

Scattering Amplitudes in Effective Gravitational Theories

Stavros Mougialakakos



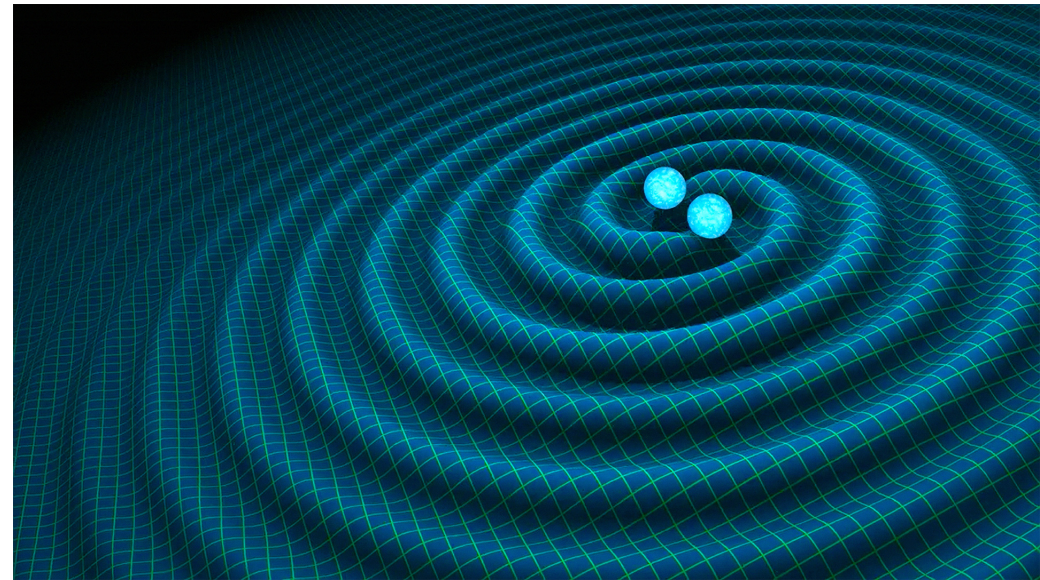
Based on:

- M. Levi, S. Mougialakakos and M. Vieira; [arXiv : 1912.06276](#)

Observational Window on gravity

The detection of gravitational waves (GW150914) has opened a new window on the physics of our universe:

- For the first time detection and test of GR in the “strong” gravity coupling regime
- For the first time dynamics of BH/NS
(not just static object curving space-time)

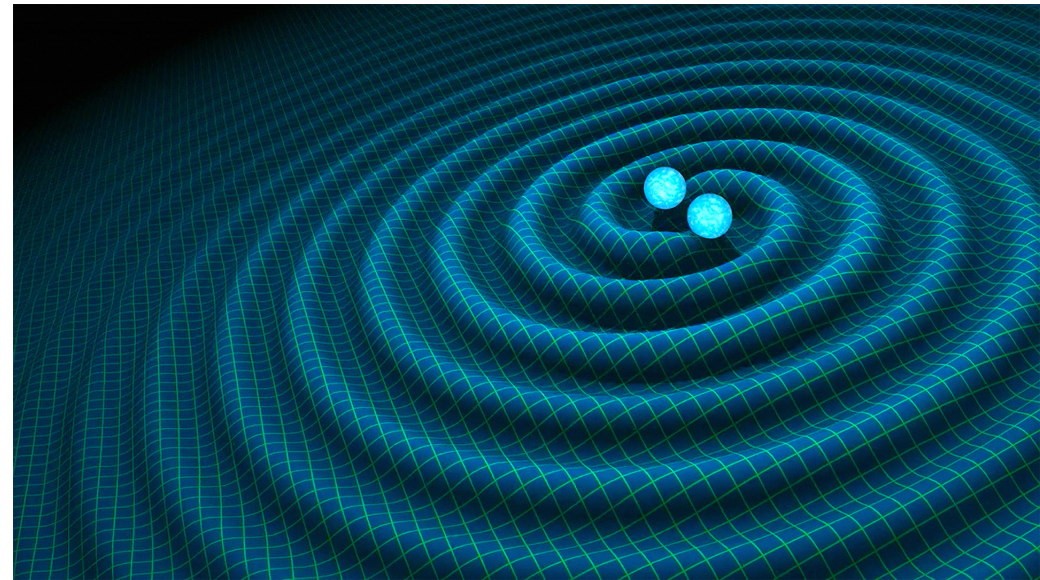


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Gravitational Wave Era has begun!



