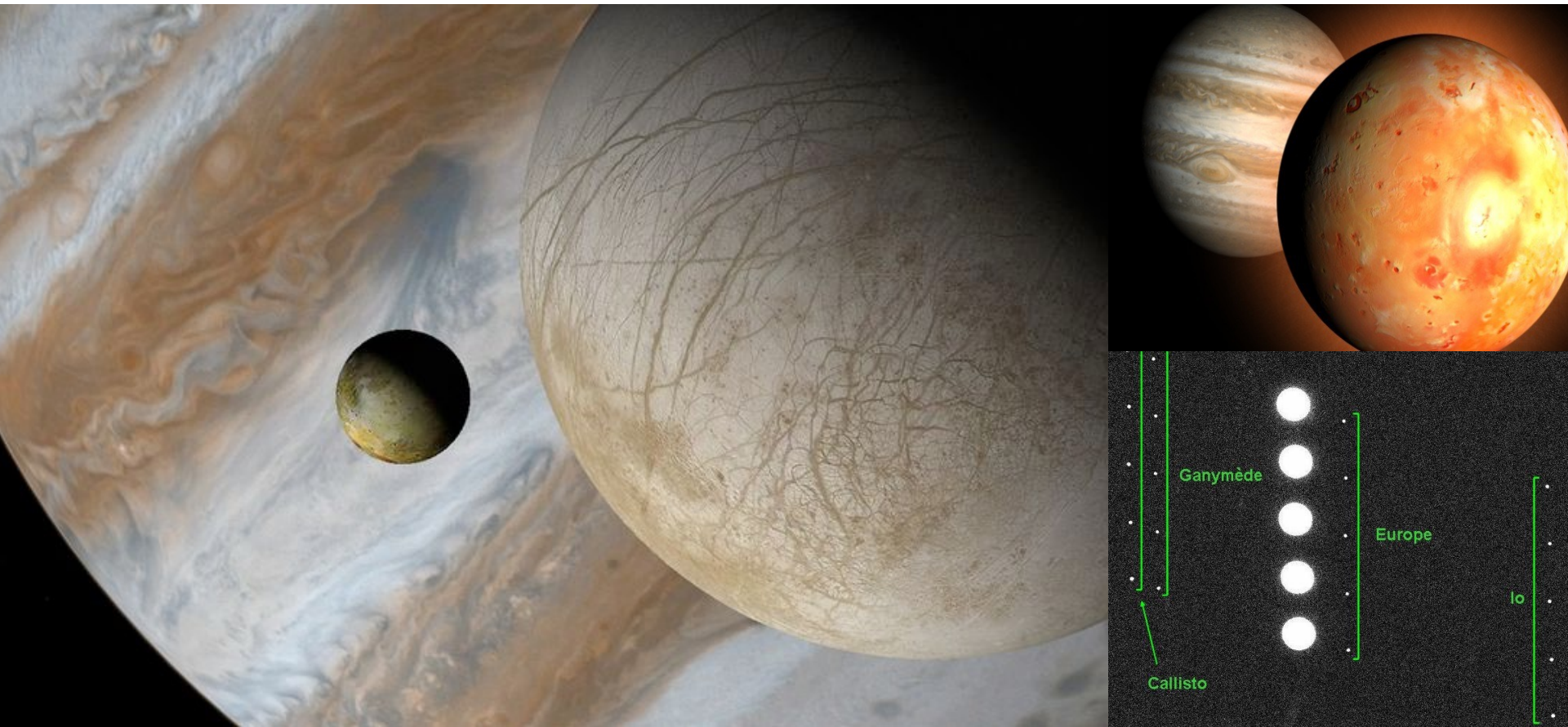


Les satellites galiléens de Jupiter, une longue histoire – Part II

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The Galilean satellites: the tidal acceleration in question



Acceleration or deceleration?

References	\dot{n}_1/n_1	\dot{n}_2/n_2	\dot{n}_3/n_3	Units in 10^{-10}yr^{-1}
de Sitter (1928)	3.3+/-0.5	2.7+/-0.7	1.5+/-0.6	
Lieske (1987)	-0.074+/-0.087	-0.082+/-0.097	-0.098+/-0.153	
Vasundhara et al. (1996)	2.46+/-0.73	-1.27+/-0.84	-0.022+/-1.07	
Aksnes & Franklin (2001)	3.6+/-1.0			

Introducing N-body code and fitting to astrometry data

One step forward...

