



Phase prediction under Taylor hypothesis using zonal models in LQG AO control



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High Performance control for AO systems



- Control loop delays:
 - WaveFront Sensor (WFS): Integration and read-out time
 - Controller: commands computation time







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Delays + High performance controller — > Turbulent phase prediction









• For prediction:









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Dynamical Phase models:

 \rightarrow MULTILAYER ATMOSPHERE WITH FROZEN FLOW HYPOTHESIS









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Phase basis well adapted to Frozen Flow models:

 \rightarrow ZONAL BASIS









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- Frozen Flow dynamical models in zonal basis:

$$\phi_{k+1} = h_{\mathrm{ff}} * \phi_k$$









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Well suited for highly parallelizable Distributed Kalman Filter (DKF) structure

Massioni & al, JOSAA 2011

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Frozen Flow models in zonal basis: good candidate for Linear Quadratic Gaussian (LQG) regulators towards ELT scale AO systems









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Sampling of one subaperture area	Strehl Ratio @ 1.65 μm
1 point / subaperture	42.2 %
4 points / subaperture	50.9 %
9 points / subaperture	51.7 %
16 points / subaperture	52.1 %









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	- 30		
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	10	9 points / subaperture	51.7 %
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9 16	-30		

- Better sampling improves LQG controller performance
- 4 points / subaperture enough to analyse performance









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• Frozen Flow hypothesis on turbulent phase model:

$$\phi_{k+1} = h_{\mathrm{ff}} * \phi_{k} \xrightarrow[N]{\text{THE TELESCOPE PUPIL}} \phi_{k+1}^{\mathrm{Tel}} = A^{\mathrm{Tel}} \phi_{k}^{\mathrm{Tel}} + A^{\mathrm{Edge}} \phi_{k}^{\mathrm{Edge}}$$

$$\phi_{k+1}^{\mathrm{Tel}} \xrightarrow[\phi_{k}]{\text{Tel}} \xrightarrow[\phi_{k$$







• Frozen Flow hypothesis on turbulent phase model:

$$\phi_{k+1} = h_{\mathrm{ff}} * \phi_{k} \qquad \longrightarrow THE TELESCOPE PUPPL \qquad \phi_{k+1}^{\mathrm{Tel}} = A^{\mathrm{Tel}}\phi_{k}^{\mathrm{Tel}} + A^{\mathrm{Edge}}\phi_{k}^{\mathrm{Edge}}$$

$$A^{\mathrm{Tel}} : \text{Part of } h_{\mathrm{ff}} \text{ inside the telescope pupil}$$

$$A^{\mathrm{Edge}} : \text{Part of } h_{\mathrm{ff}} \text{ outside the telescope pupil}$$

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$$No \text{ points outside telescope pupil} \rightarrow \phi^{\mathrm{Edge}} ?$$

























 $\phi_{\mathbf{k}+1}^{\mathrm{Tel}} = A^{\mathrm{Tel}}\phi_{\mathbf{k}}^{\mathrm{Tel}}$

2nd solution:

Static MAP estimation $\hat{\phi}_k^{Edge} = M^{Map} \phi_k^{Tel}$ MAP very local, need few points of ϕ_k^{Tel}















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New dynamical model compensating edge degradation under Taylor hypothesis

















ATMOSPHERE BEHAVIOUR	BOILING (3 layers)			FROZEN FLOW (1 layer)
Cn2 Profile (%)	0.5	0.2	0.3	1
Wind Values (m/s)	7.5	12.5	15	10
Wind Direction (°)	0	120	240	0
REPRESENTATION		.2 0.5		







Performance with edge compensation

• VLT NAOS-like case: Diameter = 8m, 15 x 15 actuators grid, ASO SH 14 x 14 ml, 500 Hz

Typical turbulence condition r0 = 0.1 m @ 0.55 μ m

Multilayer atmosphere reconstruction with LQG regulator







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Multilayer atmosphere reconstruction with LQG regulator

Strehl Ratio @ 1,65 µm:

Regulator & zonal basis	Edge	Atmosphere		
sampling	compensation	Boiling	Frozen Flow	
LQG, 4 points / subap area	none	52.5%	41.6%	
LQG, 4 points / subap area	MAP	53.6%	56.2%	
		0.2 0.5		









Performance with edge compensation

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	LQG, 4 points / subap area	none	52.5%	41.6%	
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Strong	degradation with pure Fre	ozen Flow	0.2 0.5		

• Edge compensation always effective





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Wind Values (m/s)	7.5	12.5	15
Wind Direction (°)	0	120	240
	0.2	0.3	5











ATMOSPHERE BEHAVIOUR	BOILING (3 layers)			MAI (NLY B 3 laye	OILING ers)
Cn2 Profile (%)	0.5	0.2	0.3	0.7	0.1	0.2
Wind Values (m/s)	7.5	12.5	15	10	7	15
Wind Direction (°)	0	120	240	IDE	im bo	ILING
	0.2 0.5		5		.1	0.7