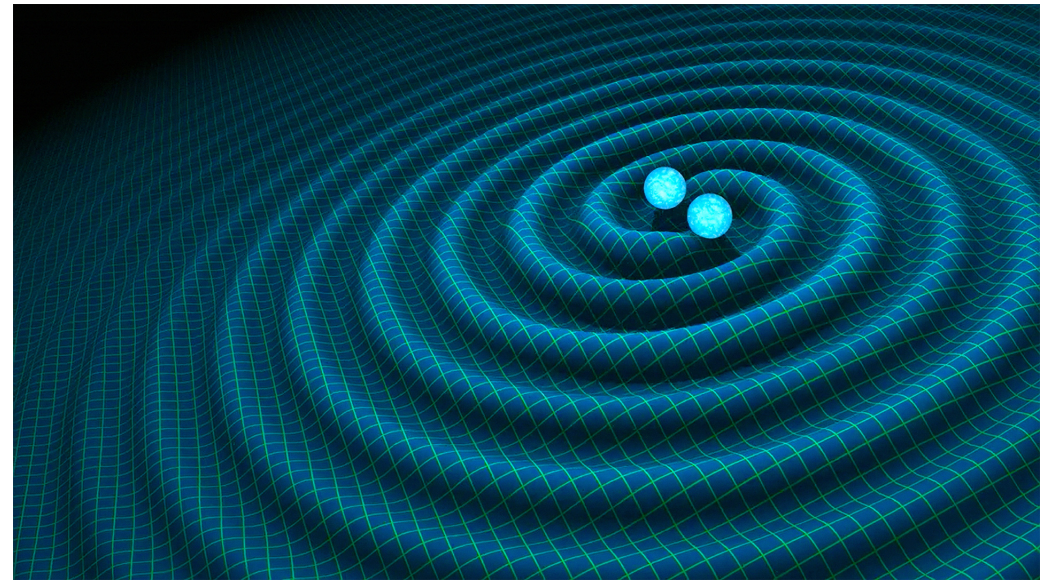
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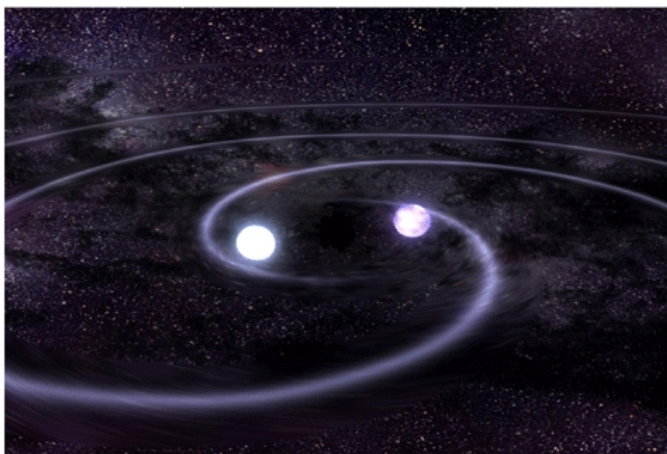
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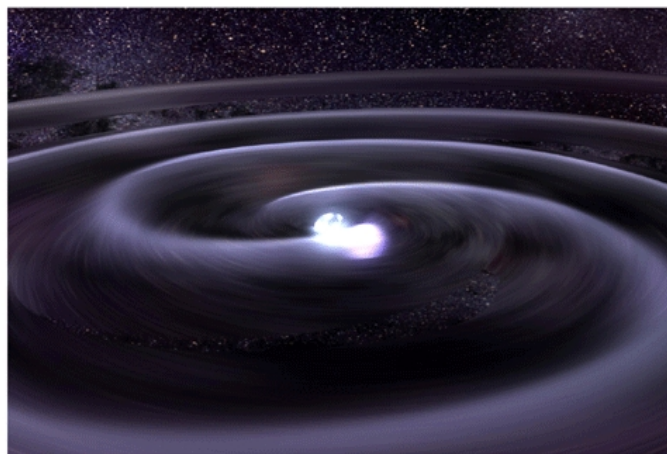
What can we learn from the gravitational wave signals?