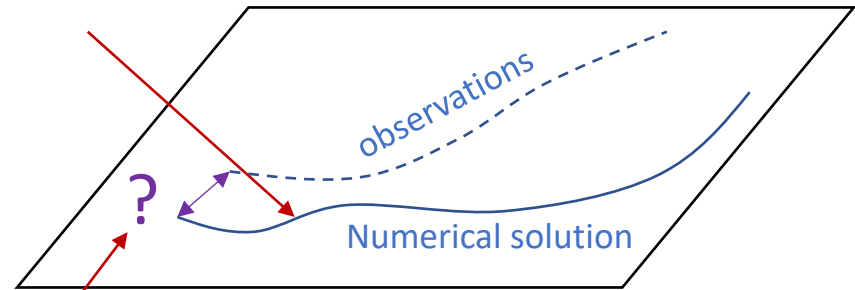
Integration of equations of motion

$$\ddot{\vec{r}}_i = -G(m_0 + m_i) \left(\frac{\vec{r}_i}{r_i^3} - \nabla_i U_{\vec{r}_i} + \nabla_0 U_{\vec{r}_i} \right) + \sum_{j=1, j \neq i}^N Gm_j \left(\frac{\vec{r}_j - \vec{r}_i}{r_{ij}^3} - \frac{\vec{r}_j}{r_j^3} - \nabla_j U_{\vec{r}_j} + \nabla_i U_{\vec{r}_j} + \nabla_j U_{\vec{r}_i} - \nabla_0 U_{\vec{r}_j} \right)$$

$$+ \frac{(m_0 + m_i)}{m_i m_0} (\vec{F}_{\vec{r}_i}^T - \vec{F}_{\vec{r}_i}^T) - \frac{1}{m_0} \sum_{j=1, j \neq i}^N (\vec{F}_{\vec{r}_j}^T - \vec{F}_{\vec{r}_j}^T) + GR$$

Simultaneously with the variational equations

$$\frac{\partial}{\partial c_l} \left(\frac{d^2 \vec{r}_i}{dt^2} \right) = \frac{1}{m_i} \left[\sum_j \left(\frac{\partial \vec{F}_i}{\partial \vec{r}_j} \frac{\partial \vec{r}_j}{\partial c_l} + \frac{\partial \vec{F}_i}{\partial \dot{\vec{r}}_j} \frac{\partial \dot{\vec{r}}_j}{\partial c_l} \right) + \frac{\partial \vec{F}_i}{\partial c_l} \right]$$

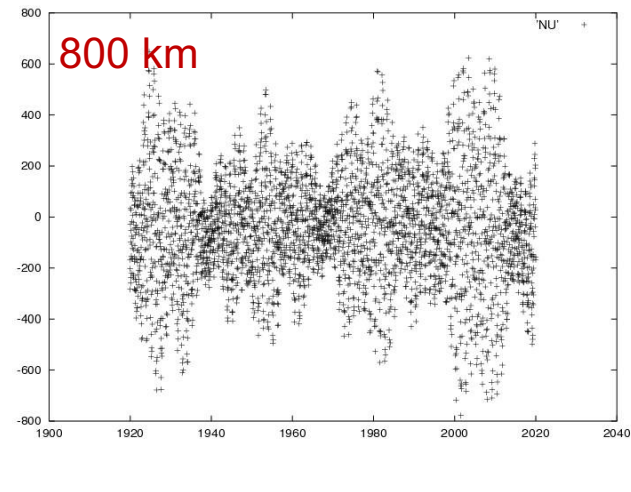
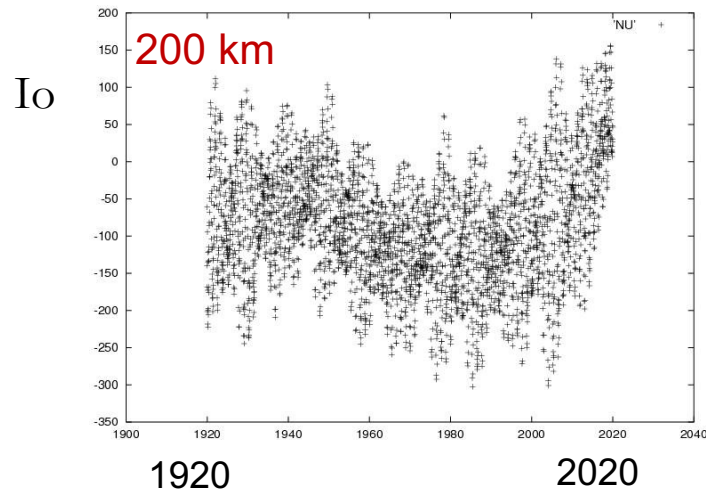


Integration of the variational system is much more tricky and computing time consuming than equations of motion.

