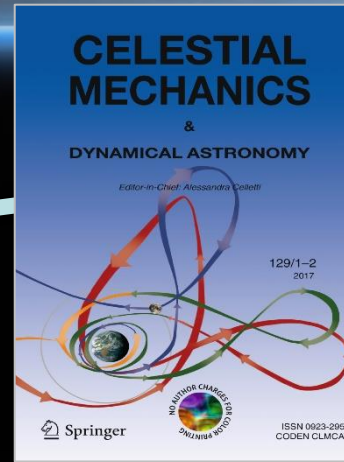
<<**Who would have guessed that the ISEE-3/ICE Team stumbled on such a momentous discovery without realizing what they had done?** >>

the big picture



GODDARD SPACE FLIGHT CENTER
GREENBELT, MARYLAND

1969



*George C. Marshall
Space Flight Center,
Huntsville, Alabama*

Giuseppe Colombo 1960-61

Robert Farquhar 1966-72

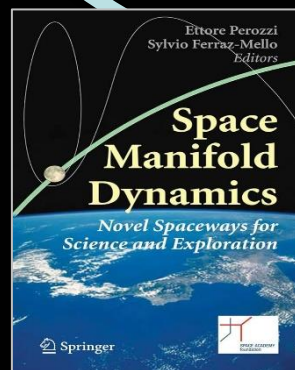
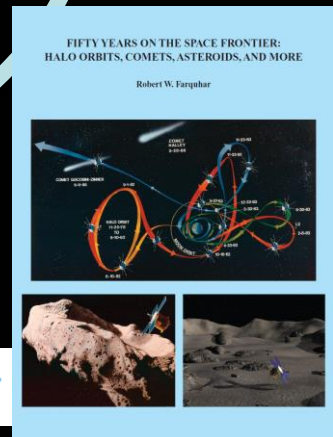
Mirt C. Davidson 1964-65

Charles C. Conley 1965-68

As written in 1990 by J.M.A. Danby ([CMDA 1990, vol. 50, 5–6]), the birth of the journal “Celestial Mechanics” dates back to a meeting at the Goddard Space Flight Center. The

the visionary concept of interplanetary highways that gave rise to a new branch of Astrodynamics, now known as “Space Manifold Dynamics.”

Alessandra Celletti |



2010

[23] Perozzi, E. and Ferraz-Mello, S., Editors, Space Manifold Dynamics, Springer, New York, Dordrecht, Heidelberg, London, 2010.

2011

lessons learned

The birth of the journal *Celestial Mechanics* and of the space manifold dynamics happened almost simultaneously in space and time.

Communication problems: for at least 20 years the libration point and the dynamical systems approach did not interact

Future work: the quest for the “cross-reference paper” (e.g.

Temporary Satellite Captures of Comets by Jupiter
A. Carusi and G. B. Valsecchi
I.A.S. – C.N.R., Rep. Planetologia, viale dell'Università 11, I-00185 Roma, Italy
Received October 17, accepted November 12, 1980

Temporary Satellite Capture of Short-Period Jupiter Family Comets from the Perspective of Dynamical Systems¹
K. C. Howell,² B. G. Marchand,³ and M. W. Lo⁴



NOTE ADDED IN PROOF: also scientific editors have communication problems!

conclusions

One cannot predict when knowledge will be applied, only that it often is

Charles Conley

Le grandi scoperte sono qualitative, la matematica seve «solo» a dimostrare

Giorgio Parisi

Le seul véritable voyage, le seul bain de Jouvence, ce ne serait pas d'aller vers de nouveaux paysages, mais d'avoir d'autres yeux

Marcel Proust

Thank you Sylvio !