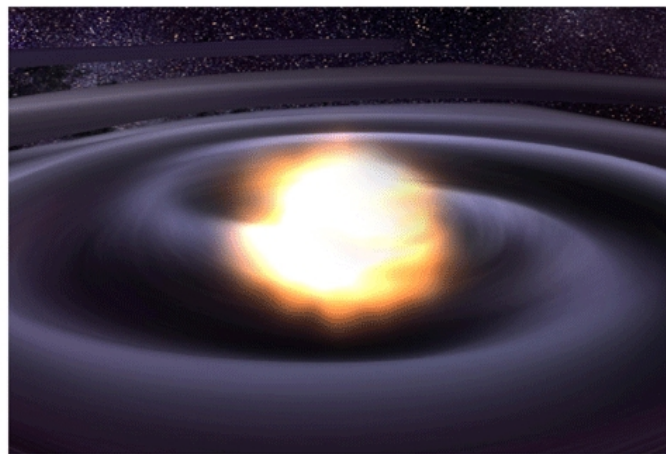
2-body problem



Inspiral

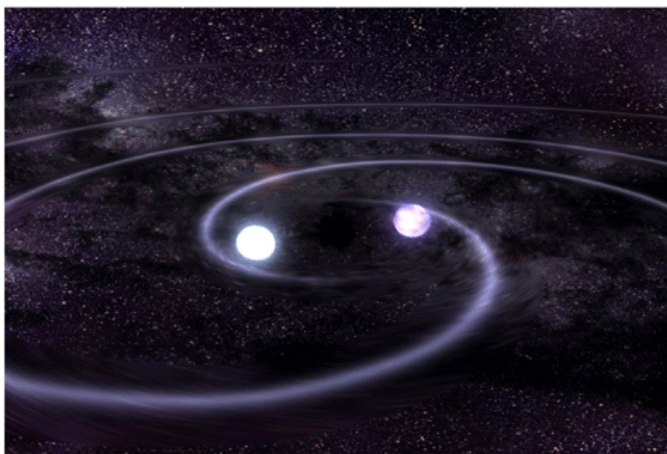


Merger

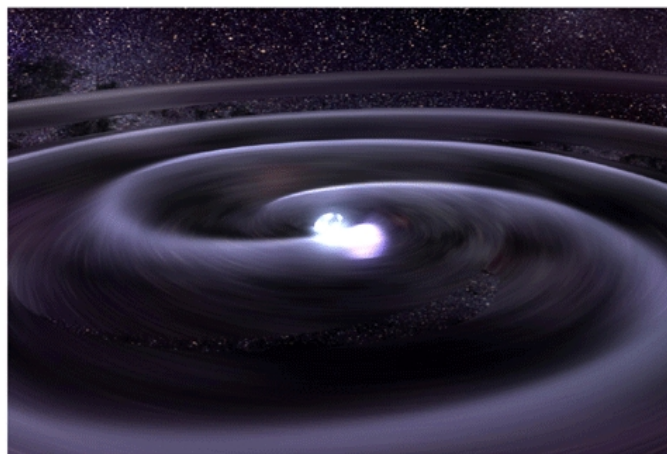


Ringdown

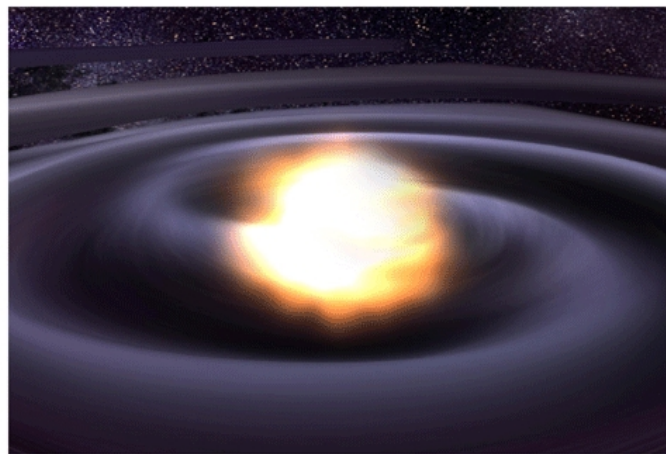
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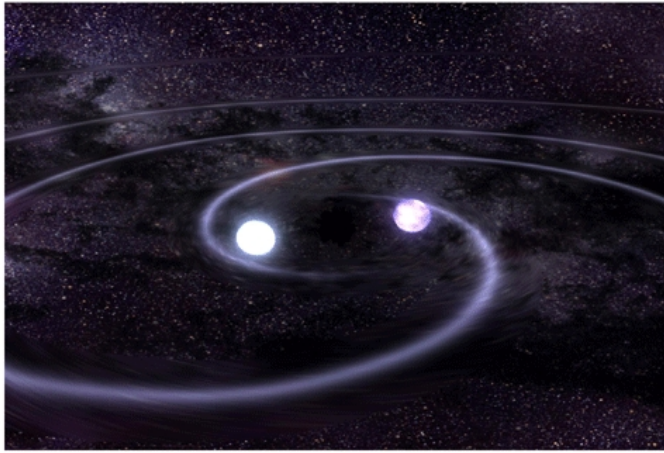


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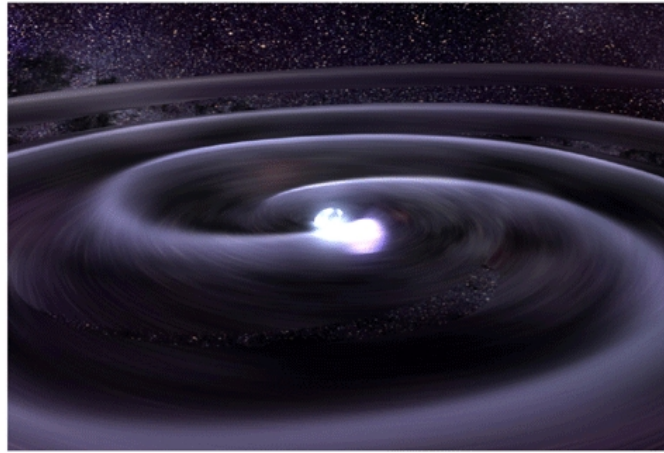


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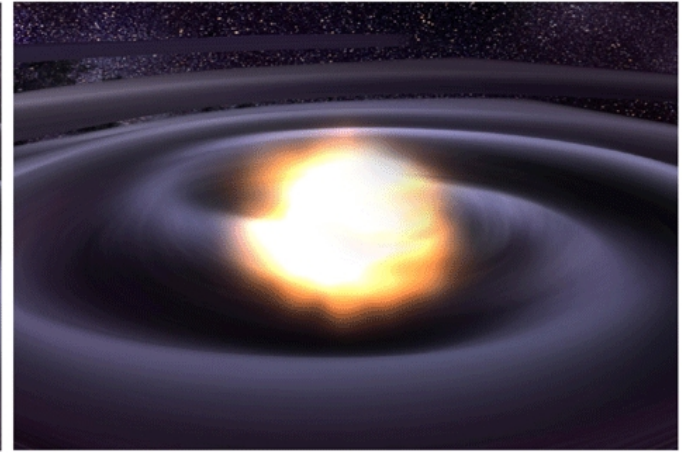
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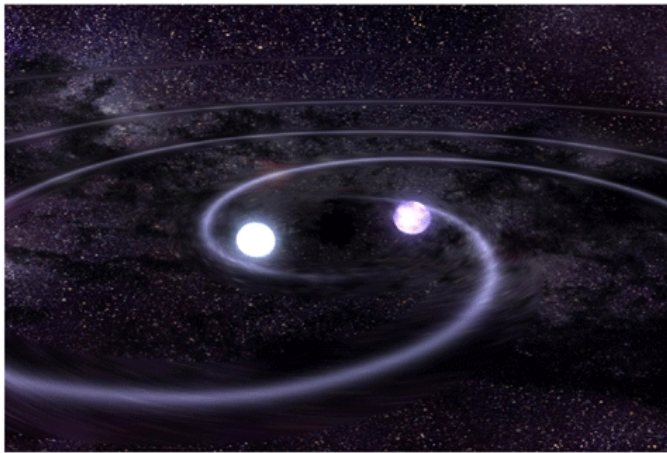


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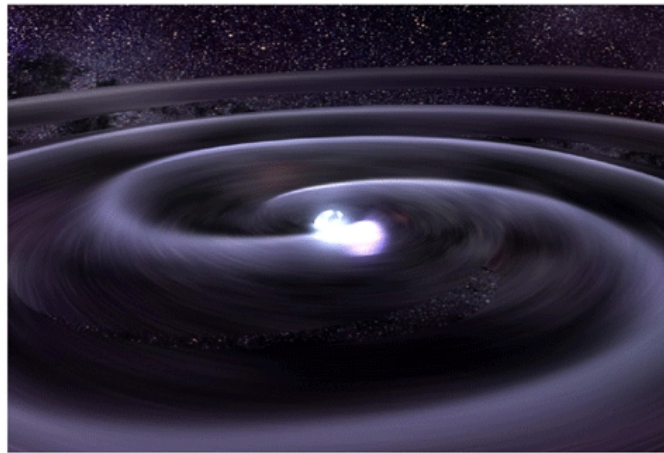
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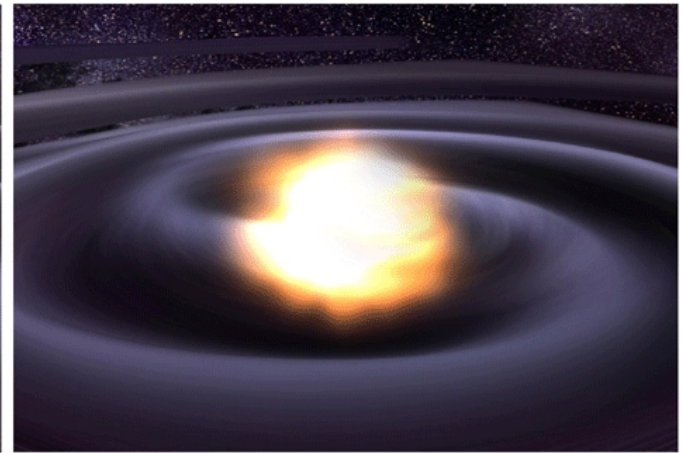
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Can the particle physics community contribute to this problem?