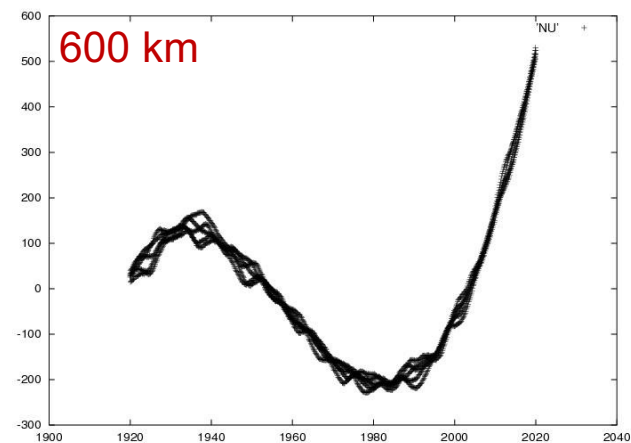
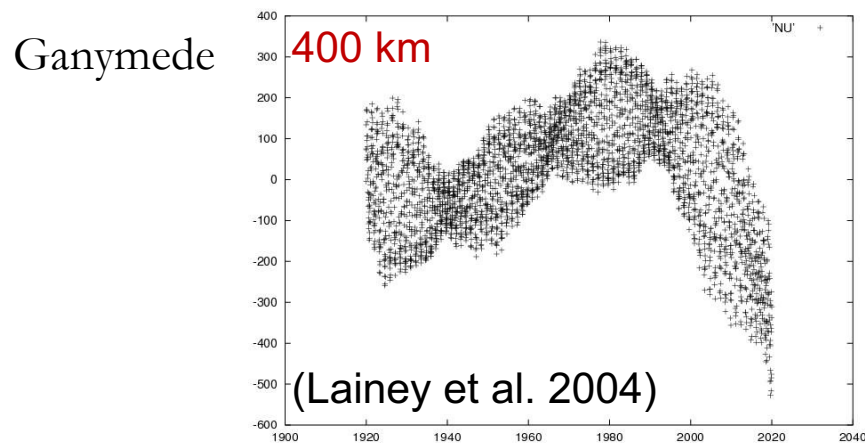
Comparing numerical solution to Sampson-Lieske

Internal precision of Sampson-Lieske's theory over 1 century:

→ few hundreds of kilometers on the longitudes!