ATMOSPHERE BEHAVIOUR	 (BOILING 3 layers	G s)	MAINLY BOILING (3 layers)		MAINLY FROZEN FLOW (3 layers)			FROZEN FLOW (1 layer)	
Cn2 Profile (%)	0.5	0.2	0.3	0.7	0.1	0.2	IDEM I	MAINLY B	OILING	1
Wind Values (m/s)	7.5	12.5	15	10	7	15	IDEM I	MAINLY B	OILING	10
Wind Direction (°)	0	120	240	IDE	M BO	ILING	0	60	-60	0
	0.2	0.3	5		.1	0.7		0.1	7	









ATMOSPHERE BEHAVIOUR	 (BOILING 3 layer:	G s)	MAI	NLY B 3 laye	OILING ers)	MAINL	Y FROZEN (3 layers	N FLOW)	FROZEN FLOW (1 layer)	/ FROZEN FLOW (1 layer)
Cn2 Profile (%)	0.5	0.2	0.3	0.7	0.1	0.2	IDEM I	MAINLY B	OILING	1	1
Wind Values (m/s)	7.5	12.5	15	10	7	15	IDEM I	MAINLY B	OILING	10	20
Wind Direction (°)	0	120	240	IDE	М ВО	ILING	0	60	-60	0	0
	0.2	0.3	5		.1	0.7		0.1			







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Typical turbulence condition r0 = 0.1 m @ 0.55 μ m

Strehl Ratio @ 1.65 µm

Regulator	Basis & sampling	Edge Compensation
Integral action	/	/
LQG - AR2	495 Zernike modes	/
LQG –AR1 multilayer	Zonal, 16 points / subap area	MAP







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Regulator	Basis &	Edge		ATMOSPHERE
	sampling	Compensation	Boiling	
Integral action	/	/	50.5%	
LQG - AR2	495 Zernike modes	/	53.7%	
LQG –AR1 multilayer	Zonal, 16 points / subap area	MAP	53.9%	
			0.2 0.5 0.3	
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Regulator	Basis & sampling	Edge Compensation	ATMOSPHERE				
			Boiling	Mainly Boiling			
Integral action	/	/	50.5%	50.6%			
LQG - AR2	495 Zernike modes	/	53.7%	53.7%			
LQG -AR1 multilayer	Zonal, 16 points / subap area	MAP	53.9%	54.4%			
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	sampling	Compensation	Boiling	Mainly Boiling	Mainly Frozen Flow	
Integral action	/	/	50.5%	50.6%	50.3%	
LQG - AR2	495 Zernike modes	/	53.7%	53.7%	53.6%	
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Regulator	Basis &	Edge Compensation	ATMOSPHERE				
	sampling		Boiling	Mainly Boiling	Mainly Frozen Flow	Frozen Flow 10 m/s	
Integral action	/	/	50.5%	50.6%	50.3%	50.7%	
LQG - AR2	495 Zernike modes	/	53.7%	53.7%	53.6%	53.8%	
LQG –AR1 multilayer	Zonal, 16 points / subap area	МАР	53.9%	54.4%	55.5%	56.8%	
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			Boiling	Mainly Boiling	Mainly Frozen Flow	Frozen Flow 10 m/s	Frozen Flow 20 m/s	
Integral action	/	/	50.5%	50.6%	50.3%	50.7%	46.4%	
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LQG-KF with Frozen Flow models and MAP compensation is efficient









• Multilayer Frozen Flow models:

+ multilayer atmosphere model \rightarrow High performance control









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 - + Highly parallelizable structure \rightarrow Fast and well adapted to ELT scale AO









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 - + Very local edge compensation with MAP \rightarrow Highly parallelizable and efficient









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 - + multilayer atmosphere model \rightarrow High performance control
 - + Highly parallelizable structure \rightarrow Fast and well adapted to ELT scale AO
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LQG regulator with multilayer Frozen Flow models and edge compensation with MAP:
 + Competitive and better than AR2 Zernike LQG regulator for any atmosphere behavior









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 - + Highly parallelizable structure \rightarrow Fast and well adapted to ELT scale AO
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- LQG regulator with multilayer Frozen Flow models and edge compensation with MAP:
 + Competitive and better than AR2 Zernike LQG regulator for any atmosphere behavior
 - Only tested with full knowledge of atmosphere and wind profiles









• Robustness in performance in the presence of model errors









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- Extension of control strategy and edge degradation study to ELT-sized systems









- Robustness in performance in the presence of model errors
- Extension of control strategy and edge degradation study to ELT-sized systems
- LQG with edge compensation efficient with Frozen Flow atmosphere:
 + well adapted to high altitude layers with strong wind
 + interesting for satellites tracking