Quantum Gravity



UV Completion of Gravity

Quantum Gravity



UV Completion of Gravity

- Main candidate: Superstring Theory
- Exciting field of research with many questions left to be answered

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I will not talk about it...

(“useful” for our problem) Quantum Gravity



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Quantum Gravity as an EFT

John F. Donoghue; arXiv : gr-qc/9512024

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We can isolate the classical from the quantum contributions

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We can isolate the classical from the quantum contributions



PNEFT

W. D. Goldberger, I. Z. Rothstein; arXiv : hep-th/0409156

Very efficient for classical contributions due to good control of power counting

Particle Physicist's Point of View on the gravitational 2-body problem



EFT of Post-Newtonian Gravity

W.D Goldberger, I. Rothstein, R. Porto ,
M. Levi et al

- Classical computation
- Takes advantage of QFT toolbox
- Non relativistic computation
- Can deal effectively with spin effects
- State of the art (conservative):
4-PN without spins
4,5-PN(S^3)



Scattering Amplitudes and Post-Minkowskian

Z. Bern, N. Arkani-Hamed, P. Vanhove, N.E.J. Bjerrum-Bohr, J. Donoghue, D. Kosower et al.

- Quantum computation
- Takes advantage of modern methods for on-shell scattering amplitudes (BCJ relations/double copy)
- Fully relativistic computation
- Active work for inclusion of spin effects
[arXiv:1709.04891](#), [arXiv:1812.08752](#)
- State of the art (conservative): 3-PM without spins

Scattering Amplitudes and Post-Minkowskian expansion

John F. Donoghue; arXiv : gr-qc/9512024v1

- Non-renormalizability can be handled order by order
- Long-range contributions can be calculated in this framework since they depend only on the structure of the low-energy fields and the classical background

$$\mathcal{L}_g = \sqrt{g} \left\{ \frac{2}{\kappa^2} R + c_1 R^2 + c_2 R_{\mu\nu} R^{\mu\nu} + \mathcal{O}(R^3) \right\}$$

Scattering Amplitudes and Post-Minkowskian expansion

Loops give classical contributions!

$$\mathcal{M}_{n-loop} = \frac{M^3}{\hbar \sqrt{-s}} (r_S \sqrt{-s})^{n+1} \sum_{k=0}^n \alpha_k (\lambda \sqrt{-s})^k$$

where

$$\lambda = \frac{\hbar}{M}$$

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WHY?!

Scattering Amplitudes and Post-Minkowskian expansion

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BECAUSE

Restoring units in Klein-Gordon eq:

$$(\square + \frac{m^2}{\hbar^2})\phi(x) = 0$$

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When we have massless+massive particles, the powercounting gives us above.

Scattering Amplitudes and Post-Minkowskian expansion

The problem of getting a Post-Minkowskian expansion of the potential comes down to computing loop diagrams.

$$V(\boldsymbol{p}, \boldsymbol{r}) = \sum_{n=1}^{\infty} \left(\frac{G}{|\boldsymbol{r}|} \right)^n c_n(\boldsymbol{p}^2)$$

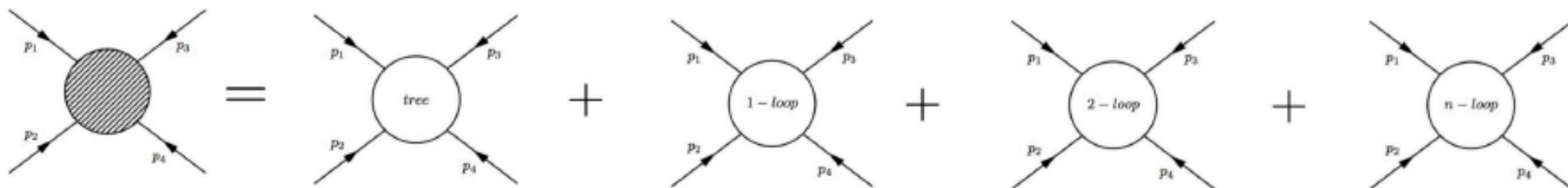
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WHICH TOPOLOGIES ARE WE LOOKING FOR?

Scattering Amplitudes and Post-Minkowskian expansion



$$\frac{Gm_1m_2}{r}$$

$$\frac{G^2m_1^2m_2}{r^2}, \frac{G^2m_1m_2^2}{r^2}$$

$$\frac{G^3m_1^3m_2}{r^3}, \frac{G^3m_1^2m_2^2}{r^3}, \frac{G^3m_1m_2^3}{r^3}$$

$$\frac{G^{n+1}m_1m_2}{r^{n+1}} \sum_{k=0}^n m_1^k m_2^{n-k}$$

In general:

$$\frac{\hbar G^2m_1m_2}{r^3}$$

$$\frac{\hbar G^3m_1^2m_2}{r^4}, \frac{\hbar G^3m_1m_2^2}{r^4}$$

$$\frac{\hbar G^{n+1}m_1m_2}{r^{n+2}} \sum_{k=0}^{n-1} m_1^k m_2^{n-1-k}$$

$$\frac{\hbar^2 G^3m_1m_2}{r^5}$$

$$\frac{\hbar^2 G^{n+1}m_1m_2}{r^{n+3}} \sum_{k=0}^{n-2} m_1^k m_2^{n-2-k}$$

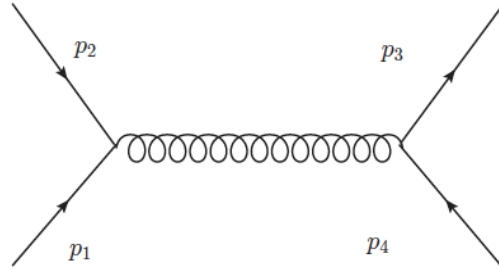
...