Europa



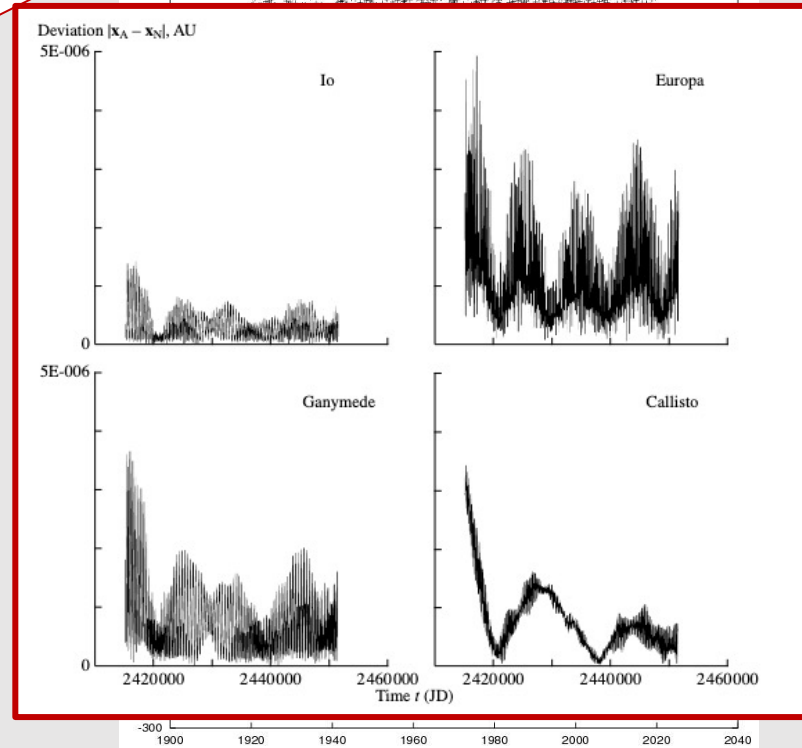
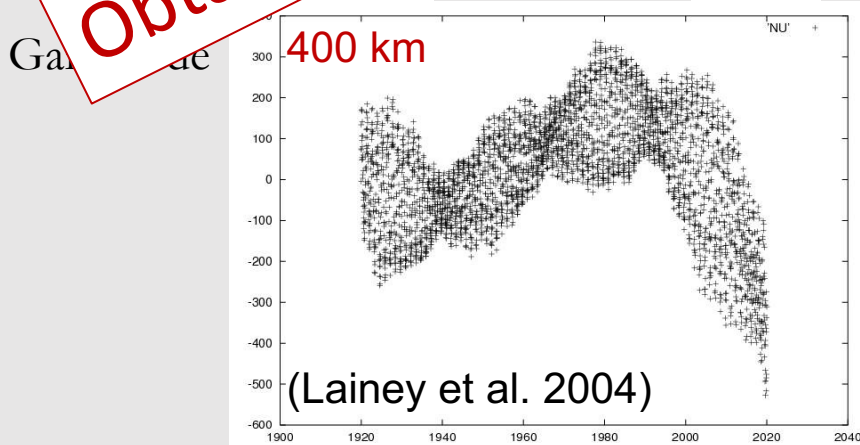
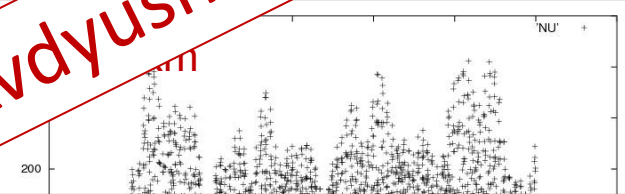
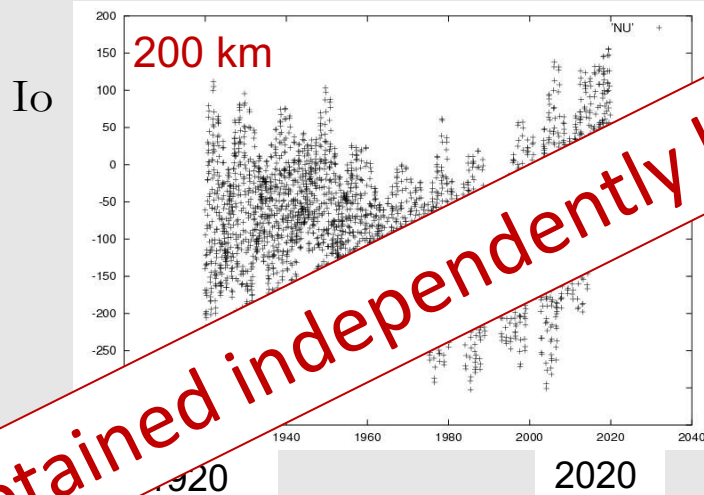
Callisto

Comparing numerical solution to Sampson-Lieske

Internal precision of Sampson-Lieske's theory over 1 cent

→ few hundreds of kilometers on the longitudinal

Obtained independently by Avdyushev 2004



Europa

Callisto

Comparing numerical solution to Sampson-Lieske

Report from Sylvio Ferraz-Mello Lainey's PhD thesis

Report on the doctor thesis "Théorie Dynamique des Satellites Galiléens" by Valéry Lainey