$$\frac{\hbar^n G^{n+1}m_1m_2}{r^{2n+1}}$$

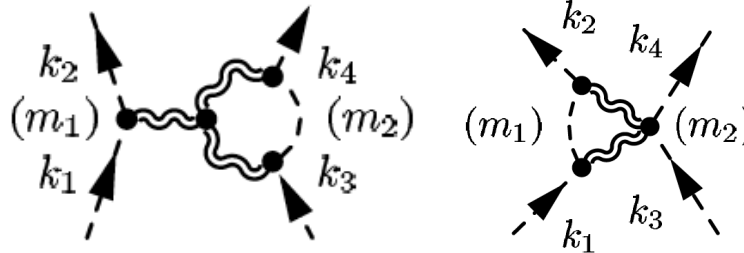
Scattering Amplitudes and Post-Minkowskian expansion

Classical terms

- Tree-level:



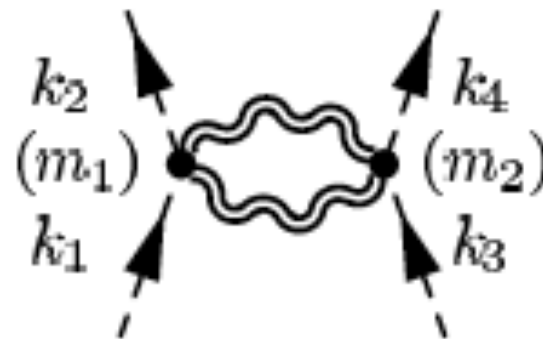
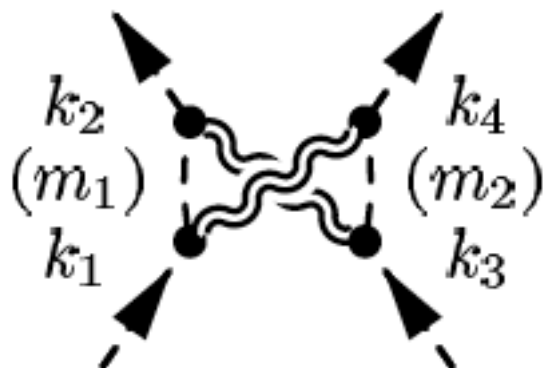
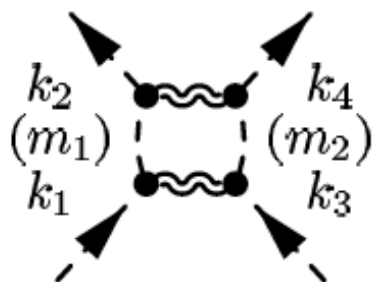
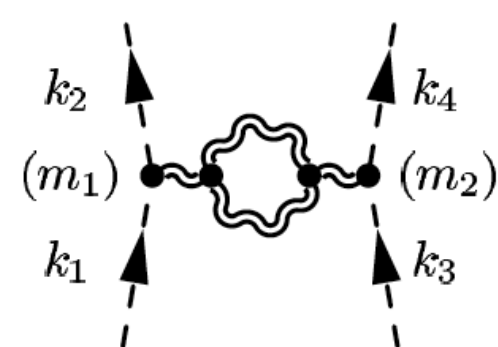
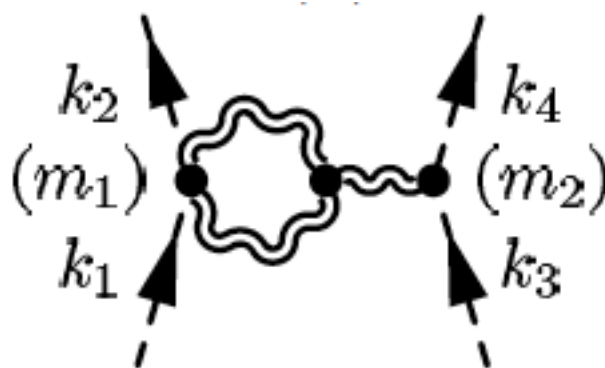
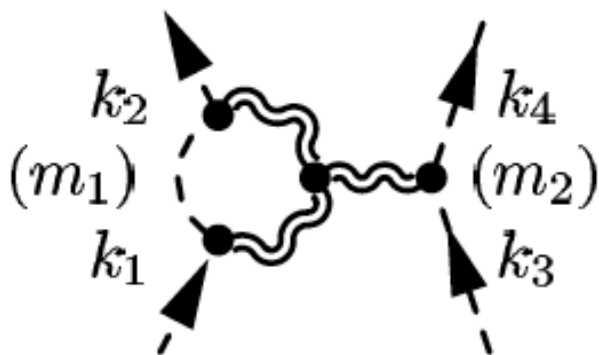
- 1-loop:



Scattering Amplitudes and Post-Minkowskian expansion

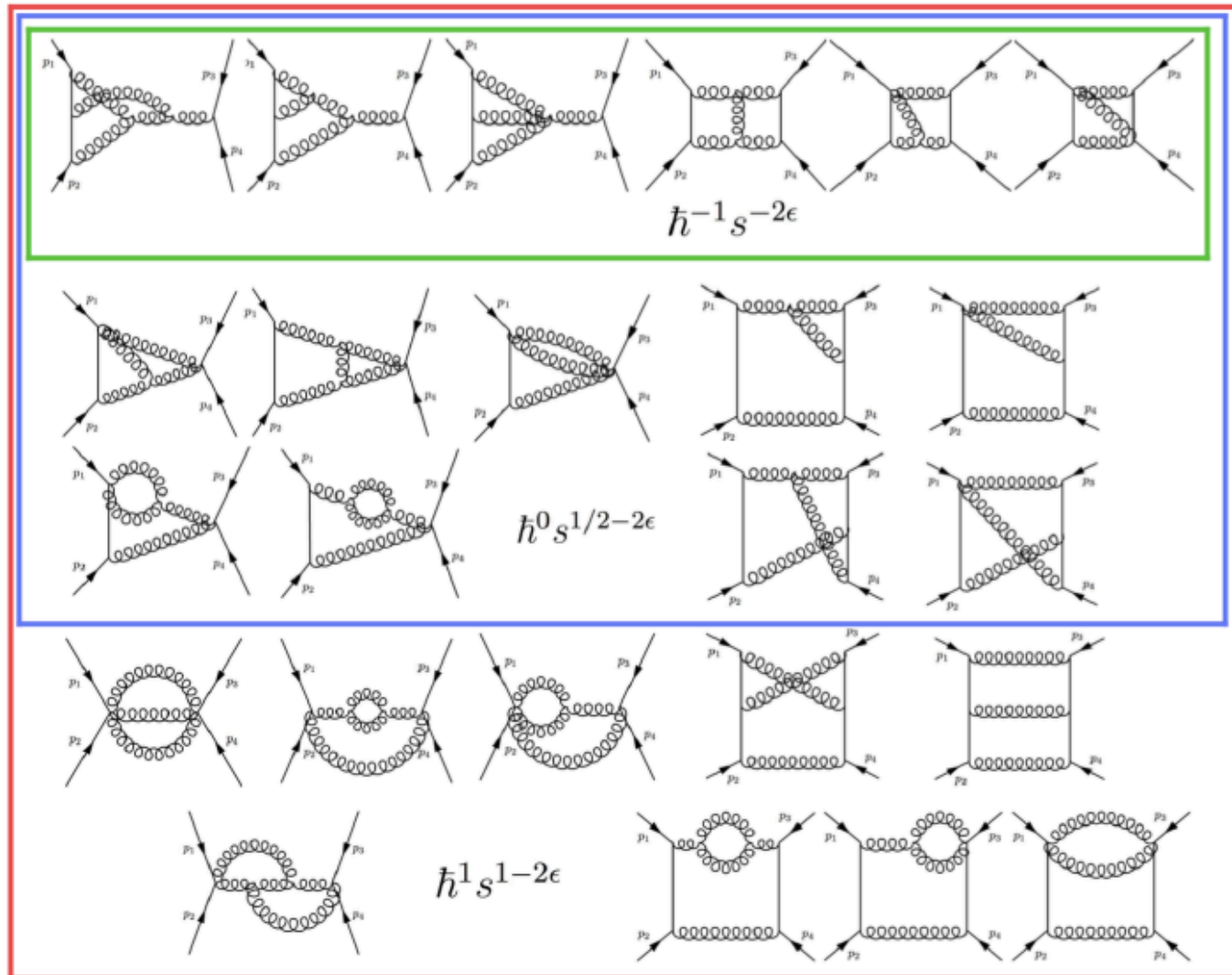
Quantum contributions

- 1-loop:



Scattering Amplitudes and Post-Minkowskian expansion

- 2-loops:
(both classical and quantum contributions)



Scattering Amplitudes and Post-Minkowskian expansion

We know which diagrams we are looking for and what contributions they give.

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DOUBLE COPY!!

$\text{gravity} \sim (\text{gauge theory}) \times (\text{gauge theory}).$

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KLT relation of string amplitudes



BCJ relations/ double copy

spinor helicity formalism

Generalized Unitarity

Scattering Amplitudes and Post-Minkowskian expansion

[illegible]

Scattering Amplitudes and Post-Minkowskian expansion

State of the art computation (Conservative Sector)

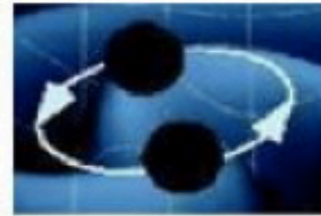
- Spin-less: 3 PM (2 loops) [arXiv:1908.01493v1](#).
- Spin effects: 2 PM (1 loop) [arXiv:1812.08752v3](#)

EFT of Post-Newtonian Gravity

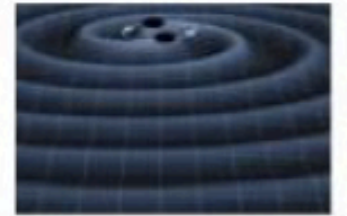
EFT of Post-Newtonian Gravity



r_s



r



λ

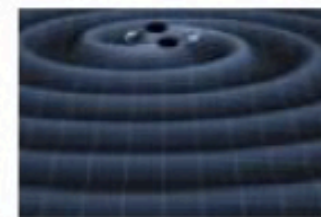
EFT of Post-Newtonian Gravity



r_s



r



λ

Hierarchy of scales:

scale of internal structure: $r_s \sim Gm$

scale of orbital separation: $r \sim r_s/v^2$

scale of radiation wavelength: $\lambda_{\text{rad}} \sim r/v$

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$S_{pp} \equiv$ point particle action

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where

$$S_{pp} = \int d\sigma \left[-m\sqrt{u^2} - \frac{1}{2} S_{\mu\nu} \Omega^{\mu\nu} + L_{\text{SI}}[u^\mu, S_{\mu\nu}, g_{\mu\nu}(y^\mu)] \right]$$

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and

$$L_{\text{SI}} = \sum_{n=1}^{\infty} \frac{(-1)^n}{(2n)!} \frac{C_{ES^{2n}}}{m^{2n-1}} D_{\mu_{2n}} \cdots D_{\mu_3} \frac{E_{\mu_1\mu_2}}{\sqrt{u^2}} S^{\mu_1} S^{\mu_2} \cdots S^{\mu_{2n-1}} S^{\mu_{2n}} \\ + \sum_{n=1}^{\infty} \frac{(-1)^n}{(2n+1)!} \frac{C_{BS^{2n+1}}}{m^{2n}} D_{\mu_{2n+1}} \cdots D_{\mu_3} \frac{B_{\mu_1\mu_2}}{\sqrt{u^2}} S^{\mu_1} S^{\mu_2} \cdots S^{\mu_{2n-1}} S^{\mu_{2n}} S^{\mu_{2n+1}}$$

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Proven useful to make a Kaluza-Klein reduction over the time dimension to decompose the metric, since we are working in the NR limit and the orbital modes are instantaneous at leading order:

$$ds^2 = g_{\mu\nu} dx^\mu dx^\nu \equiv e^{2\phi} (dt - A_i dx^i)^2 - e^{-2\phi} \gamma_{ij} dx^i dx^j$$

EFT of Post-Newtonian Gravity Spinning Particle

M. Levi, S. Mougiakakos and M. Vieira; [arXiv : 1912.06276](#)

MOTIVATION 1

$$n + l + \text{Parity}(l)/2$$

PN correction

$l \backslash n$	(N ⁰)LO	N ⁽¹⁾ LO	N ² LO	N ³ LO	N ⁴ LO
S ⁰	1	0	3	0	25
S ¹	2	7	32		
S ²	2	2	18		
S ³	4	24			
S ⁴	3				

The number of n-loop graphs that enter at each order=measure for loop computational scale

EFT of Post-Newtonian Gravity Spinning Particle

M. Levi, [S. Mougialakos](#) and M. Vieira; [arXiv : 1912.06276](#)

MOTIVATION 2

The Tulczyjew gauge for the rotational degrees of freedom, which involves the linear momentum, can no longer be approximated by the 4-velocity:

$$p^\mu = m \frac{u^\mu}{\sqrt{u^2}} + \mathcal{O}(S^2)$$

MOTIVATION 3

We can compare with results coming from scattering amplitudes for $s > 1$, specifically $s = 3/2$

[arXiv:1709.04891](#), [arXiv:1812.08752](#)

EFT of Post-Newtonian Gravity Spinning Particle

Degrees of Freedom

- Gravitational field: metric+tetrad fields

$$\eta^{ab} \tilde{e}_a^\mu(x) \tilde{e}_b^\nu(x) = g^{\mu\nu}(x)$$

- Particle Coordinate

- Particle Worldline Rotating DOFs:

worldline tetrad: $\eta^{AB} e_A^\mu(\sigma) e_B^\nu(\sigma) = g^{\mu\nu}$

$$\Omega^{\mu\nu} \equiv e_A^\mu \frac{D e^{A\nu}}{D\sigma} \rightarrow S_{\mu\nu} \equiv -2 \frac{\partial L}{\partial \Omega^{\mu\nu}}$$

We then disentangle the worldline tetrad from the tetrad field such that we are left with the local worldline DOFs:

$$\eta^{AB} \Lambda_A^a(\sigma) \Lambda_B^b(\sigma) = \eta^{ab}$$

$$S_{ab}(\sigma)$$

EFT of Post-Newtonian Gravity

Spinning Particle

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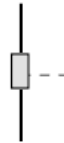
and

$$L_{\text{SI}} = \sum_{n=1}^{\infty} \frac{(-1)^n}{(2n)!} \frac{C_{ES^{2n}}}{m^{2n-1}} D_{\mu_{2n}} \cdots D_{\mu_3} \frac{E_{\mu_1\mu_2}}{\sqrt{u^2}} S^{\mu_1} S^{\mu_2} \cdots S^{\mu_{2n-1}} S^{\mu_{2n}}$$

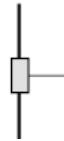
$$+ \sum_{n=1}^{\infty} \frac{(-1)^n}{(2n+1)!} \frac{C_{BS^{2n+1}}}{m^{2n}} D_{\mu_{2n+1}} \cdots D_{\mu_3} \frac{B_{\mu_1\mu_2}}{\sqrt{u^2}} S^{\mu_1} S^{\mu_2} \cdots S^{\mu_{2n-1}} S^{\mu_{2n}} S^{\mu_{2n+1}}$$

EFT of Post-Newtonian Gravity

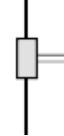
Spinning Particle



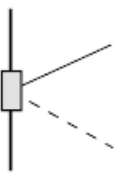
$$= \int dt \left[\frac{C_{BS^3}}{12m^2} S^i S^j \epsilon_{klm} \left[S^m \left(\partial_i \partial_j \partial_l A_k \left(1 + \frac{v^2}{2} \right) + v^l (\partial_t A_{i,jk} + \partial_t A_{k,ij}) + \right. \right. \right. \\ \left. \left. \left. + v^l v^n (A_{i,jkn} - A_{n,ijk}) \right) - \frac{v^i}{2} A_{k,jln} (S^m v^n + S^n v^m) \right] \right],$$



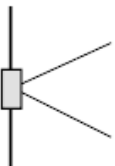
$$= \int dt \left[\frac{C_{BS^3}}{3m^2} S^i S^j \epsilon_{klm} S^m v^l \left(\partial_i \partial_j \partial_k \phi \left(1 + \frac{v^2}{2} \right) - \frac{1}{2} v^i v^n \partial_j \partial_k \partial_n \phi \right) \right],$$



$$= \int dt \left[\frac{C_{BS^3}}{12m^2} S^i S^j \epsilon_{klm} S^m \partial_i \partial_l (\partial_j \sigma_{kn} v^n - \partial_n \sigma_{jk} v^n - \partial_t \sigma_{jk}) \right]$$



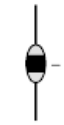
$$= \int dt \left[\frac{C_{BS^3}}{12m^2} S^i S^j \epsilon_{klm} S^m (2\phi_{,ijl} A_k - \phi_{,i} A_{k,jl} + 6\phi_{,il} A_{k,j} + 6\phi_{,j} A_{k,il} + \right. \\ \left. + 4\phi_{,l} A_{k,ij} + 4\phi_{,ij} A_{k,l} + 2\phi_{,ik} A_{j,l} + 2\phi_{,k} A_{j,il} - \delta_{ij} \phi_{,n} A_{k,ln}) \right],$$



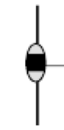
$$= \int dt \left[\frac{C_{BS^3}}{3m^2} S^i S^j \epsilon_{klm} S^m v^l (3\phi_{,j} \phi_{,ik} + 3\phi_{,k} \phi_{,ij} - 3\phi \phi_{,ijk} - \delta_{ij} \phi_{,kn} \phi_{,n}) \right]$$

$$p^\mu = m \frac{u^\mu}{\sqrt{u^2}} + \mathcal{O}(S^2)$$

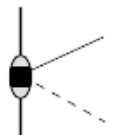
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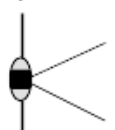
$$= \int dt \left[\frac{C_{ES^2}}{4m^2} S^i S^j \epsilon_{klm} \left[2S^m a^k (A_{l,ij} - A_{j,il} + \delta_{ij} (A_{n,ln} - A_{l,nn})) \right. \right. \\ \left. \left. + \dot{S}^m v^k (A_{l,ij} - A_{j,il} + \delta_{ij} (A_{n,ln} - A_{l,nn})) \right] \right],$$



$$= \int dt \left[\frac{C_{ES^2}}{2m^2} S^i S^j \epsilon_{klm} \left[2S^m a^k (\phi_{,il} v^j - \phi_{,ij} v^l + \delta_{ij} (\partial_t \phi_{,l} + \phi_{,nn} v^l)) \right. \right. \\ \left. \left. + \dot{S}^m v^k (\phi_{,il} v^j + \delta_{ij} \partial_t \phi_{,l} + \delta_{jl} (\partial_t \phi_{,i} + \phi_{,in} v^n)) \right] \right]$$