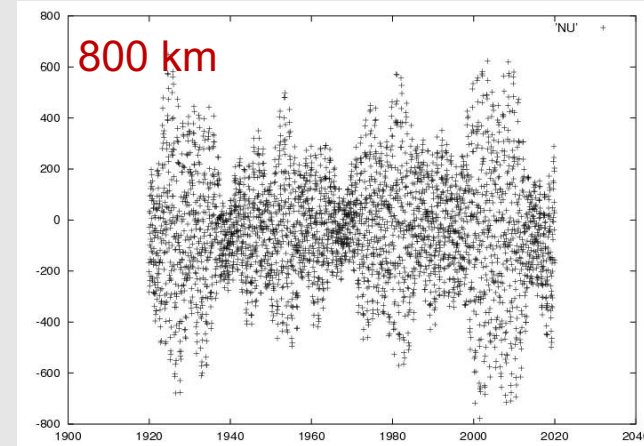
The main contribution of this thesis is a new theory of the motion of the Galilean Satellites of Jupiter. It lies in the tradition of the Bureau des Longitudes (IMCCE) where, since Andoyer, efforts were done to construct theories and algorithms able to produce good ephemerides for these satellites. The difference is that, now, we may use the decades of progress done in the improvement of computing machines which allowed, for the first time, the construction of a numerical theory able to be extended over one century or more.

To contribute with this work, I would like to make some comments.

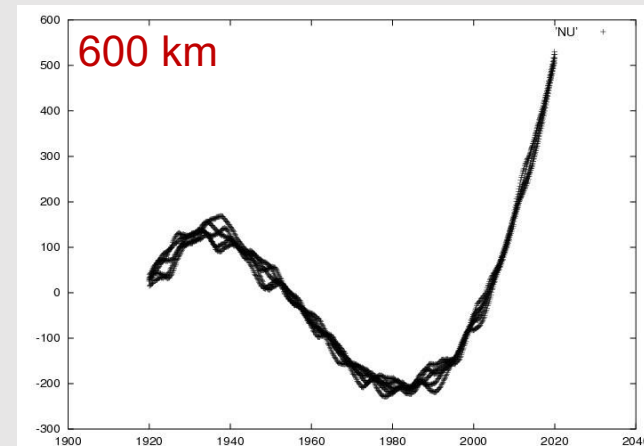
My first comment concerns the analysis of the perturbations usually neglected. In chapter I-2.3, a comment is done concerning the absorption of secular terms, but this very comment is not properly taken into account in Chapter I-3. Let us take, for instance, the largest of the perturbations listed in section I-3.7.1, which amounts to 9.000 km in one century. It is certainly due, mainly, to a difference in longitude of about 1.2 degrees, which corresponds to a contribution of only $1.6E-7$ to the constant perturbation sigma (see Tisserand, vol.IV, p.17 or reference [18], p. 65). This value means, indeed, a correction to the mean motion much larger than the current precision of its determination. Nevertheless, because of the lack of precision in the measurements of the distance scale, the mean-motion plays, actually, the role of constant of the motion, and a correction as small as the one obtained will disappear when translated into semi-major axis. Therefore, it seems to me that the relevant contribution of the considered perturbations is not given by the bulk variation in one century, but by the oscillations seen along that time. Their amplitude should be the quantity to be listed in Table 3.1. Looking at the figures, I would dare to say that the most important of the listed effects is that coming from the motion of Jupiter's equator.

I have been puzzled by the big deviations between the given theory and Lieske's theory shown in sec II-2.2. The explanation considering the problems arising by the variables used by Sampson is not very convincing, given the progressive aspect

theory over 1 century:
longitudes!



Europa



Callisto

Evolution of physical modeling

Sampson 1921

- The four Galilean moons
- Jupiter with its J_2 and J_4
- Jupiter's precession
- The Sun

Lainey (NOE-5-2010-GAL)

- The four Galilean moons with their J_2 and c_{22}
- Jupiter with its $J_2, J_3, J_4, J_6, c_{22}, s_{22}$
- Jupiter's precession
- The Sun and Saturn
- Tides inside Io and Jupiter (constant k_2/Q)

Lieske 1970s/1998

Same as Sampson but corrected for:

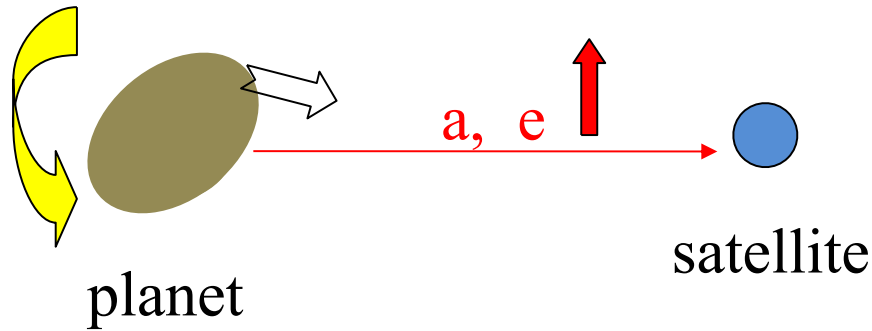
Calculus error, De Haerdtl inequality, extra solar terms, Laplace resonance libration,

Jacobson (JUP310)

- The four Galilean moons and Amalthea
- Jupiter with its J_2, J_4, J_6
- Jupiter's precession
- The Sun (inner planets in Solar mass), Saturn, Uranus, Neptune



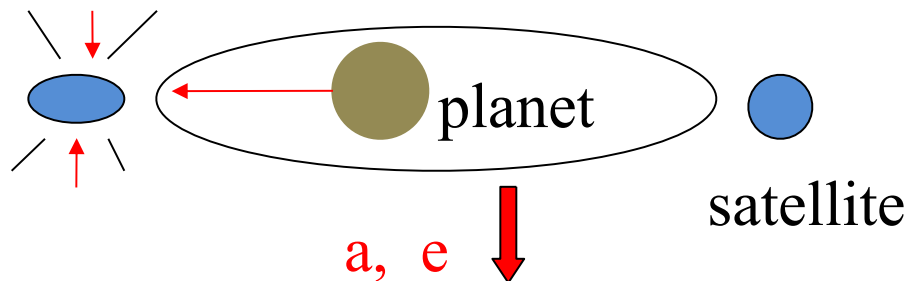
Implication of tidal dissipation on orbital motion



Secular deceleration on
the mean motion

Jovian k_2/Q

Competition between tidal dissipation effects



Secular acceleration on
the mean motion

Moon's k_2/Q

Implication of tidal dissipation on orbital motion

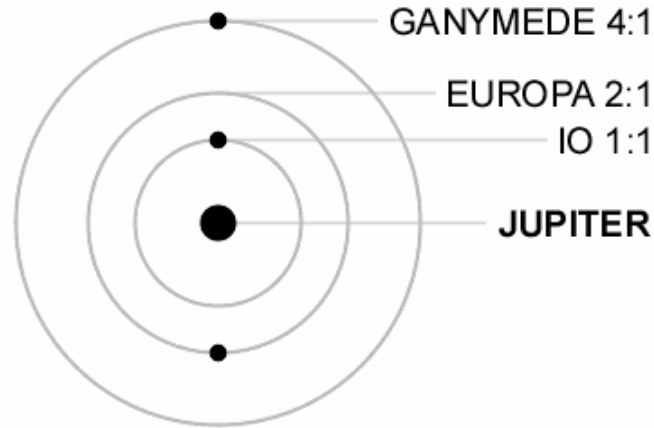
A matter of dynamics...

$$n_1 - 2n_2 = \nu$$

$$n_2 - 2n_3 = \nu$$

$$n_1 - 3n_2 + 2n_3 = 0$$

$$\langle L_1 - 3L_2 + 2L_3 \rangle = 180^\circ$$



The Laplace resonance is dynamically stable

The three moons *share* their [orbital energy](#) and [angular momentum](#)