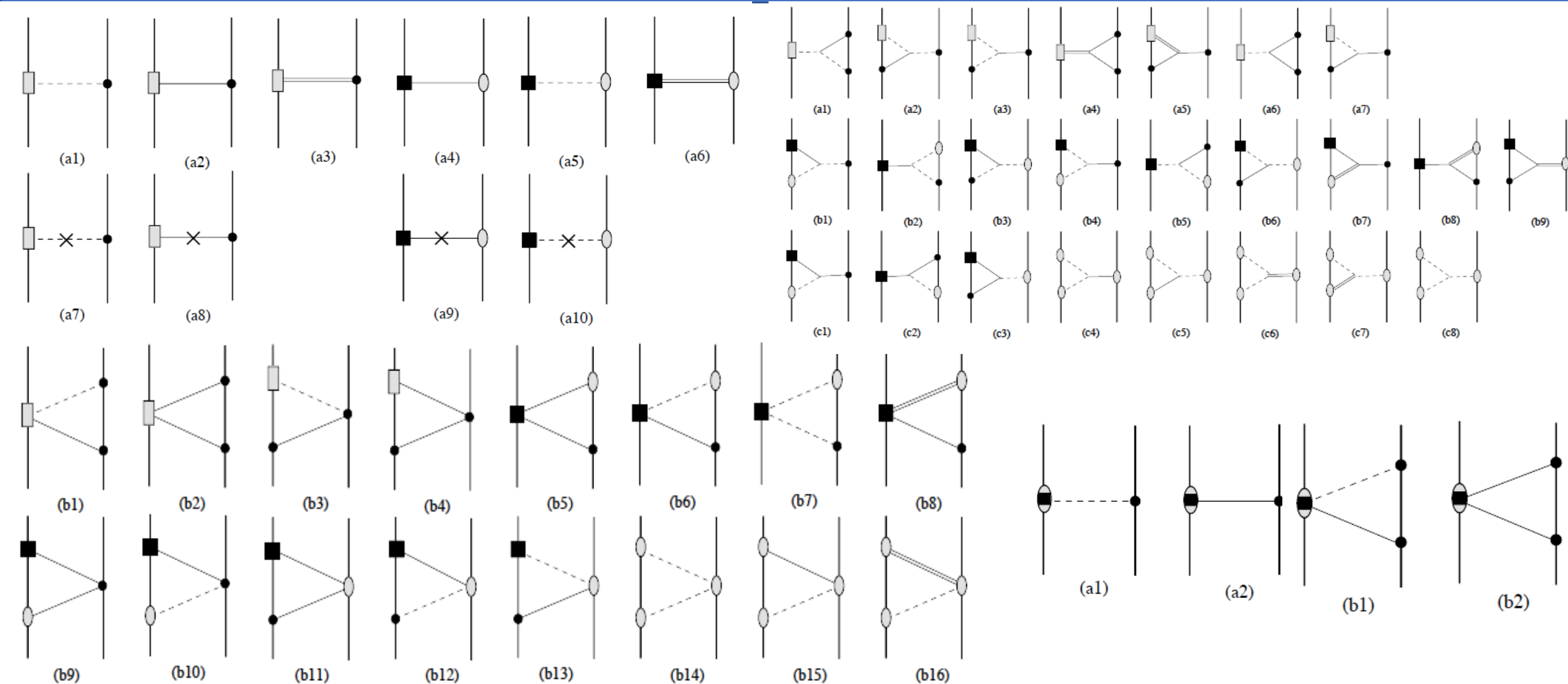
$$= \int dt \left[\frac{C_{ES^2}}{2m^2} S^i S^j \epsilon_{klm} S^m \phi_{,k} (A_{j,il} - A_{l,ij} - \delta_{ij} (A_{n,ln} - A_{l,nn})) \right]$$



$$= \int dt \left[-\frac{C_{ES^2}}{m^2} S^i S^j \epsilon_{klm} S^m \phi_{,k} (\phi_{,il} v^j - \delta_{ij} \partial_t \phi_{,l}) \right].$$

EFT of Post-Newtonian Gravity

Spinning Particle



EFT of Post-Newtonian Gravity

State of the art computation (Conservative Sector)

- Spin-less: **4 PN** [arXiv:1607.04252](#).
- Spin-less: **5 PN- static piece** [arXiv:1902.11180](#)
- Spin-Orbit at NNLO (**3.5 PN**) [arXiv:1506.05794](#)
- Spin-Orbit at NNLO (**4 PN**) [arXiv:1506.05794](#)
- Cubic in Spin interactions at NLO (**4.5 PN**)-M. Levi, **S.M.** et al [arXiv : 1912.06276](#)

Outline

Scattering Amplitudes and Post-Minkowskian expansion

By utilizing the powerful **on-shell techniques** (spinor-helicity formalism, generalized unitarity, BCJ relations etc), we can calculate both classical and quantum corrections:

- Higher order calculation of Post-Minkowskian expansion (needed for GW detectors)
- Inclusion of spin effects
- Inclusion of finite size effects
- Long-range quantum effects
- Modified gravity
- Supplementary computation to the Post-Newtonian expansion

Thank you for your attention

Outline

EFT of Post-Newtonian Gravity

By extending the computation to higher PN orders and spins:

- Tidal effects entering at 5 PN. Information about microphysics of internal structure
- Extension to radiation modes and non conservative sector
- Quantum corrections
- Modified gravity
- Supplementary computation to the Post-Minkowskian expansion