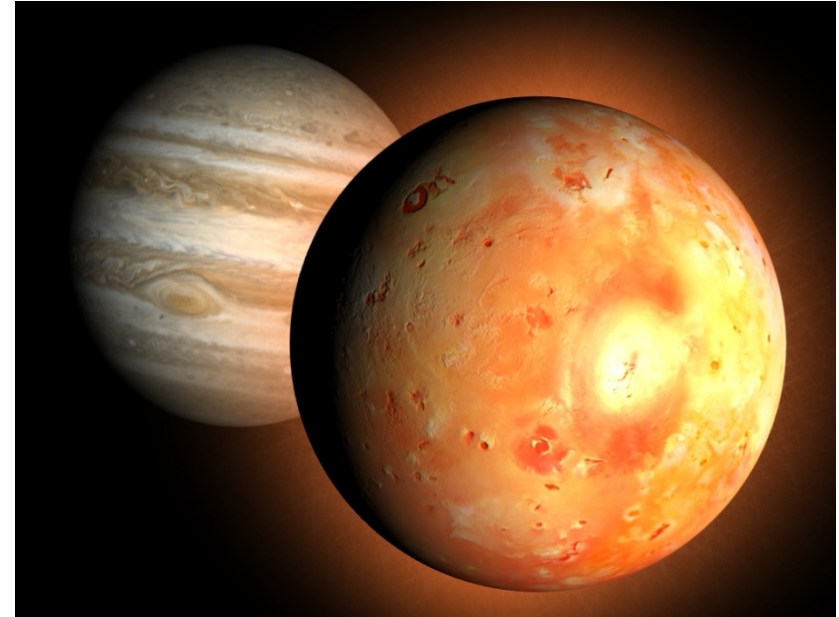
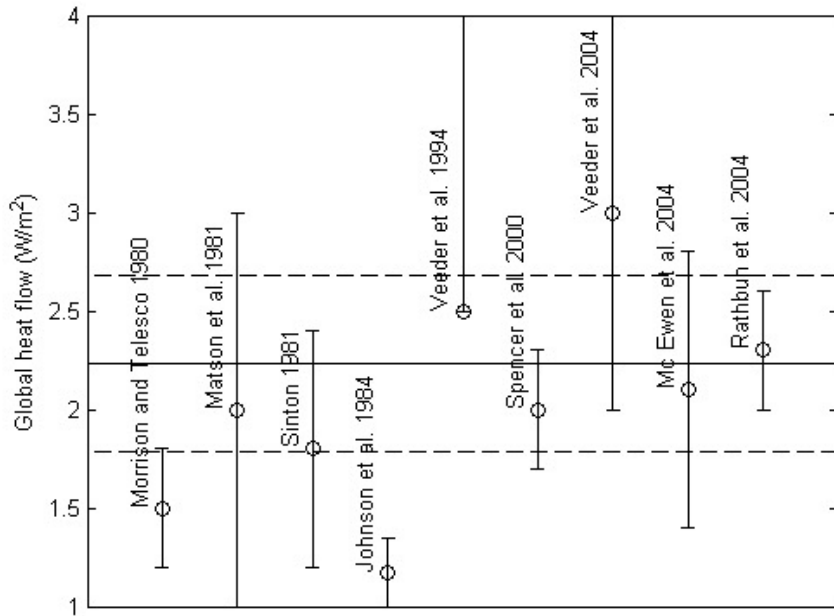
IMPORTANT:

Any perturbation affecting one of the moons will affect immediately the two others!

Estimations of tides in the Galilean system: XXIth century

Fit of Io's tidal dissipation provides $k_2/Q = 0.015 \pm 0.003$ (Lainey et al. 2009)

One can compare our value with the ones derived from IR emission



Lainey et al. (2009) obtained a very good agreement and confirmed the values derived from heat flux observations.

Those values were confirmed recently by Park et al. (2025)

Io's volcanism and tides

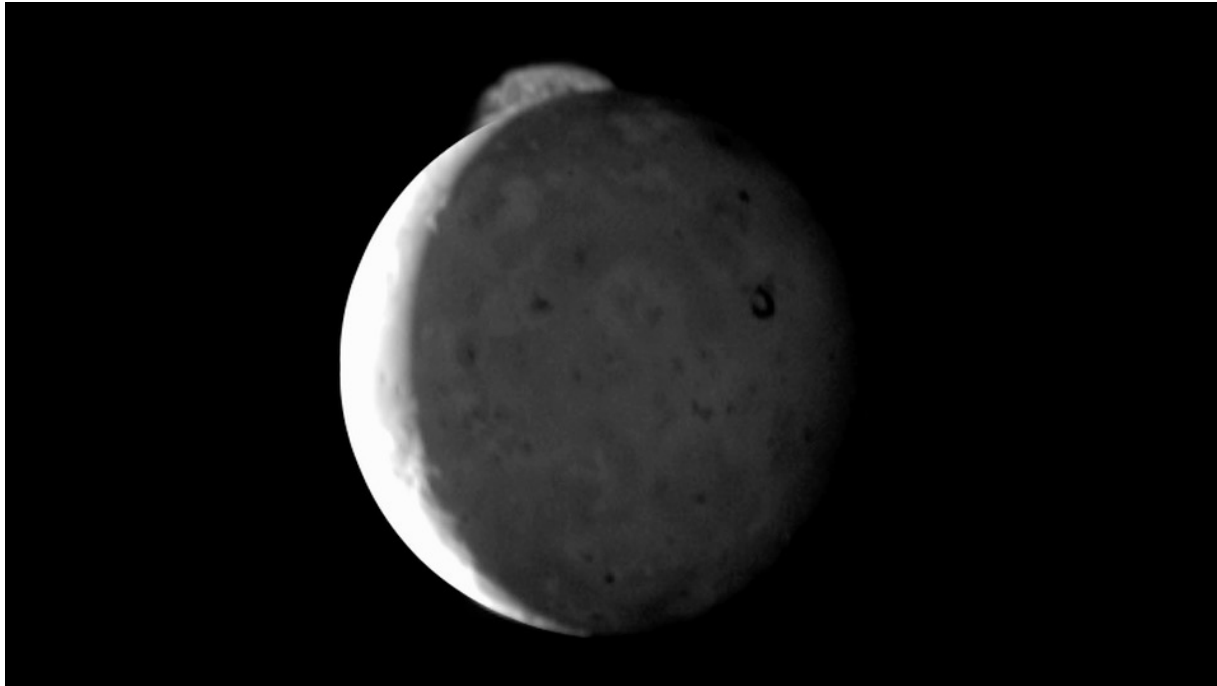
The orbital energy reservoir of the whole system involved in the Laplace resonance is

$$E = -2.672 \times 10^{31} \text{ J}$$

The orbital energy loss from Io's internal tide activity is

$$\dot{E} = (9.33 \pm 1.87) \times 10^{13} \text{ W} \quad \text{Lainey et al. (2009)}$$

There is enough energy in the orbits to still power Io's volcanism over about 9Byr



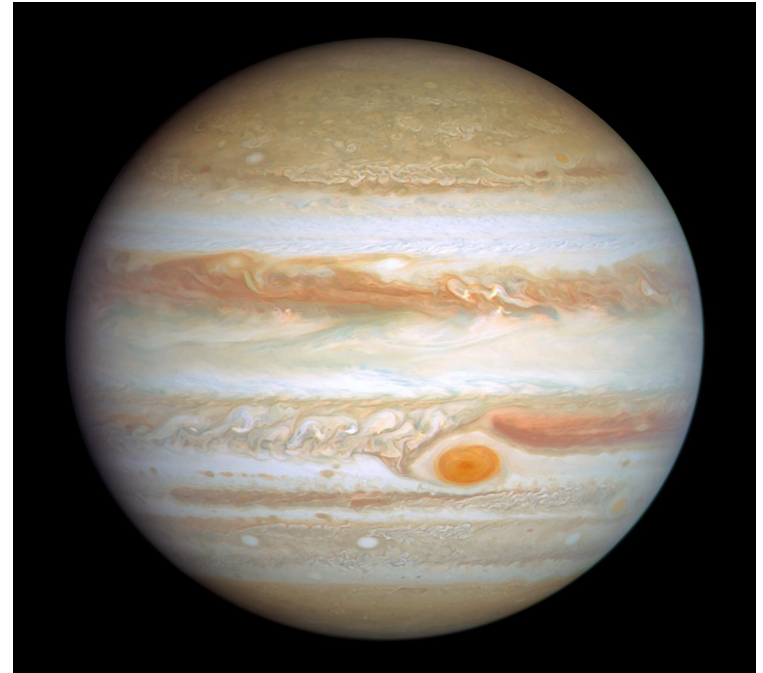
What physical mechanism triggers tides in giant planets ?

Equilibrium Tides:

- Viscoelastic deformation of core (Dermott 1979, Remus et al. 2015)
- Convective viscosity in envelope (Terquem (2024))

Dynamical Tides:

- G-modes in stably stratified layers (Morales et al. 2009, Fuller et al. 2016)
- Inertial waves in convective envelope (Ogilvie & Lin 2007, Guenel et al. 2014)



Sensitivity to tidal frequency

$Q(X) ?$

NB: Most (all?) dynamical studies of the Galilean system assume a constant Jovian k_2/Q

Conclusion

Our comprehension of the Galilean system is going to radically improve in the coming decade

